

# Correlations, Value Factor Returns, and Growth Options<sup>\*</sup>

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## Abstract

Ex ante (expected) average equity market correlation is linked to the differential correlation dynamics of growth and value firms, as well as the value premium. It predicts the value premium, returns of growth and value firms, and the level of growth options within an economy for horizons up to one year. A production-based asset-pricing model supports the existence of a homogeneous correlation among stocks with similar growth characteristics, depending on the prevailing idiosyncratic firm variance, increasing in the value of growth options and, hence, is connected to the value premium. Due to its link to growth options and the value premium, implied correlation serves as a leading procyclical state variable. Value Index-based implied correlations improve the predictability of value-related factors.

**Keywords:** implied correlations, production model, value premium, growth options, factor return predictability, option-implied information, trading strategy, diversification, factor risk

**JEL:** G11, G12, G13, G17

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Ex ante (expected) average equity market correlation is linked to the differential correlation dynamics of growth and value firms, as well as the value premium. It predicts the value premium, returns of growth and value firms, and the level of growth options within an economy for horizons up to one year. A production-based asset-pricing model supports the existence of a homogeneous correlation among stocks with similar growth characteristics, depending on the prevailing idiosyncratic firm variance, increasing in the value of growth options and, hence, is connected to the value premium. Due to its link to growth options and the value premium, implied correlation serves as a leading procyclical state variable. Value Index-based implied correlations improve the predictability of value-related factors.

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# I. Introduction

It has long been recognized that the average correlation among stocks serves as an important state variable measuring the diversification benefits in the market. It predicts market returns and risks, and is therefore a variable of interest for investors. The correlation among stocks stems from a variety of sources, depending on other variables on the business cycle. The difference in returns between growth and value portfolios, namely, the value premium is known to be strongly associated with the business cycle through its tight link to economic growth.

The main objective of the paper is to answer the following questions: How are correlations linked to growth options and the business cycle? Through which channel does correlation develop its documented predictability potential? Which stocks contribute most to the average market-wide correlation? Is there a theoretical model motivating the outlined interactions? This paper introduces theoretically motivated empirical evidence that market-wide correlations are related to one of the most fundamental drivers of the economy, namely economic growth. Correlations increase not only in market downturns, as documented in previous research, but also in anticipation of a good state of nature due to an increase in individual growth options and, hence, are related to the business cycle, market returns, and the value premium. Consequently, growth and value portfolios differ not only in their average return (the value premium) but also in their time-varying correlation dynamics, which can be linked, aside from the business cycle, to market-wide correlations.

The interplay of market-wide correlations and growth opportunities is also connected to market returns and the value premium: Expected correlations and future valuations are positively related. Hence, when firms accumulate growth options, growth stocks comove stronger with each other. Due to the accumulation of growth options, growth stocks will gain in value, reflected in an increase in market returns, and due to their overvaluation compared to value stocks in a negative return on the value premium.

My main results can be summarized as follows: i) The extension of the production-based asset-pricing model by Kogan and Papanikolaou (2014) shows that correlations are increasing in the present value of growth options (PVGO), and, therefore, the average correlation among growth stocks and the average correlation among value stocks display a time-varying pattern, in which the former exceeds the latter most of the time. The difference in correlation dynamics is linked to the market cycle and market-wide correlations. The theory is consistent with the explored empirical evidence. ii) In the model, correlation is a function of PVGO, and, therefore, explains future movements of it. Empirically, expected correlations are related to growth and value portfolio characteristics and predict the future changes in the market-wide PVGO. iii) The implications from the theoretical model can be utilized to provide an additional explanation of the already established return predictability results, and to motivate the value return predictability by market-wide correlations. iv) Other Fama and French (2015) value factors are also predicted by expected correlations. Exploiting the more specific information content in implied correlations extracted for the S&P500 Value Index improves the predictability results among value factors and their value and growth components. The higher risks of losing diversification benefits (correlation risk premium) among value stocks, compared to growth stocks, serves as a new empirical explanation for the existence of the value premium.

To obtain the aforementioned results, I proceed as follows.

First, the application of the structural model by Kogan and Papanikolaou (2014) allows me to work out economic mechanisms to explicitly study the expression for the correlation among stocks as a function of growth characteristics. The model confirms a stronger comovement among growth stocks compared to value stocks. In line with the model, I empirically document that the correlation of growth stocks is on average higher than of value stocks (resulting in a positive “correlation delta”).

The expressions for the model-implied idiosyncratic variance (and market variance) allows me to investigate the correlation dynamics in more detail and for different economic regimes. Empirically, the contemporaneous relationship between the correlation delta and market-wide

correlations is on average negative, and, therefore, when markets are expanding (low market-wide correlation), the market rally leads to a stronger comovement among growth stocks (compared to value stocks). The high market capitalization among low book-to-market (B/M) stocks (growth stocks) contributes positively to this effect on a market level.

While the prior result was purely investigating the correlation dynamics, the theoretical finding that correlation is a function of the PVGO motivates the relation between expected market-wide correlations and the changes in the economies characteristics, that is, changes in the PVGO. The anticipation of a future increase in individual PVGOs is reflected in an increase in expected correlation extracted from a large index such as the S&P500, estimated from option data. On a portfolio level, there exists a strong negative (positive) contemporaneous comovement between correlations and the characteristics of the B/M sorted growth (value) firms.<sup>1</sup> The relation between market-wide correlations and the B/M portfolio characteristic is linear and decreasing in growth.

The main theoretical motivation for this paper is the structural model developed by Kogan and Papanikolaou (2014), in which the effect of investment-specific technology shocks (IST) is related to the value of assets in place (VAP) and the PVGO. As a result, the firms' PVGO can be treated as a systematic component affecting the expected stock return negatively and, therefore, giving rise to the value premium. The model however focuses on the cross-section, and not the prediction of stock returns. Therefore the extension of the model allow me to work out detailed economic mechanisms related to the interplay of correlation, that is, its dynamics, growth, and various risk premia.

