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When education policy and housing policy interact: can they correct for the externalities?

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When education policy and housing policy interact: can they correct for the externalities?

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Abstract

A simple spatial equilibrium model with the peer group effect and local public finance can match several stylized facts of the labor market and housing market in the United States. Our counter-factual policy analyses generate further insights. First, the welfare of households can change as the government varies the location of public housing units with a neighborhood. Second, even though the public housing policy and housing voucher program deliver similar results at the household level, they are different as the former tends to benefit the offspring more, while the latter is the reverse. Third, combining school finance consolidation policy with public housing policy can lead to a Pareto improvement. Unfortunately, a policy that can benefit all agents, in the long run, may not be implemented as it can hurt some agents in the short run.

JEL Classification: H00; I20; R00

Keywords: school finance consolidation, public housing, housing voucher, endogenous sorting mechanism, short-run rigidity versus long-run flexibility.

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"For most children in the U.S., where you live determines where you go to school... As of the 2008-2009 school year, 11 percent of children went to private schools, approximately 3 percent of U.S. public school students attended charter schools, and another 5 percent attended magnet schools. Only 1 percent of public school students enrolled in different school district through interdistrict choice programs, even though 46 percent of school districts reported offering such a program." extracted from Schwartz (2013, p.24~25)

1 Introduction

Intergenerational rigidity in income is high in the United States.¹ One percent increase in parental income is associated with around a 0.5 percent increase in offspring's earnings (Solon, 1999; Black and Devereux, 2011). A child from an economically adverse family grows into a rich adult is unlikely (Chetty and Hendren, 2018; Currie and Almond, 2011; Hanushek and Yilmaz, 2011). The practice of "local public finance" may contribute to the intergenerational persistence, as the competitions for housing in well-funded school districts drive up house prices, and drive out relatively low-income families. As a result, offsprings from those families would receive lower-quality education and remain to be poor as they grow up.²

This paper focuses on the housing policies and how it could impact the labor market outcomes and educational attainments of children under local public finance. As an example, some recent research suggests positive impacts of public housing policy (Currie and Yelowitz, 2000; Olsen and Ludwig, 2013). On the other hand, public housing policies impose additional tax burdens on non-participants, which might induce non-participants (who constitute the majority of the economy) to vote against these policies. Thus, we ask whether it is possible to design a Pareto-improving policy, which promotes the quality of children from economically adverse families while keeping the welfare of other households from declining.

Casual observations suggest that the housing and education markets are imperfect, and hence Pareto-improving policy is potentially feasible. For instance, the same quality of public education is provided to heterogeneous agents within the same communities at zero price through the local public finance practice. Moreover, empirical research supports the existence of the "peer group effect" in education, which is a form of externality (Sacerdote, 2011; Stinebrickner and Stinebrickner, 2006).

Therefore, this paper adopts the Hanushek-Yilmaz (HY, henceforth) framework which incorporates all the externality and market imperfection discussed above.³ In an HY economy, there are multiple ex-ante identical districts, each of which finances its school using property taxes collected from its residents. Both the per-student education spending and peer quality affect the school quality in a district. Households choose among the districts for residence, given the school quality and property tax rate pair (Tiebout, 1956). Within a district, households also balance the tradeoff between commuting costs and possible spatial differentiation in rents to decide the exact location (Alonso, 1964). The inclusion of the spatial elements in HY also allows us to discuss the optimal location of public housing units within the city. Thus, the HY framework links the housing market

¹Throughout this paper, we will use the term "intergenerational rigidity" and "intergenerational persistence" interchangeably.

²The average level of housing costs in household budgets is around 20% in the United States, which is similar to the average figure (18%) in the OECD countries.

³Papers adopting this framework includes Hanushek et al. (2011), HY (2007, 2013, 2015), and Leung et al. (2012).

and education through local public finance, embedding the peer group effect and spatial elements in a unifying framework. Since different districts are identical ex-ante, one can easily attribute the equilibrium effect due to self-selections as well as policy changes.

Our contribution hinges on making two realistic modifications to the HY framework and shows that a Pareto-improving policy would then be possible. First, we allow the parental investment in offspring quality to differ across households. We explicit model the intra-household allocation in terms of goods and residence space, which enables us to separate the implications of various policies on the adult members and the children in the same household. Second, we model the peer group effect as a function of the average quality of the peers (e.g., Blume and Durlauf, 2006). It provides a robustness check to the useful computational shortcut adopted by existing HY papers, namely, the peer group effect depends only on the community composition. In our setting, parents explicitly make the location choice, the fertility choice, and the investment decisions in offspring, and hence, an alternative formulation of peer group effect may be appropriate.

Since there are discrete choices (e.g., which community to live) and externalities (e.g., peer group effect, public education budget), a direct estimation may not be straightforward. Therefore, we follow HY and calibrate our model to match several stylized facts of the U.S. economy circa 2010, which enables us to "identify" parameter values that might not be directly observed and ensures that our model is consistent with those stylized facts. The rent-distance gradient generated by the calibrated model is found to be close to the one estimated in some empirical literature, which adds to the credibility of the model. Based on our calibration, a school finance consolidation can lead to an improvement of the aggregate welfare, which is in contrast to the results in HY (2007, 2013). On the other hand, building public housing units for the poor can improve their well-being and the quality of their offspring at the cost of hurting the rest of the economy. The average welfare also declines as location choices are restricted, and the incentives to work are distorted. Also, we show that a combination of the school finance consolidation and public housing can be both effective (aiding the poor) and efficient (Pareto-improving). We provide more discussion and intuition in a later section.

On top of the discovery of an effective and efficient policy package, our policy experiments yield additional results. First, it is better to locate the public housing units on the "edge of the city," i.e., the land would not be occupied in the absence of the public housing program because the construction of public housing would not reduce the amount of accessible land and would face less political resistance. Second, on the household level, housing voucher provides similar welfare results as public housing policy does. Adequately designed public housing policy can induce a better peer group effect at the more impoverished community. However, children in low-income families can benefit while their parents could suffer. Under the housing voucher program, the opposite is exact in the sense that less-educated parents gain at the cost of welfare loss of their offspring. We also compare the welfare implications for the short-and long-run effects of public policies in the context of our model and find that there is a possibility of time inconsistency. To our knowledge, such comparison is relatively rare in the spatial general equilibrium literature and hence would hopefully enrich our understanding.

The rest of the paper is organized as follows. We first present a modified version of the HY model and deliver the baseline results. The model-generated rent gradients are compared with the empirical findings as a validity test of the model. We then analyze the welfare consequences of consolidating school finance and introducing various housing policies. Both short- and long-run effects are discussed. The final section concludes the paper. We present the technical details in the appendix.

2 The Model

We first provide an informal overview of the model, where our subsequent policy analysis would be based. Our model modifies the pioneering work in HY (2007), which combines the insights of Tiebout (1956) and Alonso (1964) in a multi-district spatial model. Our monocentric city is composed of two jurisdictions, East (E) and West (W), with a boundary at the Central Business District (CBD) and three household types (low, medium, and high skill). Households consume housing, a non-housing good, and leisure, but also invest in their children directly (by purchasing housing and non-housing goods for them) and indirectly (through taxes that fund schools). School funding and peer effects jointly determine school quality, and the school funding itself is determined by endogenous jurisdiction-specific property taxes, and peer effects are determined by jurisdiction-specific average educational outcomes. Parents have preferences over (the endogenous) quantity and quality of children. For the sake of simplicity, we assume that a family is formed via assortative matching, and choices are made by parents to maximize the utility of the whole household.

2.1 The General Set-up

Our formal model is a variant of the HY framework, with an elaborated form of parental altruism.⁴ Parents' well-being Ω_p depends on the amount of goods Z_p and lot sizes S_p that they consume and by how much leisure time $l \in [0, 24]$ they enjoy. Parents care about both the well-being of each offspring Ω_o^j and the quantity n_o of their offspring, where j is the community the family chooses to live (Becker, 1991; Hanushek, 1992). The well-being of each offspring Ω_o^j depends on both the public inputs, i.e., the education quality in community j, q_j and private inputs, i.e., the amount of consumption goods Z_o and the residential space S_o (Goux and Maurin, 2005; Gertler et al., 2004). We also assume that the marginal utility derived from the number of offspring declines as the fertility rate n_o increases. $g(n_o)$ measures the degree of altruism shown toward each child. Following HY (2007, 2013) and others, we assume the utility function of households to be in the Cobb-Douglas form.⁵ Formally, the utility function of a typical household in district $j \in \{W, E\}$ is

$$U(S_p, Z_p, l, S_o, Z_o, n_o) = (\Omega_p)^{k_p} (\Omega_o^j)^{k_o} n_o g(n_o)$$

$$\tag{1}$$

where $\Omega_p \equiv (S_p^{\alpha_p} Z_p^{\beta_p} l^{\eta})$, $\Omega_o^j \equiv q_j^{\gamma} S_o^{\alpha_o} Z_o^{\beta_o}$, $g(n_o) \equiv g n_o^{-\epsilon}$, with the restrictions on parameters that $\alpha_p + \beta_p + \eta = 1$, $\gamma + \alpha_o + \beta_o = 1$, $k_p + k_o = 1$, $\epsilon < 1$. The parameters k_p and k_o capture the relative importance of the parent part and the offspring part, respectively.

We now describe the budget constraint faced by the household. Consider a household located r miles away from the CBD. The two parents earn all the income for the whole family. w represents the sum of their hourly wages. The parents allocate the hours in their days to work, leisure (l hours), rearing offspring ($C(n_o)$ hours), and commuting (br hours), where b is the time cost per mile of their daily round-trip commute. For simplicity, we assume that $C(n_o) = cn_o$, where c is a constant. Hence, the total income of this household is

$$Income = [24 - l - C(n_o) - br]w.$$

⁴See also Becker and Barro (1988). Alternatively, we can assume that parents care about the utility of their children. However, given the non-intergenerational nature of the model, the two formulations are observationally equivalent.

⁵There are several merits of assuming the Cobb-Douglas form utility function. Previous studies use that as well, and hence we can easily compare our results with them. The Cobb-Douglas form is tractable. The expenditure share of each good is fixed, which seems to be consistent with the evidence (Davis and Ortalo-Magne, 2011).

The parents use their income to purchase consumption goods and pay for housing rents. We normalize the price of the composite consumption goods as unity. We assume that the daily round-trip commuting costs total of ar dollars. Formally, the total expenditure is

$$Expenditure = (S_p(r) + n_o(r)S_o(r))(1 + \tau_j)R_j(r) + Z_p(r) + n_o(r)Z_o(r) + ar.$$

Since our formulation deviates slightly from the literature, we provide a brief explanation of the Expenditure. Recall that the amount of space consumed by the parents is $S_p(r)$, and the amount of space by each offspring is $S_o(r)$. For a household with $n_o(r)$, the total amount of space demanded is $(S_p(r) + n_o(r)S_o(r))$. Given the daily unit rent $R_j(r)$ and the property tax rate τ_j in the location r, the after-tax expenditure on space is therefore $(S_p(r) + n_o(r)S_o(r))(1 + \tau_j)R_j(r)$. The total expenditure on consumption goods of this family is $Z_p(r) + n_o(r)Z_o(r)$. Notice that we include all these variables to be a function of r, reflecting the possibility that the consumption of space and consumption goods could depend on the location of residence. Our budget constraint then equates the Income to the Expenditure. We reserve the details in the appendix.

2.1.1 Household Heterogeneity

In practice, households differ in many dimensions. In this paper, we focus on the differences in income and preference on offspring quality and examine the empirical implications with such limited degrees of heterogeneity. Table 1 shows that in data, more highly educated parents on average have higher earnings and lower fertility rates. Hence, they have more resources to spend on fewer children, which makes the quality of their offspring even higher. Guided by these stylized facts, we classify the households in the model according to the educational attainment of their adult members and calibrate our model accordingly. For simplicity, we assume that there are three types of households: "Not a High school graduate" (NH), "High School to associate degree" (HA), and "Bachelors degree or above" (BA). We further assume that a family is formed with assortative matching and hence, that both of the two adults (wife and husband) have attained the same level of educational attainment in a given household.⁶ Our assumption that $w_{NH} < w_{HA} < w_{BA}$ is consistent with the U.S. data indicating that higher educational attainment leads to higher wage income on average.

The second dimension of heterogeneity among parents is the quality-quantity tradeoff of offsprings (Becker, 1991; Hanushek, 1992). In our model, a higher value of k_o means that the parents care more about the quality of their offspring than the number of offsprings they have. To capture the fact that adults who attain a higher level of education tend to bear fewer children, we assume that $k_o^{NH} < k_o^{BA} < k_o^{BA}$. With three types of agents and only two communities involved, we have imperfect sorting, which is also consistent with the empirical evidence (Davidoff, 2005; Hardman and Ioannides, 2004).

⁶In practice, marital sorting is not as extreme. According to Fernandez et al. (2005), the cross-country average of assortative matching regarding spouse education level is about 0.6. For a review of the literature and new evidence for assortative matching in marriage, see Bruze (2011), among others.

⁷There are at least two ways to interpret the assumption that income is correlated with parents' degree of altruism. According to the warm-glow theory (Andreoni, 1990), a higher income leads to a higher degree of altruism. Chowdhury and Jeon (2014) conduct a field experiment (dictator and recipient) and find support for the warm-glow theory. The second interpretation is that less-educated parents may be less informed on how to "invest" in their offspring.