The explored link between (firm) characteristics and correlation leads to the question of whether these insights can be applied to explain portfolio returns based on growth and value characteristics. The theoretical model motivates me to analyze the closed-form expressions for the firms expected returns, which are negatively related to the PVGO, giving rise to the value premium. Therefore, if expected market-wide correlations can predict changes in one of the

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<sup>1</sup>Book-to-market serves as a proxy for the PVGO.

models' state variable (PVGO), it seems natural that the ability to predict the associated value factor returns is inherited.

Empirically, I document the in-sample predictive power of correlations with respect to the value factor. In univariate regressions, expected correlations, extracted from options data, predict future factor returns for horizons of up to one year. The regression coefficient is highly significant and negative (for both the original factor and its market-neutral version), and its predictive power, measured in terms of  $R^2$ , is increasing from about 2.6% at the monthly horizon to around 22% on a yearly horizon.

By analyzing the individual long and short legs of the HML factor, both legs are predicted positively, which implies that the predictive power of expected correlations is stronger for returns on growth stocks (L). In order to verify that the return predictability of the value premium is not driven by the market return predictability, I construct a market-neutral version of the HML factor (HML\*), where the “pure” value premium (and the legs) is also predicted negatively. The predictive power of expected correlations is stronger for market-neutral returns on value stocks (H\*).

In the last step I emphasize the predictability of returns on growth and value stocks considering only the firms' B/M.<sup>2</sup> Predictive regressions for each decile portfolio sorted on B/M from growth (low B/M) to value (high B/M) show that with increasing decile, the  $R^2$ s are decreasing, confirming that the predictive power of expected correlations is concentrated among growth stocks. For the market-neutral B/M sorted portfolios, the relation is the opposite (predictive power is increasing in B/M), which indicates that implied correlations also measure the presence of “pure” value in the economy.

Overall, the empirical results are robust to various specifications including the usage of realized correlations over longer time horizons, the sample split according to the NBER recession indicator, and controlling for other known predictor variables. It is worth mentioning that

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<sup>2</sup>The HML factor also considers the size of the firm.

implied correlation outperforms realized correlation in terms of  $R^2$ s, confirming the information advantage of an option-implied variable over its realized equivalent.

The gathered empirical evidence connecting market-wide correlations to the various dynamics of growth and value portfolios, and its associated risks, indicates that (expected) correlation serves as a leading procyclical state variable.

Correlation predicts the value premium (HML) and its components. The prediction of the additional Fama and French (2015) value factors, such as CMA and RMW, and their respective long and short components, is extended, considering the regular S&P500 implied correlation and, implied correlations extracted for the S&P500 Value Index.<sup>3</sup> Interestingly, even though the S&P500 Value Index contains only about half of the stocks as the S&P500 parent index, the predictability results for the value factors are similar (or sometimes even superior), as if considering implied correlations extracted for the whole S&P500. Hence, it seems important to compute the correlation of the stocks of interest, instead of considering as many stocks as possible. When comparing the two different implied correlations with their respective realized correlation, it turns out that the implicit correlation risk premia for growth stocks is larger than for value stocks. The finding serves as a new empirical explanation for the existence of the value premium.

## II. Literature Review

This work is related to the literature dealing with theoretical models explaining the returns on the value premium and other asset pricing “anomalies.” Zhang (2005) shows, due to costly reversibility and the countercyclical price of risk, that value firms are less flexible in cutting capital, causing them to be riskier than growth firms, especially in bad times, when the price of risk is high. According to Garleanu, Kogan, and Panageas (2012), growth firms offer a hedge against “displacement risk,” which describes the process of innovation that creates a systematic risk factor, capturing that the young benefit more from innovative activity than

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<sup>3</sup>One can find the S&P500 Value Index under the ticker “SVX” or “IVE” (iShares S&P500 Value ETF).

the old. Kogan and Papanikolaou (2013) argue that firm characteristics are likely correlated within firms' exposure to the same common risk factor, which is not captured by the market. Kogan and Papanikolaou (2014) investigate the impact of investment-specific technology (IST) shocks, reflecting technological advances embodied in new capital goods, on the cross section of stock returns. They are able to show that firms with similar growth opportunities comove with each other, giving rise to the value factor in stock returns. Berk, Green, and Naik (1999) provide a theoretical model showing that stock returns are related to the market value and to book-to-market, serving as a state variable summarizing the firms' risk. Gomes, Kogan, and Zhang (2003) develop a general equilibrium model that links expected stock returns to firm characteristics, such as size, book value, investment, and productivity.

This paper also adds the role of correlation to the strands of literature dealing with systematic risk and idiosyncratic risk, which are known to be connected to the market risk premium, the value premium, growth options, and the business cycle.

Growth options have different risk characteristics than assets in place, and, therefore, also different exposure to systematic risk, measured by the firms' market beta. In the model of Santos and Veronesi (2004), the equity risk premium is low when the dispersion in systematic risk is high. Within their model they fully characterize conditional betas as a function of fundamentals and the aggregate market premium. Petkova and Zhang (2005) decompose market betas into value and growth betas, and find that  $H$  ( $L$ ) carries a positive (negative) beta premium. They further claim that  $HML$  displays a countercyclical pattern of risk and that value (growth) betas tend to covary positively (negatively) with the future market risk premium. Closely related to the market beta dispersion is the cross-sectional return dispersion (RD). In Stivers and Sun (2010) and Angelidis, Sakkas, and Tessaromatis (2015), the authors find, that RD is positively related to the subsequent value premium and negatively related to the aggregated equity premium. Therefore, RD serves as a leading countercyclical state variable, hence a quantity that tends to increase when the overall economy is slowing down. Both papers confirm a countercyclical variation in the value premium.



Campbell, Lettau, Malkiel, and Xu (2001) and Irvine and Pontiff (2009) show empirically an increase in firm-level volatility relative to the market volatility accompanied by a lower average correlation. The latter paper claims that increased competition between firms induces a lower correlation between firms' performance and cash flows, and, therefore, more idiosyncratic risk. Guo and Savickas (2008) argue that changes in average idiosyncratic volatility provides a proxy for changes in the investment opportunity set, which is closely related to the book-to-market factor. An investigation of idiosyncratic market-wide risk and the connection to growth options can be found in Cao, Simin, and Zhao (2008), in which the authors establish a positive relation between the two variables.

Since this paper is also about predictability, I contribute to a strand of literature that uses several macro- and market-based variables to predict returns. Gulen, Xing, and Zhang (2010) study the time-variations of the value premium using a two-state Markov switching frame with time-varying transition probabilities. They connect the sensitivity of expected excess returns of value stocks to high-volatility states, while the expected excess returns of growth stocks are less sensitive to worsening aggregate economic conditions. Asness, Friedman, and Liew (2000) predict annual value strategy returns formed by incorporating and composing three accounting ratios, such as earnings, book value, and sales, via their corresponding spreads. Bollerslev, Todorov, and Xu (2015) predict the value premium insample via their left risk-neutral jump tail variation measure, in which the maximal  $R^2$  is obtained around a four month predictive horizon.

This paper exploits the information content of market-wide equity correlations, which can be extracted backward-looking from historical returns (realized correlations,  $RC$ ), or forward-looking via option data (implied correlations,  $IC$ ). In Pollet and Wilson (2010), long-term market return predictability, that is, quarterly stock market excess returns, are predicted by  $RC$ . Several studies within the field of option-implied information deal with  $IC$ , which quantify the expected diversification benefits, while the correlation risk premium ( $CRP$ ) quantifies the compensation required by agents for being exposed to the risk of losing diversification benefits.

Driessen, Maenhout, and Vilkov (2005) and Driessen, Maenhout, and Vilkov (2009) demonstrate that  $IC$  predicts market returns for horizons up to 12 months. In Buss, Schoenleber, and Vilkov (2018), the authors decompose  $IC$  in its option-implied parts (market variance, cross-sectional dispersion of market betas, average idiosyncratic variance) and analyze the different information content and predictability horizons of these in the scope of market and risk predictability. A good overview about the option-implied predictive literature can be found in Christoffersen, Jacobs, and Chang (2011). To my knowledge, all of these studies explore the relation of market-wide correlations and the return predictability of stock returns on an aggregate market level (S&P500, S&P100, or the DJ30) and not on factors related to growth, value, or the value premium.

The link between correlation and other variables, as summarized in the literature review, are depicted in Figure 1. An overview of the predictive (Panel A) and contemporaneous (Panel B) interplay between (implied) correlations, systematic and idiosyncratic risk, market- and factor returns (and their respective long and short legs), the value premium, and the  $PVGO$  is displayed. In both figures the blue-dashed dotted (red-dashed) line indicates a positive (negative) connection between two edges.

The rest of this paper is organized as follows: Section III states and derives the production model. Section IV shows how to construct the various correlation measures from the (options) data. Section V empirically tests the models main implications. Section VI connects implied correlation to risk measures known to be associated with growth options and the value premium. In Section VII, the value predictability is extended to other factors and other implied correlation measures. Section VIII provides robustness tests. Section IX concludes.

### III. The Model

The production model by Kogan and Papanikolaou (2014) explains the effect of investment-specific technology shocks (IST) on the cross-sectional differences in risk premia, that is, to the firms value of assets in place ( $VAP$ ) and the value of growth opportunities ( $PVGO$ ). Their

major theoretical insight is that the stock returns of growth firms, which benefit the most from positive IST shocks, have higher exposure to IST shocks. In the model, realized returns will have a two-factor structure, and as a result the conditional CAPM fails to price the cross section of stock returns.

While taking the general setting such as the quantity and the form of the state variables as given, in this presented extension, new interesting elements of the model that are in line with the data are studied. The explicit expression of the correlation between two stocks is connected to *PVGO* and differentiated from the index variance through the model-implied idiosyncratic variance. The model implications further support the empirical results associated with the interplay between market returns, the value premium, and market-wide correlations, presented later in the paper.

Within the next sections the main equations of the model are stated and derived; for details, see the original paper or the Appendix I.E.

#### A. *Assets in Place*

Each firm  $f$  owns a finite number of individual projects  $J_t^f$ , which they create over time through investment. The output of an individual project  $j$  equals

$$y_{fjt} = \varepsilon_{ft} u_{jt} x_t K_j^\alpha \quad (1)$$

thereby  $K_j$  denotes the chosen project physical capital,  $u_{jt}$  is a project-specific component of productivity,  $\varepsilon_{ft}$  is the firm-specific component of productivity (skills), and  $x_t$  is a productivity shock affecting the output of the whole economy.

The three state variables capturing firm-specific, project-specific, and economy-wide specific shocks and evolve according to

$$d\varepsilon_{ft} = -\theta_\varepsilon(\varepsilon_{ft} - 1)dt + \sigma_\varepsilon \sqrt{\varepsilon_{ft}} dB_{ft}, \quad (2)$$

$$du_{jt} = -\theta_u(u_{jt} - 1)dt + \sigma_u \sqrt{u_{jt}} dB_{jt}, \quad (3)$$

$$dx_t = \mu_x x_t dt + \sigma_x x_t dB_{xt}, \quad (4)$$

where  $\varepsilon_f$  and  $u_j$  are CIR processes and  $x$  follows a Geometric Brownian motion (generating long-run growth). The Brownian motions  $dB_{ft}$ ,  $dB_{jt}$ , and  $dB_{xt}$  are pairwise independent.

### B. Investment

Firms acquire new projects according to a Poisson process with firm-specific arrival rate

$$\lambda_{ft} = \lambda_f \tilde{\lambda}_{ft}. \quad (5)$$

Thereby  $\tilde{\lambda}_{ft}$  follows a two-state Markov process. The two states are either that a firm is high growth  $\lambda_H$  or low growth  $\lambda_L$ . It is assumed that  $u_{jt}$  is at its long-run mean of 1 at the time of investment.

If a firm decides to invest in a project at time  $t$ , it chooses the amount of capital  $K_j$  and pays the investment costs  $z_t^{-1}x_tK_j$ , where  $z_t$  denotes the cost of capital and follows a Geometric Brownian motion,

$$dz_t = \mu_z z_t dt + \sigma_z z_t dB_{zt}, \quad (6)$$

unrelated to its current level of average productivity  $x_t$ .