For a survey of the altruism literature, see Laferrere and Wolff (2006), among others.

2.2 Basic Analysis of the Equilibrium

In this section, we define and characterize the equilibrium of our model. Our analytical characterizations, which hold for a broad and reasonable set of parameters, seem to be broadly consistent with the empirical evidence. Hence, they provide some validity of our model. These characterizations also assist our calibration in a later section.

2.2.1 Bid-rent Functions and Market Rent Curves

Like many spatial equilibrium models, all households bid for land on a featureless plane. Therefore, we solve for the bid-rent function, which expresses a household's willingness to pay for a given utility level \overline{u} . For a type $i \in \{NH, HA, BA\}$ household living in district $j \in \{W, E\}$, the maximization problem can be expressed as follows:

$$\psi_{i}(r, \overline{u}_{i}, q_{j}, \tau_{j}) = \max_{S_{p}, S_{o}, Z_{p}, l, Z_{o}, n_{o}} \left\{ \frac{Y_{i}(r) - Z_{p} - n_{o}Z_{o} - w_{i}l - w_{i}cn_{o}}{(1 + \tau_{j})(S_{p} + n_{o}S_{o})} | U_{i}(.) = \overline{u}_{i} \right\}.$$
(2)

Solving this maximization problem, we obtain the following bid-rent function,

$$\psi_i(r, \overline{u}_i, q_j, \tau_j) = \frac{1}{1 + \tau_j} \left\{ \frac{K_i q_j^{\gamma k_o^i} Y_i(r)^{k_T^i}}{\overline{u}_i} \right\}^{\frac{1}{k_S^i}}, \tag{3}$$

and the following bid-max lot size function

$$S_{i}(r,\overline{u}_{i},q_{j},\tau_{j}) = S_{p}^{i}(r,\overline{u}_{i},q_{j},\tau_{j}) + n_{o}S_{o}^{i}(r,\overline{u}_{i},q_{j},\tau_{j}) = \frac{Y_{i}(r)}{\psi_{i}(r,\overline{u}_{i},q_{j},\tau_{j})} \frac{k_{S}^{i}}{k_{T}^{i}} \frac{1}{1+\tau_{j}},$$

$$(4)$$

where K_i , k_T^i , k_S^i , k_n^i are functions of parameters. (Interested readers may refer to the appendix for details).

In the model, all of the lands are rented out via auctions. All three types of households and agricultural workers can bid for any location (r,j).⁸ For each location, the right of usage goes to the agent who offers the highest bid. Therefore, the equilibrium rent curve $R_j(r)$ is the upper envelope of the bid rent curves $\psi_i(r, \overline{u}_i, q_j, \tau_j)$ of the three types of households and the agricultural rent R_a . As the household moves away from the CBD, its bid rent declines due to the transportation cost. It means that beyond a certain distance R_{jf}^* , the agricultural rent R_a dominates the bids offered by all of the households in the economy. Hence, no one resides there. Within the fringe distance R_{jf}^* , the spatial order of two adjacent types of households is determined by the relative steepness of their bid rent curves at the intersection point. The one with the steeper curve resides closer to

⁸ Following the urban economics literature, the agricultural workers are assumed to be self-sustained, except for the participation of the land auction. They would not affect any other aspect of the model economy.

the CBD. In other words, the condition for the equilibrium location of Household 1 being further from the CBD than that of Household 2 is $\frac{\partial \psi_1(\cdot)/\partial r}{\partial \psi_2(\cdot)/\partial r} < 1$. Furthermore,

$$\frac{\partial \psi_i(\cdot)}{\partial r} = -\psi_i(r, \overline{u}_i, q_j, \tau_j) \frac{k_T^i}{k_S^i} \frac{a + bw_i}{Y_i(r)}.$$

Based on these observations, the following proposition becomes intuitive (all proofs are included in the appendix):

Proposition 1 If $\alpha_o > \alpha_p$, then in each neighborhood, households with better-educated adults live further from the CBD at the equilibrium.

There are opposing forces on the households' location choice. As long as $\frac{k_T^2}{k_S^2} > 1$ (which is true given $\alpha_o > \alpha_p$), $S_i(r,u,q_j,\tau_j)$ is increasing in the distance to CBD r. Thus, the income effect of a higher wage creates more demand for lot size consumption and induces the household to live farther away from the CBD. However, higher hourly wages also increase the opportunity cost of commuting time. This substitution effect generates an incentive for the parents to live closer to the CBD and therefore spend less time on commuting. In our model, the income effect always dominates. Thus, a higher wage income and a stronger preference for the quality of their offspring drive better-educated parents to reside farther away from the CBD. This prediction is consistent with a long-lasting stylized fact in the United States that the nation's poor are more likely to reside in central areas of cities. In the year 1990, the majority (59%) of the poor poverty area residents lived in central cities. 28% and 13% of them resided in outer-metropolitan areas and suburban areas, respectively (Bureau of the Census, 1990).

2.2.2 Population and Fertility Decision

Following the literature, the total number of households for each type $i, i \in \{NH, HA, BA\}$, is exogenously given at $\overline{N_i}$ in this model. However, the total population is endogenous as the fertility choice is endogenous. We focus on the fertility choice in this section. Suppose that in equilibrium, the locations r miles away from the CBD in district j are occupied by type i households, where $j \in \{W, E\}$. Let L(r) represent the amount of land available per unit distance, at distance r. Because the whole land is equally divided into two districts, $L(r) = \frac{1}{2}2\pi r = \pi r$ in each district. The land market is cleared, which means that within the fringe distance D_{jf}^* , $L(r) = S_i(r, u_i^*, q_j, \tau_j) m_i^j(r, u_i^*, q_j, \tau_j)$, where $m_i^j(r, u_i^*, q_j, \tau_j)$ is the equilibrium number of households per unit distance in district j assuming that distance r is occupied by type i household and u_i^* is the equilibrium utility of type i household. We introduce the function $t_j^*(r)$ to indicate the type of the residents at distance r of district j. All of the households find locations at which to reside, implying the following population constraint:

$$\int_{0}^{\infty} m_i^W(r, u_i^{\star}, q_W, \tau_W) I[t_W^{\star}(r) = i] dr + \int_{0}^{\infty} m_i^E(r, u_i^{\star}, q_E, \tau_E) I[t_E^{\star}(r) = i] dr = \overline{N}_i , \qquad (5)$$

where I[.] is an indicator function that takes the value 1 when the condition in the bracket is satisfied and 0 otherwise, $i \in \{NH, HA, BA\}$. It is easy to verify that the household number distribution

function in district j is

$$m^j(r) = \sum_{i \in \{NH, HA, BA\}} m_i^j(r, u_i^{\star}, q_j, \tau_j) I[t_W^{\star}(r) = i].$$

The total population in this economy consists of adult and child populations, where the latter is endogenous. We denote $n_o^{ij}(r)$ to be the fertility choice of type i parents in district j, located r miles from the CBD. The solution of (2) suggests that

$$n_o^{ij}(r) = n_o^i(r) = \frac{k_n^i}{w_i c k_T^i} Y_i(r)$$
, which is independent of district j .

Therefore, the offspring population located r miles from the CBD and in district j is

$$m_o^j(r) = \sum_{i \in \{NH, HA, BA\}} n_o^i(r) m_i^j(r, u_i^\star, q_j, \tau_j) I[t_j^\star(r) = i].$$

Proposition 2 If $\gamma < \frac{1}{2-\epsilon}$, then parents who care more about their offspring's quality bear fewer children, other things being equal.

$$\frac{\partial n_o^i(r)}{\partial k_o^i} < 0.$$

This proposition is rather intuitive. Parents who care more about their offspring lean more heavily towards children's quality in the quality-quantity trade-off, hence bear fewer children. Together with our assumption that more altruistic adults have higher wage income, this proposition implies a negative income-fertility relationship, which is in line with the data.

2.2.3 Property Taxes, Student Quality Dependent Peer Effect and School Quality

In the previous section, households take the school quality of each district as given in their location choice. In this section, we show how the peer group effect and school quality in each district are determined. Recall that each of the two districts finances its school through the property taxes placed on the residential land within that district. Because they do this independently, the education quality and property tax rate packages (q_j, τ_j) may differ between the two districts. As in the U.S., the publicly funded schools in our model are only open to the residents in the same districts and do not charge any tuition fees. The local government of district j would have the following budget constraint:

$$X_j N_o^j = \tau_j \int_0^{D_{jf}^*} R_j(r) L(r) dr, \tag{6}$$

where N_{oi}^{j} is the population of children from type i household in jurisdiction j, $N_{o}^{j} = \sum_{i \in \{NH, HA, BA\}} N_{oi}^{j}$

is the total population of the children in jurisdiction j, X_j is expenditure per student in district j and τ_j is the property tax rate. Thus, (6) states that the total expenditure on students $X_j N_o^j$

needs to be financed by the local property tax collected within the district $\tau_j \int_0^{D_{jj}^*} R_j(r)L(r)dr$.

In this model, the (local) education quality q_j has two determinants. First, a higher value of X_j means that the local school can afford better instructional facilities and instructors and hence provide better education quality q_j . Second, a higher value of the peer group effect Π_j , which means having more qualified peers impact a student's educational achievement positively via several channels. For instance, students may learn from their classmates during group works or even casual interactions. Competing with well-educated peers in school may also induce a student's motivation to study. Following the HY (2007, 2013), we assume that the quality is the product of expenditure and peer group effect,

$$q_j = X_j \Pi_j. (7)$$

Notice that neither school quality nor peer quality has natural units. Therefore, we can renormalize them so that (7) holds.

We now turn to the determination of peer group effect in the community, Π_j , $j \in \{W, E\}$. Some previous studies assume that the peer group effect is a function of the population composition (HY, 2007, 2013). A greater proportion of skilled adults in the total population generates a higher positive peer effect. Such formulation captures the ideas that (1) family has a significant effect on student performance and (2) the abilities of parents and children are positively correlated. However, this formulation implicitly assumes that the parental investment on offspring is identical across households, and hence the population composition would be sufficient to capture the peer group effect. This paper relaxes this assumption and allows parental investment to be an endogenous decision. Hence, in this paper, the peer effect is a function of the average quality of all of the students in the community (Blume and Durlauf, 2005; Liu et al., 2014; Sacerdote, 2011). This formulation captures the quality-dependent nature of peer effects, while it remains simple enough to be implemented in a spatial general equilibrium model with many distortions. Following HY (2013), we assume a similar functional form of $\Pi_j(\overline{\Omega_j^j})$,

$$\Pi_j(\overline{\Omega_o^j}) = c_1 + c_2 \exp(\overline{\Omega_o^j}), c_1, c_2 > 0, \tag{8}$$

where $\overline{\Omega_o^j}$ is the average quality of all of the students in the community, whose details are provided in the appendix. Given our formulation, it is straightforward to show the following:

Proposition 3 In each neighborhood, better-educated adults produce offspring with higher quality.

This proposition is intuitive. Parents with higher education levels have several advantages in producing higher quality offsprings. They earn higher wage incomes, have fewer children, and spend a more substantial proportion of those incomes on each child. As a result, the expenditure per child increases. Moreover, as these households live farther away from the CBD, where land rents are much cheaper, they can afford larger lot sizes with the same amount of expenditure, which contributes to the quality of their offspring. This proposition also agrees with the perceived high intergenerational correlation of income-education in the United States.

To close the model, we now describe how the property tax rate τ_j is determined. All of the adults (parents) in district j have the right to vote for their preferred tax rate. Hence, the preferred property tax rate of a particular household i is the tax rate which maximizes the utility, subject to

⁹Following Nechyba (1997, 2003), parents are assumed to be "myopic" when voting and do not consider the implications of their votes on the population composition, land prices and the peer effects in either communities.

all the constraints. Formally, it is the solution to the following maximization problem,

$$\max_{\tau_j^i} V_i(.) = \frac{K_i q_j^{\gamma k_o^i} Y_i(r)^{k_T^i}}{\left[(1 + \tau_j^i) R_j(r) \right]^{k_S^i}},$$
subject to $q_j = X_j \Pi_j$ and $X_j = \tau_j^i \overline{R_j}$, (9)

where $\overline{R_j}$ is the total rent collected in community j. Its detailed expression is presented in the appendix. The solution takes the following simple form,

$$\tau_j^i = \gamma k_o^i / (k_S^i - \gamma k_o^i) = \gamma k_o^i / (\alpha_p k_p^i + \alpha_o k_o^i - \gamma k_o^i). \tag{10}$$

Furthermore, the calibrated set of parameters ensures that τ_j^i is positive for all three types of households.

2.2.4 Stationary Equilibrium

We are ready to define the general equilibrium of this model economy. In the stationary equilibrium, no household has an incentive to relocate after the voting outcome is realized and observed. It can be formally defined as follows:

Definition 1 An equilibrium is a set of utility levels $\{u_{NH}^{\star}, u_{HA}^{\star}, u_{BA}^{\star}\}$, market rent curves $\{R_W(r), R_E(r)\}$, school quality and property tax rate pairs $\{(q_W, \tau_W), (q_E, \tau_E)\}$, household number/offspring population distribution functions $\{(m^W(r), m_o^W(r)), (m^E(r), m_o^E(r))\}$ and type functions $\{t_W^{\star}(r), t_E^{\star}(r)\}$ that show the equilibrium occupant of the location at distance r in district j, producing the following results

- The households offer their bids according to equation (3). The land is rented out through auction. The household that offers the highest bid wins a particular location if the bid is higher than the agricultural rent. Otherwise, the land is left for agricultural use.
- Each household rents a certain amount of land according to equation (4). The land market clears, and the population constraint (5) holds.
 - Households of the same type attain the same utility level.
- Each jurisdiction finances its school through property taxes placed on residential land. The property tax rate is determined by majority voting (9). The local government budget balances in all districts, (6).
- School quality depends on both per-student spending and the peer effect, which is a function of the average quality of the children (8).
- All of the adults commute to the CBD for work and earn wage income according to their types. Commuting presents both monetary and time costs.

2.3 Calibration

2.3.1 Parameter Set

We calibrate the stationary equilibrium of our baseline model to match a large set of stylized facts from the U.S. statistics circa 2010. We divide the parameters of our model into three categories, which are (1) budget constraint parameters w_i , a, b and c, (2) preference parameters α_p , β_p , η , α_o ,

 β_o , γ , k_o^i , k_p^i , and ϵ , and (3) macroeconomic environment parameters R_a , \overline{N}_i , c_1 and c_2 . Below we describe the calibration of each category of parameters.

We start with the budget constraint parameters. Because we assume that the two parents in one household attain the same level of education, the target wage income of the household type $i \in \{NH, HA, BA\}$ is the twice the wage income of a type i agent. Hence, the average annual earnings of type NH, HA, and BA households are about \$51,432, \$87,479, and \$155,013, respectively (U.S. Census Bureau, 2009). Based on the U.S. Department of Labor, the daily work time is around 7.64 hours, and hence we set the hourly wages to be $w_{NH} = 20$, $w_{HA} = 32$ and $w_{BA} = 55$, accordingly. The monetary cost of commuting per mile in our city is about \$0.55. In a household in which two adults commute to work, the total round-trip pecuniary cost per mile is $a = 2 \times 2 \times \$0.55 = \2.2 . Assuming the commuting speed in the city is 20 miles per hour, we set b = 0.1. Zick and Byrant (1996) estimate that each parent in a wife-husband family with two children spends an average of about $1.3607^{\circ}1.5110$ hours on childcare every day. To mimic this fact, we choose $c = \frac{1}{2} \left(\frac{1.3607 + 1.5110}{2} \right) = 0.7179$.

We then describe how we calibrate the preference parameters. Since we have imposed the restrictions that $\alpha_p + \beta_p + \eta = 1$, $\gamma + \alpha_o + \beta_o = 1$ and $k_p^i + k_o^i = 1$, there are six free parameters to be calibrated. We jointly choose values for these six parameters such that the baseline economy approximates a list of "stylized facts" of the U.S. economy. In particular, we target the follow-

ing six moments: (1) share of total expenditure on children, (2) share of total expenditure on housing, (3) share of children's expenditure on housing, (4) share of total "budget" on leisure, (5) preferred property tax rate¹¹, and (6) fertility rate. Table 2 summarizes these moments and their corresponding expressions in our model. It shows that the model counterpart of each of these six moments is almost always a function of a subset of the preference parameters. The only exception is the fertility rate, which also depends on budget constraint parameters that are already chosen in previous steps. Therefore, for each of the three types of households, the preference parameters can be determined as the solution to a six-equation, six-unknown equation system. The calibrated preference parameters are reported in Table 3a.

The last set of parameters to be determined are the macroeconomic environment parameters, i.e., agricultural rent R_a , number of household \overline{N}_i and peer effect parameters c_1 and c_2 . We fix the total number of households at 500,000. In the data sample, we have access to about 10%, 55%, 35% of the mothers are of NH, HA, and BA types, respectively. We assume that this ratio also applies to the fathers and expect the proportion of college graduates to be slightly higher in cities than in the national survey. Hence, we set the ratio of NH, HA, and BA type households to be 10%, 50%, and 40%, respectively. Given the total number of households, agricultural rent R_a determines

 $^{^{10}}$ We choose to match the national average hourly wages because, for each of the three types of households, the average hourly wage for urban residents is fairly close to the average hourly wage for the overall population. For NH and HA households, this is the case because they do not enjoy large urban wage premium. For BA household, this is the case because the vast majority (around 90%) of college graduates live in the urban area.

¹¹In the model, the property tax rate is the fraction of rents that are collected by local government. In reality, property taxes are typically based on the value of the house, which can be computed as rents divided by interest rate inte = 0.025. Hence, in the numerical section, we report the property tax rate as the fraction of house value that is collected by the local government instead. Mathematically, this property tax rate is equal to $\frac{\gamma k_o^i}{inte(\alpha_p k_p^i + \alpha_o k_o^i - \gamma k_o^i)}$.

the size of the city. The lower R_a is, the larger the city is. We set agricultural rent $R_a = \$1, 237$ per acre per month to match the endogenous calibration targets for the fringe distance, which is around $10^{\sim}15$ miles. The peer effect parameters c_1 and c_2 determine the demographic composition of the two communities. We normalize $c_2 = 1$. We show in the appendix that, the larger c_1 is, the stronger the sorting pattern is. We set $c_1 = 10$ to match the endogenous target that over 70% of the BA type households reside in and constitute the majority of the $West.^{12}$

Table 3b shows that our baseline model can *simultaneously match* some key statistics about family, the labor market, and the housing market reasonably well despite its simplicity.

(Table 3b about here)

2.3.2 Baseline Equilibrium

This model has multiple equilibria. We focus on the asymmetric equilibrium, which is the stable one.¹³ It also permits us to discuss cross-district sorting, which is related to the tradeoff between parents' well-being and offspring quality. We summarize the baseline equilibrium outcomes in a series of tables and figures. Figure 1a shows that the market rents decline as the households move away from the CBD. Richer families take advantage of the lower housing rents in remote areas to purchase larger lots. Hence, a household's lot size increases along with its distance from the CBD, as shown in Figure 1b. In each district, the NH type agents, who have the lowest wage income, live the closest to the CBD, followed by HA (middle-income) and BA (richest) types. This spatial allocation of the population is a feature of the standard Alonso-Muth model (Alonso, 1964; Muth, 1969), which describes a spatial structure similar to many U.S. metropolitan cities. Figure 1c shows that population density decreases as residents move toward suburban areas. Two economic decisions made by households drive this spatial pattern. A household's lot size increases with its distance from the CBD. Moreover, richer families who tend to live further away from the city center also tend to have fewer offspring.

The three types of households also differ in other ways. Table 4a and the "Baseline" column of Table 3b together indicate that parents who attain a higher level of education have higher incomes, achieve a higher level of well-being, and tend to bear and rear fewer offspring of more top quality. The differences in parents' well-being are much smaller than the differences in offspring quality. Better-educated parents earn higher incomes, spend a more substantial proportion of their incomes on their children's consumption, and bear fewer offspring, consequently increasing the expenditure per child. They also choose to live further away from the CBD, which allows them to provide more consumption and more space for each child. All of these effects work together and magnify the difference in offspring quality Ω_o across households. However, the results of higher education levels

¹²We choose 70% as the target because it is approximately the lowest fraction to ensure that skilled (BA type) workers can constitute the majority of the West community and determine the property tax rate. In the appendix, we perform robustness checks to examine whether increasing this target will lead to different policy implications. We find that, when we use a higher fraction as the target, the positive effect of SFC policy becomes bigger. Consequently, our main finding that combining public housing and SFC can lead to Pareto Improvement and help the poor also becomes even stronger.

¹³The instability of symmetric equilibrium in spatial equilibrium models has been noticed by the literature (e.g., Fernandez and Rogerson, 1996).

on parents' well-being are ambiguous. Devoting a larger share of expenditure on children leads to a smaller expenditure share for the parents. This intra-household allocation of resources harms parents' well-being. According to our benchmark calibration, the positive effects of a higher total income and lower rents (weakly) outweigh the adverse effects.

The "Baseline" column of Table 4b indicates (partial) income-sorting or imperfect sorting across districts. Almost half of the households (46.93%) in the West community are BA type, while only 29.40% of families in the East are of type BA. The West has a smaller proportion of NH-type households (7.05%) than the East (14.52%). Consequently, the average annual income in the West is higher than that in the East (\$116, 192 vs. \$102, 106). Such spatial sorting has several implications. First, the West has a more top average child quality and hence, a stronger peer group effect. Because the majority of the West comprises BA-type households, its property tax rate is 1.4673%, higher than that in the East (1.3992%). A higher property tax rate and better peer effect make the West a more desirable community that attracts more households than the East (about 60% of the total population).

Given that the two districts are ex-ante identical, it is interesting to note that (1) the population shares of the two communities are so different (40 to 60) and (2) the equilibrium market rent in the West, the more populated neighborhood, is significantly higher (\$41,076 vs. \$37,703 in the East). Because the schools are financed through property taxes, parents in the West effectively pay more instructional expenses for each child. As a result, the school quality, which is the product of per-child education expenditure and peer effects, is much higher in the West than in the East.

Note that the schools in the West have a better quality that benefits the children in the community. However, such benefit comes at the expense of the well-being of parents, because they need to pay for higher housing rents. Table 4a also shows how the parents make the tradeoff between the quality of their offspring and their well-being. For each type of household, the average well-being (quality) of the parents (children) is higher (lower) in the East than in the West.

2.4 Model-implied Rent gradient

To further strengthen the credibility of our model, we ask whether our model can produce a plausible rent gradient. More specifically, we use the model to generate some "artificial data" of house rent in different locations in the city, and then run a regression that resembles some existing empirical works. We will then compare the model-generated rent gradient with the empirical counterpart. Notice that the rent gradient in the model is *not* targeted in the calibration process. The negative rent gradient is well documented. Among others, Eberts and Gronberg (1982) estimate the rent gradients in Chicago around 1970 and finds that the logarithm of median housing value drops by about 9% for houses located 1 *mile* away from the CBD.

To calculate the model-implied rent gradient, we draw a random sample that contains 2,800 observations for both the East and the West from their corresponding population in the model.¹⁴ For simplicity, we adopt a semi-logarithmetic regression equation,

$$\log R_i = \beta_0 + \beta_D D_i + \beta_X X_i + u_i. \tag{11}$$

¹⁴We also estimate a large sample (over 100,000 observations) version. The results are almost identical to the small sample version and are therefore omitted here.

where R_i is the rent, D_i is the distance from CBA, and X_i are other control variables.

Notice that the location choice is endogenous and hence, in the empirical literature, regression models like (11) often include control variables X_i to mitigate the endogeneity issues. The control variables X_i normally includes (1) variables that reflect the heterogeneity of the landlords/tenants; and (2) variables that represent specific housing unit characteristics. In our model, for simplification, we assume that all housing units are identical except concerning lot-size and location. As the dependent variable is rent rate per square mile, by construction, R_i accounts for the effect caused by the difference in lot-size. Therefore, we do not need to add other hedonic variables into X_i (Malpezzi, 2003). Also, we assume that adults who purchase/rent the housing units differ only concerning their wage rates w and degree of altruism toward their children k_o . Notice further that k_o is not observable, and it is perfectly correlated with wage w in our model. Therefore, it suffices to include wage w in X_i . Thus, (11) can be rewritten as:

$$\log R_i = \beta_0 + \beta_D D_i + \beta_w w_i + u_i. \tag{12}$$

Table 5a summarizes the descriptive statistics of the two samples. As discussed in previous sections, the average rent and wage income are higher in the West than in the East because the former attracts more skilled workers than the latter. Other things being equal, the West is a more attractive community because it provides better education to the younger generation. Consequently, more land is occupied in the West. Hence, as the table indicates, families living in the West reside further away from the CBD than those in the East on average.

We estimate equation (12) for each of the two groups separately. Table 5b shows the regression results. All of the coefficient estimates are highly significant. In the West, an additional dollar in occupants' hourly wage decreases market rents by about 0.11%, and the same change raises housing rents by 0.08% in the East. Our focus is the coefficient of distance from the CBD. The estimate of β_D falls around 0.09, indicating that rental rates are about 9% cheaper at locations 1 mile away from the CBD, which is comparable to the finding of Eberts and Gronberg (1982). It suggests that our model, as a first-order approximation of "reality," is reasonably reliable.

3 Policy Analysis

Based on our calibrated model, we conduct a series of counterfactual experiments to analyze the welfare implications of various education and housing policies. In this section, welfare can refer to household utility, parents' well-being, or offspring's quality, and we will clearly distinguish their differences whenever there is a chance of ambiguity. Our primary goal is to explore the possibility of a Pareto-improving policy package. To facilitate the comparison with the previous literature, the education policy that we study is school finance consolidation. For housing market policies, we consider the provision of public housing units and housing voucher programs. To build our intuitions in this highly nonlinear environment, we first study each regime separately. Then, we consider some policy packages and their overall effects.

To compare parents' well-being, offspring quality and the average utility level across different policy regimes, we turn to a widely used consumption-equivalent measure. More specifically, we search for the discount factors/multipliers, χ_t , $t \in \{W, \Omega_o, U\}$, which must be imposed on the

consumption of parents and children in the new equilibrium to push their well-being back to their levels at the baseline equilibrium. Therefore, $\chi_t > 1$ (< 1) indicates that the households are worse off (better off) in the new equilibrium. We report the value of $1-\chi_t$, $t \in \{W, \Omega_o, U\}$ in the summary table so that the value is positive (negative) when welfare increases (declines). Here is our formal definition.