### C. Valuation

The stochastic discount factor prices the risk associated with  $x$  and  $z$

$$\frac{d\pi_t}{\pi_t} = -r dt - \gamma_x dB_{xt} - \gamma_z dB_{zt}. \quad (7)$$

Firms' investment decisions are affected by the trade-off between the market value of a new project and the cost of physical capital associated with it. Hence, the firms' market value of an existing project  $j$  at time  $t$  is equal to the present value of its cash flows,

$$p(\varepsilon_{ft}, u_{jt}, x_t, K_j) = E_t \left[ \int_t^\infty e^{-\delta(s-t)} \frac{\pi_s}{\pi_t} y_{fjs} ds \right]. \quad (8)$$

The firm chose  $K^*$  such that it maximizes the *NPV*, which is the difference between the present value of its cash flows  $p(\varepsilon_{ft}, u_{jt}, x_t, K_j)$  and the associated costs of capital  $z_t^{-1}x_tK_j$ .

The value of the firm at time  $t$  can be composed as the market value of its existing project ( $VAP$ ) and the present value of its growth options ( $PVGO$ ). Thereby the present value of cash flows generated by existing projects can, therefore, be written as (see A9)

$$VAP_{ft} = \sum_{j \in J_t^f} p(\varepsilon_{ft}, u_{jt}, x_t, K_j) = x_t \sum_{j \in J_t^f} A(\varepsilon_{ft}, u_{jt}) K_j^\alpha =: x_t \sum_f A_{ft}, \quad (9)$$

while the value of growth opportunities for firm  $f$  is given by the expected discounted NPV of future investments (see A16),

$$PVGO_{ft} = z_t^{\frac{\alpha}{1-\alpha}} x_t G(\varepsilon_{ft}, \lambda_{ft}) =: z_t^{\frac{\alpha}{1-\alpha}} x_t G_{ft}, \quad (10)$$

where  $G_{ft}$  is restated in the appendix of Kogan and Papanikolaou (2014) or in Appendix I.E.

Bringing together equation (9) and equation (10), the value of the firm equals

$$V_{ft} = VAP_{ft} + PVGO_{ft} = x_t \sum_f A_{ft} + z_t^{\frac{\alpha}{1-\alpha}} x_t G_{ft}. \quad (11)$$

#### D. Risk and Risk Premia

The expected excess return of firm  $f$  is (see A30)

$$\frac{1}{dt} E[R_{ft}] - r_f = \gamma_x \sigma_x + \frac{\alpha}{1-\alpha} \gamma_z \sigma_z \frac{PVGO_{ft}}{V_{ft}}. \quad (12)$$

In Kogan and Papanikolaou (2014) the authors argue that the price of risk for disembodied technology shocks  $\gamma_x$  is positive, while the price of risk for IST shock  $\gamma_z$  is negative.<sup>4</sup> This serves as a explanation for the outperformance of value stocks compared to growth stocks and introduces an additional systematic factor in the firms' return structure. Since market-to-book ratios are positively (negatively) correlated with the share of growth opportunities to firm value ( $PVGO/V$ ), growth (value) stocks are more strongly linked to the correction in returns and, hence, display a stronger comovement among themselves.

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<sup>4</sup>Empirically, the authors use the relative stock returns of the investment and consumption good producers to create a factor-mimicking portfolio for the IST shock. The IMC portfolio is long the investment sector and short the consumption sector. Sorting firms on their IST betas results in a declining profile of average stock returns and an increasing profile of market betas. Hence, IST shocks carry a negative risk premium.

### E. Firm Return Dynamics

The dynamics of value of assets in place ( $VAP$ ) and the present value of growth options ( $PVGO$ ) can be expressed as

$$dVAP_{ft} = dx_t \sum_f A_{ft} + x_t d \sum_f A_{ft}, \quad (13)$$

$$dPVGO_{ft} = (z_t^{\frac{\alpha}{1-\alpha}} dx_t + x_t \frac{\alpha}{1-\alpha} z_t^{\frac{\alpha}{1-\alpha}-1} dz_t + x_t R(z_t) dt) G_{ft} + z_t^{\frac{\alpha}{1-\alpha}} x_t dG_{ft}. \quad (14)$$

Therefore, the firms' price follows (see A31):

$$dV_{ft} = dVAP_{ft} + dPVGO_{ft} \quad (15)$$

$$= \bar{R}(z_t) dt + \sigma_x dB_{xt} V_{ft} + \frac{\alpha}{1-\alpha} PVGO_{ft} \sigma_z dB_{zt} + dIdio_f. \quad (16)$$

Hence, the return dynamic of the firm can be written as (see A33)

$$dR_{ft} = \frac{dV_{ft}}{V_{ft}} = E[R_{ft}] dt + \sigma_x dB_{xt} + \frac{\alpha}{1-\alpha} \frac{PVGO_{ft}}{V_{ft}} \sigma_z dB_{zt} + \frac{dIdio_f}{V_{ft}}, \quad (17)$$

where  $dIdio_f$  denotes the dynamics associated to  $A_{ft}$  (as a function of  $\varepsilon_{ft}, u_{jt}, K_j^\alpha$ ) and  $G_{ft}$ .

Since idiosyncratic terms are uncorrelated, one can calculate the covariance between two returns as (see A34)

$$dR_{kt} dR_{lt} = \sigma_x^2 dt + \left(\frac{\alpha}{1-\alpha}\right)^2 \sigma_z^2 \frac{PVGO_{kt}}{V_{kt}} \frac{PVGO_{lt}}{V_{lt}} dt, \quad (18)$$

and, hence, the covariance is increasing in the  $PVGO$ , depending on  $\alpha$  and the volatility of the cost of capital process  $\sigma_z$ . In order to calculate the correlation, one normalizes the covariance by the standard deviations of the respective processes,

$$\sigma^2(dR_{ft}) = dR_{ft} dR_{ft} = \sigma_x^2 dt + \left(\frac{\alpha}{1-\alpha}\right)^2 \sigma_z^2 \left(\frac{PVGO_{ft}}{V_{ft}}\right)^2 dt + \left(\frac{dIdio_f}{V_{ft}}\right)^2. \quad (19)$$

Therefore, the correlation can be calculates as

$$\begin{aligned}
Corr(dR_{kt}, dR_{lt}) &= \frac{dR_{kt}dR_{lt}}{\sqrt{\sigma^2(dR_{kt})}\sqrt{\sigma^2(dR_{lt})}} \\
&= \frac{\sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 \frac{PVGO_{kt}}{V_{kt}} \frac{PVGO_{lt}}{V_{lt}} dt}{\sqrt{\sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 (\frac{PVGO_{kt}}{V_{kt}})^2 dt + (\frac{dIdio_k}{V_{kt}})^2} \sqrt{\sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 (\frac{PVGO_{lt}}{V_{lt}})^2 dt + (\frac{dIdio_l}{V_{lt}})^2}}.
\end{aligned} \tag{20}$$

Figure 9 provides a plot for the correlation between two stocks for different idiosyncratic levels, confirming the positive relationship between average correlation and the individual  $PVGO$ s of the firms. The average correlation among two stocks is lower if the idiosyncratic component of the individual firms is higher and vice versa.

#### F. Market Return Dynamics

In order to obtain some expressions for the aggregate (expected) market return, the results for the individual firms are exploited. Value-weighting equation (12) across its constituents results in the expected market excess return and is given by (see A37)

$$\frac{1}{dt} E[R_{Mt}] - r_f = \gamma_x \sigma_x + \frac{\alpha}{1-\alpha} \gamma_z \sigma_z \frac{PVGO_{Mt}}{V_{Mt}}, \tag{21}$$

where  $\frac{PVGO_{Mt}}{V_{Mt}}$  denotes the market-cap-weighted averaged individual firm ratios  $\frac{PVGO_{ft}}{V_{ft}}$ .<sup>5</sup>

With the principle of diversification, the market variance can be written similarly to equation (18) as (see A38)

$$\sigma^2(dR_{Mt}) = \sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 (\frac{PVGO_{Mt}}{V_{Mt}})^2 dt, \tag{22}$$

indicating that the market variance is an increasing function of  $PVGO_M$ . Figure 10 a provides a plot for the market volatility as a function of the market-wide average of the present value of growth options ( $PVGO_M$ ).

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<sup>5</sup>It is assumed that  $\gamma_x$ ,  $\sigma_x$ ,  $\alpha$  and  $\gamma_z$  are equal for each firm.

With the principle of diversification, the market variance can be written similarly to equation (18) as (see A38)

$$\sigma^2(dR_{Mt}) = \sigma_x^2 dt + \left(\frac{\alpha}{1-\alpha}\right)^2 \sigma_z^2 \left(\frac{PVGO_{Mt}}{V_{Mt}}\right)^2 dt. \quad (23)$$

The main difference between the market variance equation (23) and the correlation among stocks (equation (20)) is captured in the idiosyncratic dynamics of the firm (see A32) as follows:

$$dIdio_f = x_t d \sum_{j \in J_t^f} A(\varepsilon_{ft}, u_{jt}) K_j^\alpha + z_t^{\frac{\alpha}{1-\alpha}} x_t dG(\varepsilon_{ft}, \lambda_{ft}). \quad (24)$$

In order to better understand the idiosyncratic component of the firm, both parts of  $dIdio_f$  are analyzed next.

Since  $d \sum_{j \in J_t^f} A(\varepsilon_{ft}, u_{jt}) K_j^\alpha = \sum_{j \in J_t^f} dA(\varepsilon_{ft}, u_{jt}) K_j^\alpha$ , the object of interest is the change in  $A(\varepsilon_{ft}, u_{jt})$ , which is a function of the firm-specific component  $\varepsilon_{ft}$ , and the project-specific component  $u_{jt}$  and is, therefore, directly associated with the value of assets in place (see A9). As follows from equation (13), the change in  $VAP$  can be decomposed in the change of the economic-wide growth variable  $x_t$  and the change of the project-specific components  $dA(\varepsilon_{ft}, u_{jt})$ . As inferable from A17,  $G(\varepsilon_{ft}, \lambda_{ft})$  is a function of the returns to scale at the project level  $\alpha$ , the firm-specific component  $\varepsilon_{ft}$  (such as managerial skill, i.e., a “success rate” of the project), and the individual firms’ arrival rate of the project  $\lambda_{ft}$ .  $G(\varepsilon_{ft}, \lambda_{ft})$ , therefore, combines the success of the project with the average project arrival rate of the firm. Overall, a high level of idiosyncratic variance corresponds to positive changes in the project-specific components, a high success of the project, and a high project arrival rate. Such economic environments are typically characterized by economic expansion.

In order to distinguish the variables of interest, namely the market variance, the correlation among stocks, and idiosyncratic components, their dynamics are further investigated in a comparative statics setting.

The market volatility is monotonically increasing in the market-wide level of  $PVGO_M$  (Figure 10). Correlation dynamics are richer and can be interpreted as the division of the market



variance by the idiosyncratic variance. In Figure 9 the correlation (equation 20) is depicted as a function of the firms' *PVGOs* and for different idiosyncratic levels (Panel A – Panel D). Comparing the different plots for the correlation between two stocks, it appears that for a low idiosyncratic level (Panel A), the correlation is on average higher whenever the stocks' *PVGOs* are similar (hence, for *PVGOs*, close to 1 or close to 0). The level of correlation among growth (value) stocks is 0.85 (0.75), while the lowest correlation attainable is about 0.55 (if two firms are maximally heterogeneous in their *PVGO* characteristics). For a high idiosyncratic level (Panel D), the correlation is lower and determined by the absolute level of the *PVGOs* rather than the homogeneity among them. Overall, a higher idiosyncratic variance leads to a lower absolute correlation but with the correlation concentrated among the growth stocks. The level of correlation among growth (value) stocks is 0.26 (0.15), while the lowest correlation attainable is about 0.15. In relative terms, the difference in correlation among growth and value stocks is higher (lower) in a low (high) correlation environment (high (low) idiosyncratic variance).

To conclude this section the main predictions of the model, which will later be tested empirically, are restated: i) An average market-wide increase in  $PVGO_M$  reduces the expected market returns (equation 21), and, therefore, variables contemporaneously linked to  $PVGO_M$  should predict market returns and the value premium. ii) The correlation among growth stocks exceeds the correlation among value stocks. iii) The difference in correlation is linked to the market-wide correlations. iv) Correlation is a function of *PVGO* and, therefore, expected correlation should predict future movements in *PVGO*.