Definition 2 For certain group of households with average utility level, parental well-being and offspring quality levels equal to U_{base} , W_{base} and Ω_{obase} in the baseline equilibrium, the welfare measure χ_U , χ_W and χ_Ω satisfy the following equations:

$$Average(U(\chi_{U}Z_{p}^{\star},\chi_{U}Z_{o}^{\star},...)) = U_{base}; Average(W(\chi_{W}Z_{p}^{\star},...)) = W_{base};$$
$$Average(\Omega_{o}(\chi_{\Omega}Z_{o}^{\star},...)) = \Omega_{obase},$$

where $U(Z_p^{\star}, Z_o^{\star}, ...)$, $W(Z_p^{\star}, ...)$ and $\Omega_o(Z_o^{\star}, ...)$ are the utility, parental well-being and child quality levels of the households in the new equilibrium, respectively.

3.1 School Finance Consolidation (An education policy may impact the housing market)

School Finance Consolidation (SFC), or School District Consolidation, is an apparent post-war trend in the U.S. The number of school districts that provide elementary and secondary education had dropped from 117,108 in 1939~1940 to 13,862 in 2006-07 (National Center for Education Statistics). In HY's model setting, the central government moves all students to a single school, which it finances through the property taxes collected from all of the lands in the economy. HY (2007) calibrate their baseline equilibrium to match a representative United States city circa 1997. Based on the parameter set obtained from the calibration, they show that enforcing SFC hurts everyone in the economy. Their finding supports the arguments of Fischel (2006), which describes consolidation policy as an external distortion leading to welfare decline. In practice, although the government can make per-child educational spending equalization possible, it is not easy to enforce the equalization of peer group quality, which can only be achieved as market equilibrium. To complement the literature, we assume that the two communities have the same per-child educational spending, but can potentially differ in school quality when we consider SFC.

We summarize the new equilibrium in the "SFC" column of Table 3b and 4b and compare this SFC equilibrium with our baseline equilibrium. Note that after the consolidation of school districts, the property tax rate is now voted by all the adult members in the economy and applies to both the West and the East communities. Because HA-type adults comprise the majority, their preferred property tax rate of 1.3992% will be the equilibrium property tax rate. It is slightly lower than the level preferred by the BA. The drop in property tax rate decreases per-child educational expenditure in the West, which induces BA- and HA- type households, who value the quality of their offspring, to move from the West to the East. Their movement increases (decreases) the average income in the East (West), which boosts (lowers) the rent in the East (West). Because school funding is derived from property taxes, which are proportional to housing rents, the per-child school funding is higher (lower) in the East (West) than before. The movement also tends to decrease the gap in peer-group quality between the two communities.

In summary, the SFC narrows the school quality gap between the West and the East. The population is evenly distributed in the two districts after the SFC policy is imposed. Figure 2 shows this pattern explicitly.

(Figure 2 about here)

Our welfare results are summarized in the "SFC" column of Table 6. Unlike in HY (2007), the SFC policy makes all types of households better off. On the one hand, SFC indeed restricts the choices of school quality to one, potentially resulting in a more substantial average individual deviation from optimal levels of school quality. On the other hand, the SFC policy also substantially reduces the gap of school qualities, rents, and hence population compositions between the two communities, leading to more efficient use of land. Whether the SFC policy is welfare-improving or not depends on which of the two effects dominates the other. It, in turn, depends on how extreme the sorting pattern is in the baseline case since extreme sorting leads to inefficient use of land. It appears that the sorting pattern is more extreme in our baseline case than in the baseline case of previous HY papers. As a result, when we remove sorting, the positive effect from the more efficient use of land dominates the negative effect of restrictions on choices. Our focus here is not to overturn the conclusion of HY (2007, 2013) on SFC, but rather to highlight that SFC can potentially lead to Pareto Improvement in a variant of HY.

Furthermore, Table 6 shows that the adult members in BA- and HA-type households enjoy better well-being while the quality of their offspring suffers. In other words, SFC is Pareto improving at the household level, but not the individual level. There are intuitive reasons for this finding. First, some of the BA- and HA-type families move to the East where the housing rents are lower than the West, and hence, they can consume larger lot sizes than they would if they stay in the West. Second, cross-community sorting becomes much weaker. Recall that in our model, parents with a higher level of education tend to produce higher-quality children. Consequently, children from BA- and HA-type households are faced with lower peer group quality on average because they are pooled with children from NH-type families. The converse applies to NH-type families.

(Table 6 about here)

3.2 Public Housing and Housing Vouchers (Housing market policies may impact education)

In the previous section, we focus on SFC, which is an education policy that has implications on the housing market. In this section, we consider two housing aid policies, including government-subsidized public housing and housing vouchers, which would, in turn, affect education quality. These housing aid programs are designed to provide low-income groups with basic residential spaces. In our model, 10% of the households are of the NH-type. The adults in these families earn meager wage incomes that total about 60% and 33% of the wages of adults in the HA- and BA-type households, respectively. Hence, we assume that public aid programs are only open to NH-type households. We further assume that all NH-type households can receive assistance. A central government finances the programs through the income taxes paid by the adults. As a simplification of the progressive income taxation imposed in the U.S., we assume that the NH-type adults, who would enjoy the housing policy benefits, do not need to pay the income taxes and that all of the other adults are faced with uniform income tax rate θ .

 $^{^{15}}$ For more robustness checks for alternative targets of community compositions, see the appendix.

¹⁶In practice, there are more U.S. families are eligible for public housing programs than receiving assistance. Leung et al. (2012) study the case when the public housing units are "under-supplied," and low-income families can get those units through rationing.

¹⁷ Again, the uniform tax rate across HA- and BA-type households is imposed to simplify the analysis. The crucial point is that the NH-type households do not need to pay the income tax while receiving the benefits. The results

We introduce public housing into the baseline model and study its implications to economic outcomes and social welfare. Under this policy, each participating household enjoys a lot of size S_{PH} and contributes $S_{PH}R_{PH}$ to the program. The government receives contributions from the participators and income taxes from the non-participators. Then, she purchases land and builds housing units for the program participators. Therefore, a particular program participant's decision problem is reduced to

$$\max_{S_p,S_o,Z_p,l,Z_o,n_o} U_{NH}\left(S_p,Z_p,l,S_o,Z_o,n_o\right) = \left(S_p^{\alpha_p} Z_p^{\beta_p} l^{\eta}\right)^{k_p^{NH}} \left(q^{\gamma} S_o^{\alpha_o} Z_o^{\beta_o}\right)^{k_o^{NH}} g n_o^{1-\epsilon},$$

subject to
$$Y_{NH}(r) = w_{NH}l(r) + w_{NH}cn_o(r) + S_{PH}R_{PH} + Z_p(r) + n_o(r)Z_o(r),$$

 $S_p + n_o(r)S_o = S_{PH}.$

In the appendix, we show the detailed formula for the new fertility decision, $n_o^{Pub}(r)$, and the new children's quality function $\Omega^j_{oPub}(r)$.

Recall that one of the main goals of public housing policies is to assist children from economically adverse families and to promote intergenerational mobility. Hence, we are interested in the effects of government housing programs on the quality of children from NH-type families. With the above derivations, it is simple to prove the following propositions.

Lemma 1 At a given location, NH-type adults under housing program give birth to fewer offspring than they would at the baseline equilibrium if their contribution to the program is more prominent than their expenditures on housing in the baseline situation

If
$$S_{PH}R_{PH} > [(1+\tau_j)S_{NH}(r,u_{NH}^{\star},q_j,\tau_j)\psi_{NH}(r,u_{NH}^{\star},q_j,\tau_j)]_{Baseline}$$
, then $n_o^{Pub}(r) < n_o^{NH}(r)_{Baseline}$.

Proposition 4 Given the same location and school quality, when NH-type households receive larger lot size and pay more under the public housing program than in the baseline equilibrium, they produce higher-quality offspring.

$$\begin{array}{ll} \textit{If } S_{PH}R_{PH} & > & [(1+\tau_j)S_{NH}(r,u_{NH}^{\star},q_j,\tau_j)\psi_{NH}(r,u_{NH}^{\star},q_j,\tau_j)]_{Baseline} \\ & \textit{and } S_{PH} & > & S_{NH}(r,u_{NH}^{\star},q_j,\tau_j)_{Baseline}, \\ & \textit{then } \Omega_{oPub}^{j}(r) & > & \Omega_{oNH}^{j}(r)_{Baseline}. \end{array}$$

The intuitions are straightforward. Facing the government-subsidized rent with public housing units that are larger than they would otherwise rent from the market, the NH-type households choose to have fewer children, which in turn enables those families to spend more on each child and raise their quality.

3.2.1 Public Housing Policy 1: Units Located at the Middle Ring of the City

In practice, public housing units are not evenly distributed within a city. In this paper, we consider only the case where public housing units are built in only one district, which is the East. The central government must decide where to locate those public housing units within the neighborhood. We

would carry to the environment when different groups of agents all face different tax rates.

investigate two alternatives. First, we consider a case similar to Leung et al. (2012), where public housing units are located between D_i and D_o miles from the CBD. We assume that the land in this area is rented from the market. Hence, the central government needs to calculate the rent she needs to pay in a competitive rental market, where the rental rates are determined at auction with type $i \in \{HA, BA\}$ households and agricultural workers. Since the analysis is analogous to the baseline case with no public housing, we refer the interested readers to the appendix for details.

In addition to the rental costs, the central government must make a payment known as the Payment in Lieu of Tax (PILOT) to compensate the local government in the East for some of the property tax revenue lost due to the public housing program. Here, we follow Leung et al. (2012) to make the simplifying assumption that the PILOT is equal to the property taxes placed on the public housing recipients' contribution to the program,

$$PILOT = \tau_E \overline{N_{NH}} S_{PH} R_{PH}, \tag{13}$$

where \overline{N}_{NH} is the total number of NH-type households.

This program is financed by the contribution of the residents of the public housing and the income taxes paid by non-participant households. The former can be calculated by the simple formula $Contribution = \overline{N_{NH}}S_{PH}R_{PH}$. The central government adjust the parameters $(\theta, S_{PH}, R_{PH}, D_i)$, and D_o of the public housing program so that the public budget constraint holds,

$$R_{Pub} + PILOT = Contribution + IT, (14)$$

where R_{Pub} is the sum of rents that the central government needs to pay to the private sector to obtain the land for public housing, IT is the total income tax revenue. We reserve the tedious details in the appendix.

To compute the Public Housing Equilibrium, we impose some parameter values. The public housing units are located only in the East and start from 4 miles away from the CBD. The family-specific lot size is set to be 0.001 square mile, which is about 25% larger than the average unit within that band in the baseline equilibrium. We can then determine the outside boundary of the public housing band, which is 6.916 miles. The central government charges an income tax rate IT = 0.8% to balance its budget, which endogenously matches the calibration target for the participant contribution to the program of \$221.4 per month. The increase in utility that the participants obtain by joining the public housing program is close to the one derived from a 25% consumption subsidy in the baseline equilibrium.

Figure 3a and the "PH1" column of Table 4b display powerful sorting at the equilibrium.¹⁸ All of the BA-type and most of the HA-type households choose to live in the West in response to the sharp decline in peer effect in the East caused by the massive allocation of all the public housing recipients (NH-type, who care the least about the quality of their offspring) in the East. This strong sorting makes the two districts significantly distinct. Both the property tax rates and the lot sizes in the two communities are almost identical. However, with the strong sorting effect, the market rent in the West exceeds that in the East by a large margin, which leads to much higher expenditure on education in the West. Combined with the peer group effect, school quality in the West is also much higher.

¹⁸ Although the sorting in our public housing equilibrium is qualitatively stronger than that shown by LSY (2012), they are essentially similar in spirit.

The "PH1" column of Table 5 presents the welfare effects of this policy. At the household level, the public housing residents (NH) are better off, and all of the other types are worse off. This result is intuitive. Under this policy, all of the household location choices deviate from the efficient ones. As a result, the welfare of the whole economy declines. A careful inspection of the results reveals that the improvement of the level of happiness of NH-type households comes from an increase in parents' well-being. These parents can enjoy large lot sizes without paying more. However, there is no free lunch. The education quality in the East drops dramatically as all NH-type households concentrate in one district. Consequently, public housing policy hurts the quality of NH-type children.

On the other hand, the proportion of offsprings from BA-type families increase in the West, and through the peer group effect, BA-type children benefit from the outstanding quality of education in the West. However, the public housing policy hurts adults from BA-type families the most for two main reasons. First, the BA-type households now all located in the West and hence drive up the housing rents significantly. Second, because they do not constitute the majority of their community, the voting outcome of the property tax rate is not their preferred outcome. Both parents and offspring of HA-type households are worse off to a relatively mild extent.

3.2.2 Public Housing Policy 2: Units Located at the Edge of the City

In the previous section, we assumed that public housing units are located in areas that would otherwise be occupied by non-participating households. Consequently, this type of public housing policy decreases the amount of accessible land and probably results in higher market rents and less-efficient land allocation. In this section, we consider an alternative public housing policy, which would have minimal effect on the land that is already occupied. More specifically, we assume the public housing units are located at the edge of the city, and we compare the new equilibrium with the one in the previous section concerning resource allocation as well as welfare. Under this scenario, the households who are not eligible for public housing would first compete with agricultural use on each piece of land they desire. Then the government builds the public housing unit outside the fringe of the East district. In other words, the public housing units are located in areas that would not be occupied by different households, and thus, the government acquires the land at the agrarian rent R_a . For the sake of comparison, we maintain the assumption that $S_{PH} = 0.001$ square mile and $\theta = 0.8\%$. Each participated family must contribute \$199.4 to the program so that (14) holds. The required contribution is smaller than that in the previous case, as the market value of the public housing band is less than before. In the equilibrium, this band is located between 6.0871 miles and 8.2997 miles away from the CBD. Figure 3b shows the housing rents and occupants of all of the locations in the city. For the public housing area, market rent is defined as the participants' contribution (per square mile).

(Figure 3b about here)

A comparison between the "PH1" column with the "PH2" column of Table 4b highlights the difference in the household distribution of the two public housing policies. Although we still observe no BA-type household in the East, the proportion of HA-type families residing in the East increases from 9.29% to 21.33%. The spatial sorting is weaker. At the same time, the BA-type households outnumber the HA-type households in the West and determine the property tax rate to be 1.4673%. The corresponding "Community Comparison" column of Table 4b summarizes other essential statistics of this equilibrium. As more HA-type households move from the West to the

East, the demand for land in the East (West) becomes stronger (weaker), resulting in higher (lower) housing rents. Per-child education spending increases in both communities. In the East, this is a consequence of higher rents. The community attracts more HA-type households and has a stronger peer group effect than before. In the West, although housing rents decrease slightly, the property tax rate and total tax income increase. We observe better school quality in both communities in equilibrium. Comparing the "PH2" with "PH1" columns in Table 5, we conclude that all of the family members from all of the household groups are better off after the government puts the public housing units outside the fringe. It confirms the intuition that decreasing the amount of accessible land has an adverse welfare effect on the whole economy. In a sense, the government kills two birds with one stone (i.e., implementing the second, at-the-edge type public housing policy, rather than the within-the-city type that is considered in the previous section). First, it can improve the welfare of the most impoverished families (NH) at a lower welfare cost imposed on other households in the economy. Second, it can reallocate resources between adults and children. Under the public housing policy, children are better off, and parents are worse off.

Notice that our results are also broadly consistent with other empirical studies of public housing unit residents. For instance, Olsen and Barton (1983) study the benefits and costs of public housing based on New York City data, and find that "...the mean benefit of the program to these families is substantial relative to their mean income but small compared with the cost to taxpayers." Currie and Yelowitz (2000), Jacob (2004), among others, also confirm that public housing per sec can lead to an improvement of the younger generation of public housing residents.¹⁹

3.2.3 Housing Voucher

Instead of building public housing units and hence directly change the housing supply, the government may distribute cash, which is also known as the housing voucher program (VC). Under this scheme, the government collects income taxes from the skilled workers and redistributes them to the poor in the form of a housing voucher, which can only be used to purchase housing services. Hence, program participants can still choose their desired locations, desired lot sizes, etc. In the context of HY (2007), Leung et al. (2012) show that housing voucher is better than public housing provision. Since we obtain different welfare results than HY (2007), it may be worthwhile to reconsider the housing voucher in the current setup.

Here are the details of VC. For non-participating households, the utility maximization problem is the same as that under public housing policy. For participating families, they are exempted from the income tax but instead receive housing vouchers from the government that amounts to v_p , which is for housing consumption only. Hence, the program participant's budget constraint becomes

$$Y_{NH}(r) = w_{NH}l(r) + w_{NH}cn_o(r) + Z_p(r) + n_o(r)Z_o(r) + \max\{0, (S_p(r) + n_o(r)S_o(r))(1 + \tau_j)R_j(r) - v_p\}.$$
 (15)

Since the utility function is monotonically increasing in lot size, all of the participating households spend no less than the number of their vouchers on housing. Whether they will have a higher expenditure on housing depends on their housing preference and income levels. Intuitively, the housing voucher induces the household to spend more on housing, and hence, they may either have fewer children or by investing less on each child. On the other hand, the housing voucher also effectively gives more resources to the recipient household, who can only spend more on family and

¹⁹Public housing plays a more important role in Asia. Among others, see Leung and Tang (2015), and the reference therein.

children. In the appendix, we provide more elaborations on this and conclude that the overall effect is ambiguous and can solely be determined by numerical exercise.

The rest of the program is simple. All of the lands are rented out through the same market mechanism, as we have described in previous sections. The government chooses policy parameters (θ, v_p) correctly so that the income tax revenue IT is equal to the total cost of financing the program, which is $v_p \overline{N}_{NH}$.

The computation of the market equilibrium under the housing voucher program is similar to other cases. To be compatible with previous sections, we keep the income tax rate at 0.8%. It implies that each participating household receives the equilibrium housing vouchers that amounts to \$23.12 each day, and all of the participants spend more than this amount on housing units. As we observe from Figure 3c and the "VC" column of Table 4b, household sorting is stronger than that at the baseline and weaker than the one under public housing policy. Although there are no BA-type households in the East under the VC program, we observe NH-type households that amount to 2.69% of the total number of households in the West. Land demand and market rents increase in the West, where all of the rich families live. They constitute the majority in the West and determine the property tax rate there to be 1.4673%, which is the same as the baseline case. Having higher housing rents allows the local government of the West to collect more property taxes and hence provide more funding to the schools there.

Conversely, in the East, the average market rent declines from \$37,703 to \$35,172, indicating that less funding for schools is collected. The change in school funding amplifies the gap in school quality between the two communities. Recall that skilled workers care more about their offspring hence tend to produce higher-quality children. Under our model setting, this means that schools with higher percentages of students from high-income families provide better peer quality. Therefore, the gap in school conditions is further enlarged because the West now attracts all of the BA-type households. As a result, the educational qualities are 741 in the West and 123 in the East compared with 564 and 280 at the baseline, respectively. In other words, stronger sorting occurs under the VC program, and an amplified gap in school quality is observed. NH-type parents seek a better education for their offspring and are willing to pay higher housing rents to do so.

(Figure 3c about here)

The "VC" column of Table 6 shows the welfare implications of the housing voucher program. The overall welfare changes are very similar to those in the public housing case. The average utility of program participants increases by about 18.5% while the overall welfare of other families declines slightly, as in Leung et al. (2012). The economy-wide average welfare decreases by only 0.19%. Hence, the housing voucher program incurs less loss of total welfare than the public housing policy because the former imposes fewer restrictions than the latter on household choices. Hence, the increase in NH-type households' welfare is less costly, which leads to a smaller welfare loss for HA-and BA-type families.

On the other hand, while the housing voucher program and public housing policy deliver similar aggregate utility, their *intra-household welfare implications* are very different. Recall that the public housing policy is very useful in improving the quality of children from low-income families. Hence, the gaps in child quality between different groups of households are reduced, potentially increasing intergenerational social mobility. On the other hand, our welfare results show that VC policy

 $^{^{20}}$ In this section, public housing policy refers to the scenario where all public housing units are placed outside of the fringe distance.

enlarges the gap between affluent and low-income families. When the school quality of two districts become drastically different, skilled parents tend to cluster more heavily in the community with higher rents, and better schools and unskilled parents do the opposite.

3.3 Policy Package: Combination of School Finance Consolidation and Housing Market Policies

The previous section, which studies each of the education and housing policies in isolation, delivers the following lessons. First, due to the presence of peer effect, imposing school finance consolidation may increase the aggregate utility. Second, an appropriately designed public housing program can be a handy tool concerning aiding children from low-income families. Third, housing voucher tends to enlarge the quality gap between the children from high income and low-income families. Based on these observations, this section addresses a natural question: is it possible to help needy children while keeping other families at least as well off as before by combining education and housing policies?

We consider different policy packages. One possibility involves combining school finance consolidation with a housing voucher program. As we discussed previously, the housing voucher policy does not perform well regarding increasing the living and educational qualities of needy children. However, we consider this combination for the sake of completeness. Figure 4a depicts the rent-distance relationship in this case. The "SFC+VC" column of Table 6 summarizes the welfare changes caused by this combination. At the household level, a combination of the school finance consolidation and housing voucher makes all families better off. It may not be surprising because the school finance consolidation policy alone generates a similar result, and the current policy package can be considered as a wealth-redistributed version of the standalone version of the school finance consolidation. However, this policy package is not a Pareto improvement over the baseline situation at the individual level because non-participants are slightly worse off. Moreover, it does not help children from low-income families, and their average quality slightly decreases (-0.33%) comparing with the baseline case.

Hence, we consider another policy package, which combines the school finance consolidation with public housing. It equalizes the per-child funding in the two districts and put all public housing units outside of the fringe distance in the East. As Figure 9 and the "SFC+PH" column of Table 4b show, the cross-community sorting in this equilibrium is stronger than the baseline case but much milder than the scenario of public housing policy only. This observation confirms our conjecture: SFC makes the two districts less different and therefore weakens the magnitude of sorting. The "SFC+PH" column of Table 6 shows the welfare results of this policy package. Comparing with the baseline equilibrium, all three types of households are better off. We also observe a substantial improvement in children's quality of NH-type families. Hence, the government can bring welfare improvement to the economy and increases the quality of children from low-income families as well.

3.4 Short- vs. Long-run Analysis

Thus far, our policy analyses have followed the tradition of urban equilibrium models, which typically assume that markets are originally in equilibrium, upon which policy is then imposed unexpectedly. Agents re-optimize their choices, such as their location and consumption. The markets

instantly clear, and we compare the welfare under the new equilibrium with the original one. With our static model, such analysis is interpreted as a long-run assessment of public policies. However, as Quigley and Swoboda (2010) and others recognize, some choices cannot be altered in the short-run. Consequently, the long-run welfare implications for some policies can be dramatically different from their short-run counterparts. For instance, policy changes typically do not significantly alter the housing supply in the short run, which is often assumed to be fixed. However, the long-run supply of housing should arguably be flexible. Housing decays over time, and economic agents can decide to replace it. As such, it may be important for us to re-examine our welfare results while taking the short-run rigidity into consideration.²¹

To facilitate the comparison, we make minimal modifications to the current framework.²² More specifically, we differentiate variables according to their corresponding "flexibilities." In our model, all of the choices are flexible in the long-run, and some choices are more flexible than others in the short-run. Table 7 summarizes the flexibility of different choices. We consider fertility choices to be the most inflexible. It is physically impossible to decrease the number of children that parents have already had. In any given year, it would take at least another year for parents to bear an additional child.

Furthermore, residential choices cannot be easily adjusted. In many places, the term length of a residential rental lease is typically one year or longer. Depending on the market condition, it may take a similarly lengthy period to sell a house.

(Table 7 about here)

The recognition that households are not allowed to move in the short-run is important. Recall that in the public housing experiments in which program participants are forced to relocate across districts. Thus short-run immobility could impact our results. To address this concern, we conduct only a "short- vs. long-run" analysis for the SFC and housing voucher experiments and the experiment that combines the two. At the same time, households are free to decide how many non-durable goods to consume even in the short-run. We also assume that the amount of leisure can be easily adjusted.

Hence, the time allocation in our model is not entirely flexible. For instance, childcare time is a linear function of the fertility rate and is therefore inflexible in the short-run, just like fertility choices. A worker's commute time is also rigid, as it is merely a multiple of the distance from the worker's home to the CBD. In this paper, we present only the results for the case in which leisure time is treated as a flexible good.

Table 8a summarizes some relevant statistics. Household's consumption choices and working hours in the short and long runs are similar. It is because, in our model, a household's optimal expenditure on consumption and leisure are constant fractions of their total potential income hence do not depend on their lot size choices. Thus, the fact that a household cannot adjust its residential area in the short run does not affect its consumption and leisure decisions. Nevertheless, the short-and long-run choices are not identical for at least two reasons. First, a household's location decision affects its potential income and hence, its consumption and leisure choices. Therefore, as the economy has significantly different household space distributions in the short and long-run, the average

²¹In this section, the term "goods" is inclusive. All of the parents' choices, including those related to fertility, consumptions, space, and leisure, are considered "goods."

²²Short- vs. long-run analysis is not a perfect substitute for the transition dynamics analysis, which is feasible only when a fully dynamic general equilibrium (DGE) setting is available. In this paper, we focus on a static setup and leave the DGE for future research. For a review of the related literature, see Leung and Ng (2019), among others.

consumption and leisure time take different values in the two situations. Second, a household's decision on leisure and working hours are subject to time constraints. Households allocate their time endowments to different activities, including childcare, commuting, the enjoyment of leisure and work. Both childcare and commute time are fixed in the short run, as fertility and location choices are also set in the short run. Because agents are allowed to re-optimize these decisions in the long run, the leisure choice is affected. As childcare and commute time are fixed in the short-run, we can take them out of the household's time endowment and define the residual as the "effective time endowment." It is then apparent that different people have different effective time endowments in the short-run but converges to the same level in the long-run. Hence, their optimal working hour choices differ in the short and long run.