Before the empirical testing of the model implications is conducted, availability, preparation, and the construction of the variables is explained in the next section.

## IV. Data and Preparation of Variables

Expected correlations are estimated by comparing the variance of the index with the variance of the portfolio of its components. The composition of all the indices is obtained from

Compustat, while the data on returns and market capitalization are received from CRSP.<sup>6</sup> As a proxy for index weights on each day, the relative market cap of each stock in an index from the previous day is considered.

Computing the option-based variables relies on the Surface File from OptionMetrics, selecting for each underlying options with 30, 91, 182, 273 and 365 days to maturity and (absolute) delta lower or equal to 0.5. The surface proved to be a valuable source of information that can be used in generating in asset-pricing tests (e.g., DeMiguel, Plyakha, Uppal, and Vilkov (2013) and Driessen, Maenhout, and Vilkov (2005), among others).<sup>7</sup>

Option-implied second moments are computed as simple variance swaps following Martin (2013). The options for the S&P500 are available from January 1996 through December 2017 while for the S&P500 Value Index the availability starts in August 2006.<sup>8</sup>

Option-implied equicorrelations are estimated, following Driessen, Maenhout, and Vilkov (2005), from the restriction that the variance of the index  $I$  has to be equal to the variance of the portfolio of its constituents (which holds under both—objective and risk-neutral—measures). Given the variances of the index  $\sigma_I^2(t)$ , its components  $\sigma_i^2(t), i = 1 \dots N$ , and the index weights  $w_i(t)$ , the equicorrelation  $\rho_{ij}(t) = \rho(t)$  is calculated as

$$\rho(t) = \frac{\sigma_I^2(t) - \sum_{i=1}^N w_i(t)^2 \sigma_i^2(t)}{\sum_{i=1}^N \sum_{j \neq i} w_i(t) w_j(t) \sigma_i(t) \sigma_j(t)}. \quad (25)$$

When using risk-neutral implied (realized) variances and volatilities in equation (25), one calculates implied (realized) correlations —  $IC$  ( $RC$ ). In Table I the summary statistics for realized and implied correlations are presented. The time series are displayed in Figure 2 Panels A and C.

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<sup>6</sup>Merging CRSP with Compustat is done via the CCM Linking Table using GVKEY and IID to link to PERMNO, following the second-best method from Dobelman, Kang, and Park (2014).

<sup>7</sup>Matching the historical data with options happens through the historical CUSIP link provided by OptionMetrics. PERMNO is used as the main identifier in the merged database.

<sup>8</sup>The traded continuum of index options on the SVX, i.e., the S&P500 Value Index, is sometimes limited, and the change in the associated implied index variance can be quite large. To overcome the fluctuation, the simple variance swaps are averaged over a rolling window of 5 trading days.

The variance risk premium (*VRP*) (correlation risk premium (*CRP*)) is computed in an *ex ante* version as risk-neutral variance (correlation) observed at the end of day  $t$  minus the realized variance (correlation) from  $t - \Delta t$  to  $t$ .

A number of realized portfolio risk measures computed for each time  $t$  over a particular future horizon of 30, 91, 182, 273, and 365 days are prepared: The cross-sectional dispersion of market betas ( $\sigma^2(\beta_M)$ ) for the available CRSP universe, quantifying portfolio risks — calculated as the cross-sectional variance of the market betas (which are obtained for each stock in the sample over the required future period from a six-factor model<sup>9</sup>).<sup>10</sup> The residuals from the just outlined regressions are considered for the calculation of the sum of squared residuals (*SSR*) at each point in time.<sup>11</sup> Value and growth betas are calculated as in Petkova and Zhang (2005), where value and growth portfolio excess returns ( $H - r_f$  and  $L - r_f$ ) are regressed on the market excess return (*MKTRF*). The return dispersion (*RD*) is obtained following Stivers and Sun (2010), by simply calculating the daily cross-sectional standard deviation of 100 size and book-to-market sorted portfolios returns.

To analyze the correlation dynamics, CRSP stocks are getting classified into growth and value by considering their book-to-market value.<sup>12</sup> Knowing which stock belongs into which decile allows calculating the average correlation within the portfolio, whenever the portfolio was formed.

The US Business Cycle Expansion and Contraction indicator is provided by NBER. The reference dates and business cycle lengths are stated in Appendix I.D.

The return data for the factors and the portfolios are available over the whole sample period and are available in daily and monthly frequency on Kenneth French’s website.<sup>13</sup> The market-neutral versions of the Fama and French factors are obtained by regressing, for each point in

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<sup>9</sup>Considering *MKTRF*, *SMB*, *HML*, *MOM*, *RMW*, and *CMA*.

<sup>10</sup>For the stock to be included in the beta computation for a given period  $t$  to  $t + \Delta t$ , it must have more than 30% of valid returns available.

<sup>11</sup>The *SSR* are either averaged equally; (*EWIV*) or market-cap-weighted (*VWIV*) across firms.

<sup>12</sup>A helpful Python code replicating *HML* and the B/M sorted decile portfolios can be found on WRDS.

<sup>13</sup>A more detailed definition and construction of the individual factors can be found in Fama and French (1993) for *MKTRF*, *SMB*, and *HML*, in Jegadeesh and Titman (1993) and Carhart (1997) for *MOM*, and for *RMW* and *CMA* in Fama and French (2015). A high-level value factor overview is provided in Appendix I.A.

time, the considered value factor on a constant and the market return over a window of 21 business days, as follows

$$HML_{t-21 \rightarrow t} = \alpha + \beta_{MKTRF} MKTRF_{t-21 \rightarrow t} + \varepsilon_t. \quad (26)$$

$\varepsilon_t + \alpha$  are then considered the market-neutral return of the factor at the given date.

The present value of growth options is defined as the present value of dividends from all firms' projects to be adopted in the future and can be calculated as the difference between the aggregate market value and the value of assets in place.

As a first approach measuring the average value of growth options in the economy the market-to-book characteristics for the 10 Fama and French book-to-market sorted portfolios are considered. The data are available on a yearly frequency on Kenneth French's website and covers the period from 1965 to 2017.