(Table 8a about here)

When the school finance consolidation is imposed, school quality almost does not change when the time horizon moves from the short-run and long-run. In contrast, short- and long-run school quality can differ significantly if the schools are not consolidated. Recall that in this model, the school quality of a community is simply the product of average education expenditure and average student quality in that community. Both of these components depend on the population share of highly educated households in the community because their presence tends to drive up the rents, which in turn leads to more school funding, and because higher-quality offspring tend to be associated with higher quality parents. Under the school finance consolidation regime, there is only one school district whose composition is always the population distribution in both the short and long runs. Consequently, school quality under SFC does not vary as much as under alternative policies when the economy moves from the short-run to the long-run.

Table 8b reports welfare comparisons. Households in the East are generally better off than those in the West in the short run, especially when school finance consolidation policy is imposed. In the long term, economic agents are mobile and hence, their welfare depends only on their types. Our set-up enables us to conveniently decompose the total welfare of a household into parents' well-being and offspring quality. The extra benefits that residents in the East obtain come mainly in the form of offspring quality. Recall that the East has lower average rental rates and peer quality. SFC policy enables children from the East to go to better schools in the West, bringing significant welfare improvement to those households. At the same time, because the agents are unable to move in the short run, households in the East are effectively given a "free-ride" on the better education provided in the West. In other words, short-run rigidity prevent the housing market from functioning efficiently, and agents' welfare becomes location-dependent as a result.

(Table 8b about here)

Another important finding is that long-run equilibria are not always better than short-run equilibria. According to Table 8b, the long-run average welfare of households is higher than the short-run counterpart only when school finance consolidation policy is imposed. When the housing voucher program alone is imposed, the average welfare in the economy increases in the short-run (relative to the laissez-faire benchmark) but deteriorates in the long run. In particular, the welfare of Group 2 agents (i.e., HA-type) is hurt in the short-run (relative to the laissez-faire benchmark) and hurt even more in the long run. This finding is at odds with conventional wisdom. Moving from the short-run to the long-run, households have more choices, and economic agents are usually better off. However, such intuition is based on a perfect market, and our agents live in an imperfect

world characterized by many forms of market imperfection, including the externality generated by the peer effect and the non-convexity of consumption caused by household's location choices. Thus, HA-type agents can be hurt in the long run if they find the proportion of BA agents in their community drops dramatically. Our numerical exercises with plausible parameter values suggest that the intuitions based on the perfect market can fail. It is because when the housing voucher program is imposed, wealthy families cluster more intensively in the West when given such an opportunity, greatly enlarging the difference in community composition.²³

4 Concluding Remarks

This paper builds a simple spatial equilibrium model that embeds fertility choice, location choice, and work-leisure choice in a unifying framework. Our model distinguishes from some previous work by separating the welfare of the children from their parents, which in turn enables us to differentiate policies which benefit all households but not all individuals, from policy regimes that help all individuals. Our calibration confirms that the model can match specific family, labor market, and housing market outcomes simultaneously. Our model-implied rent gradient also matches previous empirical estimates. We analyze various educational and housing policies and their combinations. We demonstrate that public housing policy can induce intense sorting among different types of agents, and the welfare result depends crucially on whether the public housing units are built on land that would otherwise be used. On the other hand, the housing voucher program can increase the overall welfare of low-income households, it is the parents who capture the welfare gains, and their offsprings can be hurt.

We also compare the implications of the short-run (in which some specific choices are restricted after the economic policy is imposed), versus the long-run (in which all decisions are flexible). To the best of our knowledge, other than the study by Quigley and Swoboda (2010), such short-vs. long-run analysis has been relatively underexplored in the urban economics literature. For instance, we find that the housing voucher program can increase the average welfare of the economy in the short-run but decreases it in the long run with plausible parametrization. This result points to the possibility that some policies which can bring long-run gains to the economy may not be implemented due to their short-run adverse impact.

We also demonstrate that in some situations, middle-income agents can lose more in the long run than in the short run after a policy change. It is because their utility levels depend on the proportion of high-income agents living in the same neighborhood. In the short term, agents stay in the original houses, and hence the welfare loss of the policy is simply the direct policy effect. In the long run, however, the high-income agents may move to another community, driving down the school quality of the neighborhood. The middle-income agents either stay and live with the depreciated school quality or migrate with the high-income agents and face possibly higher rents and taxes. Future research should further explore such considerations.

Other aspects of this paper can also be extended. For instance, our model has a simple commuting cost structure, while the reality may be more complicated (e.g. Leroy and Sonstelie, 1983). Chetty and Hendron (2018b) find that high commute time is associated with low intergenerational mobility. Thus, future research should re-examine the optimal location of public housing units with more realistic transportation system. we could allow for assortative but imperfect matching

²³The result here is consistent in spirit with studies of "second-best theory" in which the laissez-faire equilibrium is inefficient.

of spouses in the model. We could also consider some possible racial issues. Capital market imperfections present another challenge to future research. Urban policy analysis in those environments remains a challenge to be met.

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Figure 1 Rent-Distance Curve

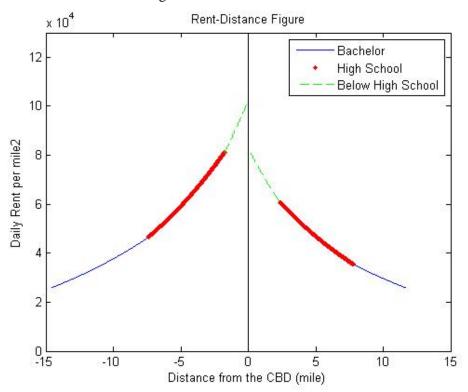


Figure 2 Lot Size-Distance Curve

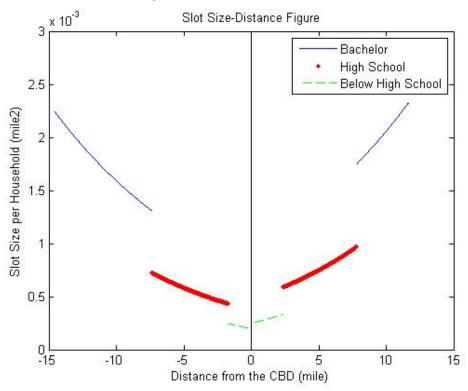


Figure 3 Population Density-Distance Curve

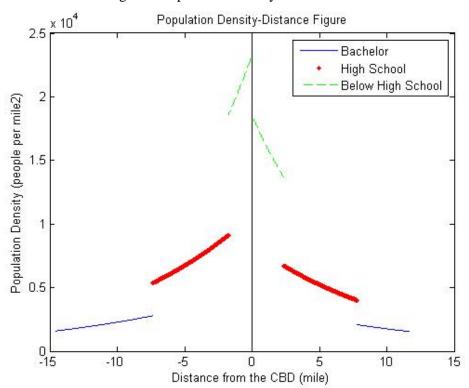


Figure 4 Rent-Distance Curve (School Finance Consolidation)

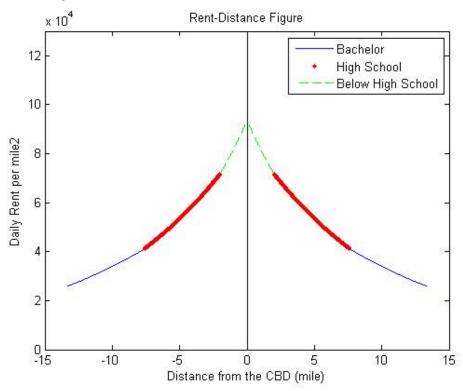


Figure 5 Rent-Distance Curve (Public Housing within Fringe Distance)

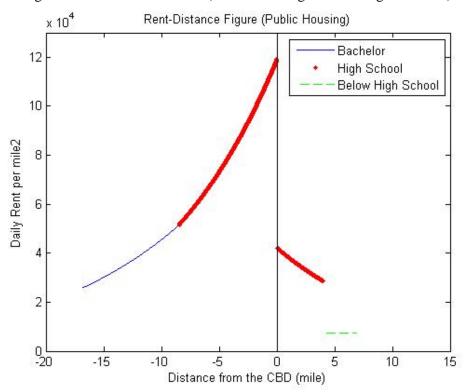


Figure 6 Rent-Distance Curve (Public Housing beyond Fringe Distance)

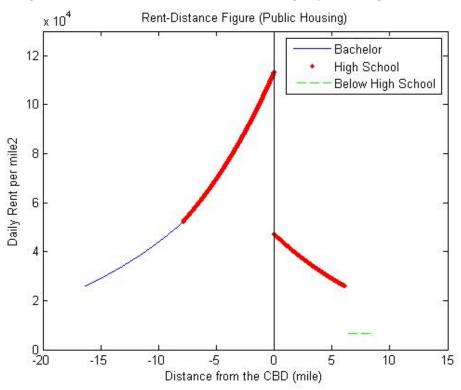


Figure 7 Rent-Distance Curve (Housing Voucher)

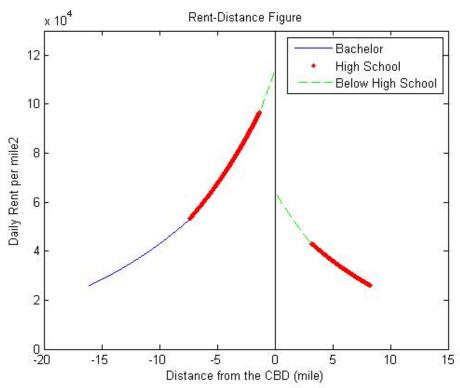


Figure 8 Rent-Distance Curve (School Finance Consolidation + Housing Voucher)

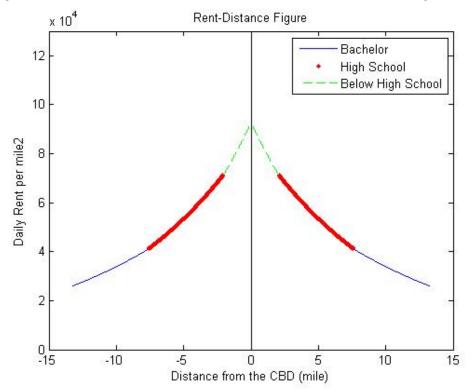


Figure 9 Rent-Distance Curve ((School Finance Consolidation + Public Housing)

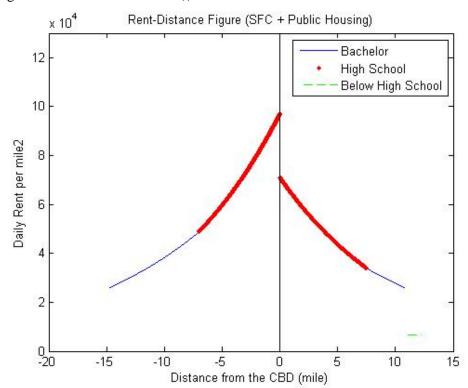


Table 1 Educational Attainment, Annual Income and Fertility Rate

Level of	Male	Female	Income of	Female	Average	Average
Education	Income	income	Pseudo	Fertility	Income	Fer. Rate
	(in \$)	(in \$)	Household	Rate	(\$) across	across
			(in \$)		Groups	Groups
Less than	26,604	19,588	46,192			
9th grade				2.521	51,432	2.521
9th to 12th	33,194	23,478	56,672			
grade						
High school	43,140	32,227	75,367	1.954		
graduate						
Some	52,580	36,553	89,133	1.892	87,479	1.918
college						
Associate	55,631	42,307	97,938	1.869		
degree						
Bachelors				1.682		
degree						
Graduate or	92,815	62,198	155,013		155,013	1.652
professional				1.597		
degree						
Total	62,445	44,857	107,302	1.888	N/A	N/A

Note: Income data is in current dollar and is from U.S. Census Bureau (2009). Fertility data is from U.S. Census Bureau (2010). Due to data availability, we calculate the across group average income by taking simple average. The average fertility rate is accurately calculated.

Table 2 Statistics and Expressions

	Statistics	Expression
Share of Total Expenditure on Children	31% - 47%	$\frac{(\alpha_o + \beta_o)k_o^i}{(\alpha_p + \beta_p)k_p^i + (\alpha_o + \beta_o)k_o^i}$
Share of Total Expenditure on Housing	20%	$\frac{\alpha_o k_o^i + \alpha_p k_p^i}{(\alpha_p + \beta_p) k_p^i + (\alpha_o + \beta_o) k_o^i}$
Share of Children's Expenditure on Housing	31%	$\frac{\alpha_{_{o}}}{\alpha_{_{o}}+eta_{_{o}}}$
Share of Total 'Budget' on Leisure	65% - 70%	$rac{k_p^i\eta}{1-k_o^i\gamma}$
Property Tax Rate	1.22% - 1.47% (of house value)	$\frac{\gamma k_o^i}{\alpha_p k_p^i + \alpha_o k_o^i - \gamma k_o^i}$
Fertility Rate	2.521 - 1.652	$\frac{k_n^i}{w_i c k_T^i} Y_i(\mathbf{r})$

Table 3a Parameter Values

a = 2.2	b = 0.1	c = 0.7179	$W_{BA} = 55$	$W_{HA}=32$	$W_{NH} = 20$	$\varepsilon = 0.8$
$k_o^{BA} = 0.176$	$k_o^{HA} = 0.166$	$k_o^{NH} = 0.141$	$k_p^{BA} = 0.824$	$k_p^{HA} = 0.834$	$k_p^{NH} = 0.859$	g = 1
$\eta = 0.78$	$\alpha_p = 0.04$	$\beta_p = 0.18$	$\gamma = 0.165$	$\alpha_{o} = 0.2588$	$\beta_o = 0.5761$	$R_a = $1,237$
$c_1 = 10$	c ₂ = 1	$\overline{N_1} = 200000$	$\overline{N_2} = 250000$	$\overline{N_3} = 50000$		

Table 3b Statistics and Calibration Results

Hannual Income Group 1 51,432 51,233 51,219 46,311 46,837 45,366 48,686 45,234 Income (%) Group 2 87,479 88,288 88,288 87,522 87,615 87,492 87,607 (%) Group 3 155,013 153,394 153,412 152,003 152,075 152,108 152,225 152,232 Time Spent on Working (hour) Group 2 7.64 7.56 7.56 7.56 7.56 7.56 7.56 7.56 7.56 7.56 7.57 7.56 7.55 7.56	Targ	et	Real data	Baseline	SFC	PH1	PH2	VC	SFC+PH	SFC+VC
Income Group 2 87,479 88,288 88,288 87,583 87,522 87,615 87,492 87,607 Group 3 155,013 153,394 153,412 152,030 152,075 152,108 152,225 152,232 Time Spent Group 1 7.02 7.02 6.34 6.42 6.21 6.67 6.20 On Working Group 2 7.64 7.66 7.56 7.55 7.55 7.55 7.55 For Day (hour) 7.64 7.64 7.64 7.63 7.64 7.64 7.64 7.64 Fertility Group 1 2.521 2.566 2.567 2.604 2.568 2.683 2.464 2.691 Rate Group 2 1.918 1.913 1.913 1.915 1.919 1.912 1.921 1.913 Group 3 1.652 1.624 1.626 1.604 1.608 1.612 1.625 1.626 Child-care Group 1 1.3607 1.8421 1.8427 1.8696 1.8437 1.9261 1.7691 1.9320 Time Cost Group 2 7.64 7.63 1.3745 1.3774 1.3728 1.3793 1.3732 per Day (hour) 7.57 7.57 7.57 Proportion Group 1 31% 38.39% 35.34% 35.33% 38.39% 35.29% 38.39% Group 3 47% 7.64 7.64 7.64 7.64 7.64 Froportion Group 1 31% 38.39% 35.44% 35.33% 38.39% 35.29% 38.39% Group 3 47% 7.64 7.64 7.64 7.64 7.64 7.64 Froportion Group 1 31% 38.39% 35.44% 35.33% 38.39% 35.29% 38.39% Group 3 47% 7.64 7.64 7.64 7.64 7.64 7.64 Froportion Group 1 31% 38.39% 35.44% 35.33% 38.39% 35.29% 38.39% Group 3 47% 7.64 7.64 7.64 7.64 7.64 7.64 Froportion Group 1 31% 31% 38.39% 35.39% 35.29% 38.39% Group 3 47% 7.64 7.64 7.64 7.64 7.64 7.64 7.64 7.64 Froportion Group 1 31% 3				Labor	Market-rel	ated variabl	les			
(\$) Group 3 155,013 153,394 153,412 152,030 152,075 152,108 152,225 152,232 Time Spent on Working Per Day (hour) Group 2 7.64 7.62 7.56 </td <td>Annual</td> <td>Group 1</td> <td>51,432</td> <td>51,233</td> <td>51,219</td> <td>46,311</td> <td>46,837</td> <td>45,366</td> <td>48,686</td> <td>45,234</td>	Annual	Group 1	51,432	51,233	51,219	46,311	46,837	45,366	48,686	45,234
Time Spent on Working on Working per Day (hour) Group 2 Group 3 (hour) 7.02 (roup 3) 7.02 (roup 3) 7.02 (roup 3) 7.02 (roup 3) 7.03 (roup 3) 7.04 (roup 3) 7.05 (roup 3) 7.06 (roup 3) 7.07 (roup 3)	Income	Group 2	87,479	88,288	88,288	87,583	87,522	87,615	87,492	87,607
on Working per Day (hour) Group 2 Group 3 (hour) 7.64 (hour) 7.56 (hour) 7.64 (hour)	(\$)	Group 3	155,013	153,394	153,412	152,030	152,075	152,108	152,225	152,232
per Day (hour) Group 3 (hour) Group 3 (hour) 7.64 7.64 7.63 7.64	Time Spent	Group 1		7.02	7.02	6.34	6.42	6.21	6.67	6.20
(hour) Group 1 2.521 2.566 2.567 2.604 2.568 2.683 2.464 2.691 Group 2 1.918 1.913 1.913 1.915 1.919 1.912 1.921 1.913 Child-care Group 1 Group 3 1.652 1.624 1.644 1.606 1.644 1.602 1.625 1.626 Child-care Group 1 Group 1 1.3607 1.8421 1.8427 1.8696 1.8437 1.9261 1.7691 1.9320 per Day (hour) Group 3 1.5110 1.1657 1.1670 1.1511 1.1546 1.1573 1.1664 1.1670 Proportion of Group 2 Group 3 47% 35.44% 35.33% 38.39% 35.29% 38.39% Expenditure on Children Group 3 47% 44.77% 44.77% 44.77% 44.77% 23.10% 4.93% 23.10% Proportion of Total Expenditure on Housing Group 2 Group 3 31% 8.45% 7.55% 31% 7.20% 31%	on Working	Group 2	7.64	7.56	7.56	7.56	7.55	7.56	7.55	7.56
Fertility Group 1 2.521 2.566 2.567 2.604 2.568 2.683 2.464 2.691	per Day	Group 3		7.64	7.64	7.63	7.64	7.64	7.64	7.64
Fertility Rate Group 1 County 2 County 3 County 3 County 4 County 4 County 5 County 5 County 6 County 6 County 6 County 6 County 6 County 7 County 6 County 6 County 7 Coun	(hour)									
Rate Group 2 1.918 1.913 1.913 1.915 1.919 1.912 1.921 1.913 Group 3 1.652 1.624 1.626 1.604 1.608 1.612 1.625 1.626 Child-care Time Cost per Day (hour) Group 2 per Day (hour) 1.3607 1.8421 1.8427 1.8696 1.8437 1.9261 1.7691 1.9320 Proportion of Group 1 of Group 1 of Total Group 2 31% 38.39% 35.44% 35.33% 38.39% 35.29% 38.39% Proportion of Total Group 2 Expenditure on Housing Group 3 on Housing Around Group 2 23.10% 5.82% 5.18% 23.10% 4.93% 23.10% Expenditure on Housing Group 3 on Housing 31% 31% 8.45% 7.55% 31% 7.20% 31% Expenditure on Housing Group 3 on Housing 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Population per Acre Preferred Group 1 Group 2 Group 2 (1.40%) 4.63 5.53 5.43 5.82				Fa	mily-related	l variables				
Group 3	Fertility	Group 1	2.521	2.566	2.567	2.604	2.568	2.683	2.464	2.691
Child-care Time Cost Time Cost Pay (hour) Group 2 (hour) 1.3607 1.8421 1.8427 1.8696 1.8437 1.9261 1.7691 1.9320 Proportion (hour) Group 3 (hour) 1.5110 1.1657 1.1670 1.1511 1.1546 1.1573 1.1664 1.1670 Proportion of Group 2 On Children Group 3 (hour) 47% 38.39% 35.44% 35.33% 38.39% 35.29% 38.39% Expenditure on Children Group 3 (hour) 47% 47% 44.7	Rate	Group 2	1.918	1.913	1.913	1.915	1.919	1.912	1.921	1.913
Time Cost per Day (hour) Group 2 (hour) ~ 1.3736 1.3736 1.3745 1.3777 1.3728 1.3793 1.3732 Proportion (hour) Group 1 of Group 1 of Group 2 31% 38.39% 35.44% 35.33% 38.39% 35.29% 38.39% Expenditure on Children Group 3 on Children Arwan		Group 3	1.652	1.624	1.626	1.604	1.608	1.612	1.625	1.626
per Day (hour) Group 3 (hour) 1.5110 1.1657 1.1670 1.1511 1.1546 1.1573 1.1664 1.1670 Proportion of Group 1 on Children Group 3 on Children 47% 38.39% 35.34% 35.33% 38.39% 35.29% 38.39% Expenditure on Housing Housing Market-related variables Proportion of Total Group 2 Expenditure on Housing Around 23.10% 5.82% 5.18% 23.10% 4.93% 23.10% Share of Children's Group 2 Expenditure on Housing Group 3 31% 31% 8.45% 7.55% 31% 7.20% 31% Population per Acre Housing 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Fred Group 1 Property Group 2 Group 2 I.40% 1.51 1.15 1.15 1.15	Child-care	Group 1	1.3607	1.8421	1.8427	1.8696	1.8437	1.9261	1.7691	1.9320
(hour) Group 1 of Group 2 on Children 31% of Group 3 on Children 38.39% 35.44% 35.33% 38.39% 35.29% 38.39% Expenditure on Children Group 3 of Total of Total Of Total On Housing Around 20% 23.10% 5.82% 5.18% 23.10% 4.93% 23.10% Share of Children's Group 1 On Housing on Housing Group 2 Expenditure on Housing 31% 31% 31% 8.45% 7.55% 31% 7.20% 31% Population per Acre 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Foreight Group 1 Oroup 2 1.40% 1.40% 1.40% 1.40% 1.40%	Time Cost	Group 2	~	1.3736	1.3736	1.3745	1.3777	1.3728	1.3793	1.3732
Proportion of Group 1 of Group 2 Expenditure on Children Group 3 of Group 3 of Children 47% 38.39% 35.44% 35.33% 38.39% 35.29% 38.39% Proportion of Total Expenditure on Housing Group 1 Group 1 Group 3 Around 20% 23.10% 5.82% 5.18% 23.10% 4.93% 23.10% Share of Children's Expenditure on Housing Group 1 Group 3 Group 3 31% 31% 8.45% 7.55% 31% 7.20% 31% Population per Acre 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Property Group 2 Group 1 About About About Brown 1.40% 1.40% 1.40% 1.40%	per Day	Group 3	1.5110	1.1657	1.1670	1.1511	1.1546	1.1573	1.1664	1.1670
Care	(hour)									
Expenditure on Children	Proportion	Group 1	31%	38.39% 35.44% 35.33% 38.39% 35.29% 38.39						38.39%
Children Housing Market-related variables Housing Market-related variables Proportion of Total Expenditure on Housing Group 2 Group 3 Around 20% 5.82% 5.18% 23.10% 4.93% 23.10% Share of Children's Group 2 Expenditure on Housing Group 2 Group 3 31% 31% 8.45% 7.55% 31% 7.20% 31% Population per Acre Preferred Property Group 1 Group 2 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Property Group 2 1.40% 1.40% 1.40% 1.40% 1.40%	of	Group 2	~				43.03%			
Children Housing Market-related variables Proportion of Total Group 2 on Housing Group 3 on Housing Group 1 of Total Group 3 on Housing Around 23.10% 5.82% 5.18% 23.10% 4.93% 23.10% Share of Children's Children's on Housing Group 1 on Housing 31% 31% 31% 8.45% 7.55% 31% 7.20% 31% Population per Acre on Housing Group 3 on Housing 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Property Group 2 or Labout 1.40% 1.40% 1.40% 1.40% 1.40%	Expenditure	Group 3	47%				44.77%			
Proportion Group 1 Around 23.10% 5.82% 5.18% 23.10% 4.93% 23.10%	on									
Proportion of Total of Total of Total Expenditure on Housing on Housing on Housing Group 1 Group 3 (and Housing on Housing or Acre Around 20.1 (and 10.1 (and 10.	Children									
of Total Expenditure on Housing Group 3 on Housing 20% 23.70% Share of Children's Expenditure on Housing Group 1 on Housing 31% 31% 8.45% 7.55% 31% 7.20% 31% Population per Acre Preferred Group 1 Property 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Property Group 2 1.40% 1.40% 1.40%				Housin	g Market-re	lated varial	oles			
Expenditure on Housing Share of Group 1 31% 31% 31% 8.45% 7.55% 31% 7.20% 31% Children's Group 2 Expenditure on Housing Population per Acre 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Group 1 About Property Group 2 1.40%	Proportion	Group 1	Around	23.1	10%	5.82%	5.18%	23.10%	4.93%	23.10%
On Housing Group 1 31% 31% 8.45% 7.55% 31% 7.20% 31% Children's Group 2 on Housing Group 3 on Housing Group 3 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Property Group 2 1.40% 1.40% 1.40%	of Total	Group 2	20%				23.70%			
Share of Children's Children's Expenditure on Housing Group 2 31% 31% 8.45% 7.55% 31% 7.20% 31% Population per Acre 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Property Group 2 1.40% 1.40% 1.40%	Expenditure	Group 3					23.92%			
Children's Expenditure on Housing Group 3 on Housing 31% Population per Acre 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Property Group 1 Group 2 1.40% 1.40% 1.40% 1.40%	on Housing									
Expenditure on Housing Group 3 on Housing Group 3 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Property Group 1 Group 2 About 1.40% 1.40% 1.40%	Share of	Group 1	31%	31%	31%	8.45%	7.55%	31%	7.20%	31%
On Housing Image: Control of Housing of Housing Population per Acre Population per Acre Preferred Group 1 About Property 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Property Group 1 Group 2 1.40% 1.40% 1.40%	Children's	Group 2					31	.%		
Population per Acre 4.63 5.53 5.43 5.82 5.69 5.87 5.24 5.48 Preferred Property Group 1 Group 2 About 1.40% 1.40% 1.40% 1.40%	Expenditure	Group 3								
Preferred Property Group 1 Group 2 About 1.40% 1.40% 1.40%	on Housing									
Property Group 2 1.40% 1.40%	Population	per Acre	4.63	5.53	5.43	5.82	5.69	5.87	5.24	5.48
	Preferred	Group 1	•				1.22%			
Tax Rate Group 3 1.47%		Group 2	1.40%	1.40%						
	Tax Rate	Group 3			1.47%					