To obtain data on a higher frequency and different from Fama and French's book-to-market, several variables associated with the present value of growth options are constructed, as in Cao, Simin, and Zhao (2008): The Market Value to Book Value ratio (*MABA*) proxies for corporate growth options due the incorporation of the market value of assets (only the book value does not). Tobin's *Q* is the ratio between the physical asset market value and its replacement value. The Debt to Equity ratio (*DTE*) represents growth options, since firms with significant growth opportunities may have lower financial leverage (lower *DTE*). From the perspective of trade-off theory, growth firms should use less debt because growth opportunities are intangible assets which cannot be used as collateral in the event of bankruptcy. *CAPEX* acts as a proxy for growth options since capital expenditures lead to new investment opportunities. A direct measure of the present value of growth options (*PVGO*) is also included. In the empirical tests, I follow insights from Cao, Simin, and Zhao (2008) and Long, Wald, and Jingfeng (2002) to obtain the value-weighted averages for *MABA*, *Q*, *DTE*, *CAPEX*, and *PVGO*. Details on the calculation can be found in Appendix I.C. The summary statistics for the value of growth options proxies are displayed in Panel A of Table II.

## V. Testing Model Predictions

In this section the theoretical insights provided in section III are now investigated in an empirical setting. Throughout this section, the focus will lie on correlation, and the summary state variable of the model, which is the present value of growth options. The new theoretical insights are getting first connected to known empirically documented results, such as the return predictability by idiosyncratic variances or market-wide correlations. In a next step, new empirical observations, which are in line with the theory, are investigated and documented, the difference in correlation among growth stocks and among value stocks, and the predictive interplay of market-wide correlations and  $PVGO$  can be seen as the major insights in this analysis.

The discussion starts with two empirical results that have been documented in the past in the scope of market return prediction that support the theory that an average market-wide increase in  $PVGO_{Mt}$  reduces the expected market return, that is, are in line with equation (21)

$$\frac{1}{dt}E[R_{Mt}] - r_f = \gamma_x \sigma_x + \frac{\alpha}{1 - \alpha} \gamma_z \sigma_z \frac{PVGO_{Mt}}{V_{Mt}},$$

where  $\gamma_x(\gamma_z)$  is positive (negative).

First, the interplay of idiosyncratic variance,  $PVGO_M$ , and future market returns is in line with the new theoretical insights, that is, equation (21). As reported by Cao, Simin, and Zhao (2008), aggregate idiosyncratic volatility is (contemporaneously) positively related to  $PVGO_M$ . Guo and Savickas (2008) argue that the value-weighted idiosyncratic volatility measure is negatively related to the future equity premium (controlling for the market volatility).

Second, it is shown that market-wide correlations (realized or implied) predict market returns positively for horizons up to 1 year see Pollet and Wilson (2010), Driessen, Maenhout, and Vilkov (2005), and Buss, Schoenleber, and Vilkov (2018). A potential explanation is again given by equation (21). The contemporaneous correlation between  $IC$  ( $RC$ ) and the proxies for the absolute level of growth options are displayed in Table II. In Panel B the interplay is

presented and behaves as expected: A high market correlation is associated with a low absolute level of growth options in the economy (hence, the sign is negative (positive) for growth option proxies positively (negatively) related to growth options ( $MABA$ ,  $Q$ ,  $CAPEX$ , and  $PVGO$  vs.  $DTE$ ).<sup>14</sup> The results are robust (but weaker) considering the differences in the growth options proxies and (expected) correlations see Panel C. In line with the equation for expected market returns, a low implied correlation corresponds to a high level in  $PVGO_M$  (contemporaneously), and, therefore, to a reduction of the future market return.

Overall, the previously outlined connections motivate from a theoretical point of view the empirical finding that correlation (idiosyncratic volatility) positively (negatively) predicts future market returns.

An additional way of connecting correlations to  $PVGO$  is obtained when investigating the different value characteristics among growth and value stocks. As a first approach connecting market-wide correlations and the value of growth options, the contemporaneous time series correlation for the yearly implied correlations (with 365 days maturity) and the (yearly) market-to-book value of the 10 decile portfolios is calculated. The time series correlation in Figure 5 displays a clear increasing monotonic pattern with the lowest (highest) value for the lowest (highest) book-to-market sorted portfolio ( $-0.5$  vs.  $0.2$ ). Hence, the characteristics of low B/M portfolios (growth firms), are comoving negatively with an increase in implied correlations, while the opposite is true, but less pronounced, for high B/M portfolios (value firms). As shown in the later return predictability, (expected) correlation predicts the return on growth stocks (rather than the return on value stocks).

Not only existing theories fit to the explored theoretical insights, also new predictions of the theory are in line with new empirics. A major hypothesis testable from the model is that correlation is increasing in the  $PVGO$  of the stocks (equation (20)), or in other words, that growth stocks comove more strongly among themselves (compared to value stocks).

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<sup>14</sup>Even though the contemporaneous relationship is on average negative, on a yearly rolling basis it displays time-varying patterns with high absolute correlations between  $-0.75$  to  $0.75$ .

First, the average correlation among growth and value stocks based on the B/M characteristic starting in 1965 is investigated. For each yearly formation date  $t$  (June), all stocks in the corresponding decile are selected and the realized average correlation within the actual holding period from  $t$  to  $t + 1$  is calculated. Figure 3, Panel A, displays the time-varying correlation dynamics of the two portfolios and its difference (called correlation delta). As depicted in the plot, the average correlation delta fluctuates around zero, with a time series average of around 2.5%.

In Figure 3, Panel B, the correlation delta and the recession indicator are displayed together. Peaks in the correlation delta are associated with the recession indicator being equal to 1 (recession). Immediately recognizable, the largest correlation delta peak happened during the dot-com tech bubble where especially companies adapting new internet services experienced a huge market turmoil. In the 90s era such companies were the flagship growth stocks per se.

A second hypothesis testable from the model is the negative relationship between the correlation delta and the market-wide correlation. As emphasized in the model section: The relative difference among the correlation of growth stocks and the correlation of value stocks is higher (lower) in a low (high) correlation environment.