Key 2: SFC: School finance consolidation regime; PH1: Public Housing policy regime (Public housing units locate within the fringe distance); PH2: Public Housing policy regime (Public housing units locate outside the fringe distance); VC: Housing Voucher; SFC+PH: School finance consolidation and Public Housing policy (Public housing units locate outside the fringe distance) are imposed simultaneously; SFC + VC: School finance consolidation and Housing Voucher policy are imposed simultaneously

Table 4a Cross-community Welfare Comparison at the Baseline equilibrium

	Total Welfare	Parent Dir	ect Utility	Offspring Quality		
	(Utility level)	West	East	West	East	
Group 1	10.4342	12.3364	12.4337	0.9857	0.9441	
Group 2	11.4934	13.4727	13.5910	2.3647	2.2709	
Group 3	13.6434	14.9952	15.2109	5.0705	4.6966	
Average	12.2474	14.0249		3.0554		

Table 4b Equilibrium Outcome Summary

Variab	les	Baseline	SFC	PH1	PH2	VC	SFC+PH	SFC+VC
			House	hold Distr	ibution			
Number	Group	4.26%	5%	0%	0%	2.69%	0%	5%
of	1							
Household	Group	27.83%	25%	45.35%	39.34%	32.72%	27.66%	25%
in the	2							
West	Group	28.38%	20%	40%	40%	40%	30.62%	20%
	3							
Number	Group	5.74%	5%	10%	10%	7.31%	10%	5%
of	1							
Household	Group	22.17%	25%	4.65%	10.66%	17.28%	22.34%	25%
in the	2							
East	Group	11.62%	20%	0%	0%	0%	9.38%	20%
	3							
			Comm	unity Com	parison			
(W) School (Quality/	564/	406/	618/	774/	741/	632/	386/
Property Ta	x Rate	1.47%	1.40%	1.40%	1.47%	1.47%	1.40%	1.40%
(E) School (Quality/	280/	406/	34/	64/	123/	264/	386/
Property Ta	x Rate	1.40%	1.40%	1.40%	1.40%	1.40%	1.40%	1.40%
(W) Average	Rent (\$)	41,076	39,515	44,709	43,861	43,309	41,212	39,513
(E) Average l	Rent (\$)	37,703	39,515	28,488	29,316	35,172	34,405	39,513
(W) Annual	Income	116,192	110,631	117,810	120,090	120,269	121,491	109,219
(\$)								
(E) Annual In	come (\$)	102,106	110,631	59,255	67,752	75,187	92,726	109,219
(W) Ann	ıual	5,321	4,815	5,362	5,668	5,627	4,578	4,757
Edu-Spendi	ing (\$)							
(E) Ann	ual	4,308	4,815	957	1,651	2,931	4,578	4,757
Edu-Spendi	ing (\$)							

Key 2: SFC: School finance consolidation regime; PH1: Public Housing policy regime (Public housing units locate within the fringe distance); PH2: Public Housing policy regime (Public housing units locate outside the fringe distance); VC: Housing Voucher; SFC+PH: School finance consolidation and Public Housing policy (Public housing units locate outside the fringe distance) are imposed simultaneously; SFC + VC: School finance consolidation and Housing Voucher policy are imposed simultaneously.

Table 5a Summary Statistics of the Model-Generated Data

Variables	Mean		Minimum		Maximum		Standard Deviation	
	West	East	West	East	West	East	West	East
R_{i}	52,605	46,692	26,042	26,050	102,408	82,834	20,560	15,812
D_i	7.2857	5.7909	0.0031	0.0015	14.5629	11.6291	4.1937	3.3888
W_i	41.8436	37.1336	20	20	55	55	13.3761	13.3541

Table 5b Regression Results

$$\log R_i = \beta_0 + \beta_D D_i + \beta_w w_i + u_i$$

	Point Es	timate
	(Standard D	Deviation)
	West	East
$oldsymbol{eta}_{\!\scriptscriptstyle 0}$	11.4857	11.2497
ρ_0	(0.0018)	(0.0016)
$eta_{\scriptscriptstyle D}$	-0.0880	-0.1005
$ ho_D$	(0.0002)	(0.0003)
$oldsymbol{eta}_{\scriptscriptstyle w}$	-0.0011	0.0008
P_w	(0.0001)	(0.0001)
Sample Size	2,800	2,800
R^2	0.9962	0.9951
F-statistics	370,278	286,228

Table 6 Equilibrium Welfare Comparison

Household Type	Baseline	SFC	PH1	PH2	VC	SFC +	SFC +			
						PH	VC			
Welfare Comparison (Consumption-Equivalent Measure %)										
Panel A: Household Level										
Group 1		+0.02	+19.98	+20.22	+18.59	+17.53	+18.93			
Group 2	Benchmark	+0.02	-6.30	-2.69	-2.14	+0.45	-1.62			
Group 3	ımark	+0.01	-5.55	-2.26	-2.06	+0.28	-1.62			
Average		+0.02	-3.46	-0.35	-0.19	+1.92	+0.28			
Panel B: Parent Direct Utility (PDU) Only										
Group 1		-0.44	+31.13	+25.81	+25.79	+7.52	+22.89			
Group 2	Benchmark	+0.15	-5.59	-2.08	-1.58	+0.87	-0.91			
Group 3	ımark	+1.33	-10.33	-9.02	-7.83	-0.79	+0.36			
Average		+0.61	-3.45	-1.98	-1.27	+0.78	+2.05			
Panel C: Offspring Qu	ality (OQ)	Only								
Group 1		+0.75	-10.54	+8.12	-8.13	+39.92	-0.33			
Group 2	Benchmark	-0.24	-6.96	-3.63	-2.66	-1.02	-2.74			
Group 3	mark	-2.28	+3.45	+8.58	+7.14	+1.74	-4.93			
Average		-1.30	-1.78	+3.62	+1.85	+3.58	-4.63			

Key 2: SFC: School finance consolidation regime; PH1: Public Housing policy regime (Public housing units locate within the fringe distance); PH2: Public Housing policy regime (Public housing units locate outside the fringe distance); VC: Housing Voucher; SFC+PH: School finance consolidation and Public Housing policy (Public housing units locate outside the fringe distance) are imposed simultaneously; SFC + VC: School finance consolidation and Housing Voucher policy are imposed simultaneously.

Table 7 Flexibility of Various Choices

Type of Goods	Short-run	Long-run		
Fertility Rate	Inflexible	Flexible		
Lot Size	Inflexible	Flexible		
Rental Rate	Inflexible	Flexible		
Residential Location	Inflexible	Flexible		
Non-durable Good	Flexible	Flexible		
Leisure	Flexible	Flexible		
Property Tax Rate	Flexible	Flexible		
School Quality	Flexible	Flexible		

Table 8a Short-run VS Long-run (Statistics)

Statisti	cs	Baseline	SI	FC	V	C	SFC	+ VC
			SR	LR	SR	LR	SR	LR
Annual	Group 1	51,233	51,170	51,219	44,990	45,366	44,927	45,234
Income	Group 2	88,288	88,149	88,288	88,428	87,615	88,289	87,607
(\$)	Group 3	153,394	153,090	153,412	153,645	152,108	153,339	152,232
Annual	Group 1	38,554	38,576	38,567	40,752	40,311	40,773	40,434
Consumption	Group 2	64,227	64,279	64,224	63,660	63,678	63,712	63,696
(\$)	Group 3	110,175	110,293	110,299	109,197	108,505	109,315	109,415
Hours	Group 1	7.02	7.01	7.02	6.16	6.21	6.15	6.20
Worked per	Group 2	7.56	7.55	7.56	7.57	7.56	7.56	7.56
Day	Group 3	7.64	7.62	7.64	7.65	7.64	7.64	7.64
Voucher Rece	eived per	N.A.	N.A.	N.A.	23.1249	23.1223	23.1249	23.1326
Day (S	S)							
Property Tax	West	1.47%	1.40%	1.40%	1.47%	1.47%	1.40%	1.40%
Rate	East	1.40%	1.40%	1.40%	1.40%	1.40%	1.40%	1.40%
Annual Edv. Spanding	West	5,321	4,761	4,815	5,321	5,627	4,761	4,757
Edu-Spending (\$)	East	4,308	4,761	4,815	4,308	2,931	4,761	4,757
Peer Quality	West	38.67	30.18	30.75	38.02	48.08	29.87	29.62
	East	23.73	30.18	30.75	23.61	15.11	29.87	29.62
School	West	564	394	406	554	741	390	386
Quality	East	280	394	406	279	123	390	386

Key 2: SFC: School finance consolidation regime; VC: Housing Voucher; SFC + VC: School finance consolidation and Housing Voucher policy are imposed simultaneously.

Key 3: SR: Short-run; LR: Long-run.

Key 4: N.A.: Not Applicable.

Table 8b Short-run VS Long-run (Welfare)

Househo	old Type	Baseline	SF	FC	V	C	SFC	+ VC		
			SR	LR	SR	LR	SR	LR		
	Welfare Comparison (Consumption-Equivalent Measure %)									
Panel A: Hou	1	1	r		1		1			
Group 1	W		-3.07	+0.02	+19.01	+18.59	+16.55	+18.93		
	Е		+3.30	+0.02	+19.16	+18.59	+21.79	+18.93		
Group 2	W	Ве	-3.53	+0.02	-1.30	-2.14	-4.80	-1.62		
	Е	nch	+3.72	+0.02	-1.17	-2.14	+2.54	-1.62		
Group 3	W	Benchmark	-3.70	+0.01	-1.33	-2.06	-5.00	-1.62		
	Е		+3.88	+0.01	-1.18	N.A.	+2.69	-1.62		
Ave	rage		-0.70	+0.02	+0.62	-0.19	-0.04	+0.28		
Panel B: Pare	nt Direct Utilit	y Only								
Group 1	W		+0.71	+2.05	+25.55	+21.61	+26.06	+24.80		
	Е		0	-2.32	+25.63	+26.58	+25.63	+21.45		
Group 2	W	Ben	+0.78	+2.28	-1.25	-3.76	-0.26	+1.25		
	Е	Benchmark	0	-2.58	-1.26	+3.68	-1.26	-3.66		
Group 3	W	nark	+0.80	+3.59	-1.29	-5.26	-0.27	+2.64		
	Е		0	-4.38	-1.27	N.A.	-1.27	-5.40		
Ave	rage		+0.48	+0.61	+1.52	-1.27	+2.00	+2.05		
Panel C: Offs	pring Quality (Only								
Group 1	W		-10.69	-3.56	+4.92	+1.08	-5.04	-4.68		
	Е		+9.28	+3.91	+5.26	-10.23	+13.93	+2.87		
Group 2	W	Ber	-10.68	-3.37	-1.38	+0.16	-11.99	-5.95		
	Е	Benchmark	+9.28	+3.64	-1.04	-11.02	+8.20	+1.24		
Group 3	W	ıark	-10.67	-6.22	-1.38	+3.56	-11.99	-8.97		
	Е	+9.28	+7.00	-1.04	N.A.	+8.20	+4.60			
Ave	rage		-2.96	-1.30	-0.97	+1.85	-3.88	-4.63		

Key 2: SFC: School finance consolidation regime; VC: Housing Voucher; SFC + VC: School finance consolidation and Housing Voucher policy are imposed simultaneously.

Key 3: SR: Short-run; LR: Long-run.

Key 4: W: West; E: East.

Key 5: N.A.: No Group 3 household reside in the East under VC policy in the LR.

The following table summarizes different symbols and their corresponding interpretations of the model.

Table A Variables and Parameters

Symbol	Interpretation	Symbol	Interpretation
S_p	lot size for parents	α_p	weight of S_p in parent direct
			utility
Z_p	consumption goods for parents	$oldsymbol{eta}_p$	weight of Z_p in parent direct
			utility
l	leisure time	η	weight of l in parent direct utility
q	educational quality	γ	weight of q in offspring
			quality
S_o	lot size for offspring	$\alpha_{\scriptscriptstyle o}$	weight of S_o in offspring
			quality
Z_o	consumption goods for offspring	$oldsymbol{eta_o}$	weight of Z_o in offspring
			quality
n_o	number of offspring	k_{p}	weight of parent direct utility in the utility function
$g(n_o) = g n_o^{-\varepsilon}$	degree of altruism toward each child	k_o	weight of offspring quality in the utility function
$C(n_o) = cn_o$	time cost of bearing n_o	а	per mile pecuniary cost
	offspring		
w	hourly wage	b	per mile commuting time cost
r	distance from the CBD		