In Figure 4 the correlation delta is plotted against market-wide realized (Panel A) and implied correlations (Panel B). For realized (implied) correlations and the correlation delta the time series correlation is on average negative, about -0.14 (-0.44), affirming that if market conditions are temporarily good (low  $IC$ ), growth stocks comove more strongly with each other (compared to value stocks). Overall, the empirical evidence confirms that the comovement among growth and value stocks differs, and, depending on the economic conditions, they display different correlation dynamics over time. As visible in Figure 6, the high market capitalization among low book-to-market stocks (growth stocks) contributes positively to this effect on a market level.

Investigating the correlation dynamics of the model (equation 20), the hypothesis can be formed that a market-wide correlation proxy (as a function of *PVGO*) can predict future changes in the proxies for the absolute level of growth options.

The main results for the insample predictability of the value of aggregate growth options can be inferred from Table III, where the the following predictive regressions is performed

$$\Delta_{log}GO_{t \rightarrow t+\tau_r} = \gamma + \beta_{IC}IC(t, t + \tau_r) + \varepsilon_t, \quad (27)$$

where *GO* equals *MABA*, *Q*, *DTE*, *CAPEX*, or *PVGO* in the respective regressions. The regressions are repeated, considering *RC* as a correlation proxy over the same sample starting in 1996. As displayed in Table III, *MABA*, *Q*, *CAPEX*, and *PVGO* are positively related to *IC* with significant coefficients for all horizons (30–365 days) and with increasing  $R^2$ s for longer predictive horizons, while future changes in *DTE* are, as expected, negatively related to implied correlations.<sup>15</sup> While the contemporaneous relationship between realized correlations and growth options is comparable as to implied correlations, the predictive power is clearly not: The significance among the coefficients is given for just a few growth level proxies and  $R^2$ s do not exceed 4%.

Equation (12) relates the outperformance of value stocks (over growth stocks) to the present value of growth options. Since future growth proxies are predicted by market-wide correlations, it is expected that the predictive power of correlation is inherited when predicting future returns on B/M sorted portfolios or the value premium. Before getting to the main empirical results, some summary statistics will be provided.

The annualized portfolio statistics (returns, standard deviations, and sharp ratios) for the horizon from 1965 to 2018 of the factors are presented in Table V, Panel A. Table V, Panel B, displays the correlation of the value factors from 1965 to 2018 sampled on a monthly frequency. The value factor is negatively correlated with the market ( $-0.26$ ), in contrast, the corresponding legs of the factor are highly positively correlated with the market ( $0.89$  for *H* and  $0.95$  for *L*).

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<sup>15</sup>As pointed out by Cao, Simin, and Zhao (2008), *MABA*, *Q*, *CAPEX*, and *PVGO* are positively related to the absolute average level of growth options, while *DTE* is negatively related.



In Table V, Panel C, the correlation between the market and the B/M sorted decile portfolios is displayed, which is higher for low B/M portfolios. For the market-neutral value factor  $HML^*$ , its legs  $H^*$  and  $L^*$  and the market-neutral B/M sorted portfolios, the correlation with the market displays lower values (per construction).

The return predictability will be performed on  $HML$ , and  $HML^*$ , and its individual legs ( $H$ ,  $L$ ,  $H^*$ , and  $L^*$ ). In order to illustrate the relation of market-wide correlations and value factor returns, the following specification is performed:

$$r_{t \rightarrow t+\tau_r}^F = \gamma + \beta_{IC} IC(t, t + \tau_r) + \varepsilon_t, \quad (28)$$

where  $r_{t \rightarrow t+\tau_r}^F$  denotes the factor return for a period from  $t$  to  $\tau_r$ . Standard errors are corrected to account for autocorrelation introduced by overlapping return observations, see Newey and West (1987). In order to compare the information content between  $IC$  and  $RC$ , the sample starts from 1996.

The results for the insample return predictability are presented Table VI. Expected correlation predicts the value premium with a negative and significant coefficient for all maturities, with increasing  $R^2$ s ranging from over 2% to almost 23% for a yearly return predictability. The performance of  $IC$  predicting the value premium is displayed in Figure 7, Panel A.

To better understand the source of prediction, the predictability of the long and short legs of the value factor returns are analyzed next. In Table VII the results for the insample predictability of the individual legs of the considered value strategy by  $IC$  and  $RC$  are presented. It turns out that market-wide correlation does not predict value stocks ( $H$ ) but rather the returns of growth stocks ( $L$ ) with positive regression coefficient (and, therefore, its difference ( $HML$ ) with a negative coefficient). The contrary is true for the market-neutral  $HML^*$  factor:  $IC$  and  $RC$  negatively predict value stocks ( $H^*$ ), while returns of growth stocks ( $L^*$ ) are not predicted significantly (and, therefore, the difference  $HML^*$  is predicted negatively). The performance of  $IC$  predicting the different factors is displayed in Figure 7, Panel B.

Even though signs and significance of both predictors are comparable, the advantageous information content of  $IC$  leads to substantial higher significance and  $R^2$  (compared to  $RC$ ). Due to the forward-looking information encapsulated in the derivatives, better predictive results are obtained, and, hence, the rest of the analysis is accomplished using purely expected correlations as a predictor.

To further investigate whether  $IC$  predicts the return on growth or value firms, predictive regressions on the 10 B/M sorted Fama and French decile portfolios are performed. The results are presented in Table VIII and visualized in Figure 8, Panel A, and Panel B. The significance and  $R^2$ s of the univariate regression coefficients shows a monotonic pattern: Starting with high significance for B/M, the statistics are decreasing considering portfolio deciles containing more and more value stocks, and by no later than the fourth decile all significance is gone. The same procedure for the market-neutralized 10 B/M sorted decile portfolios is repeated. The results are presented in Table IX and visualized in Figure 8 Panel C and Panel D. Analogue to the previous results when considering market-neutral portfolios,  $IC$  predicts the portfolios with a larger amount of “pure” value rather than growth, even though the results for the market-neutral B/M portfolios are less linear.

Overall, the return predictability draws a clear picture: Correlation negatively predicts future value factor returns. When considering  $HML$ , the predictiveness is primarily through the positive prediction of the short leg ( $L$ ), which is characterized through a higher amount of growth stocks. In view of the market-neutral value factor  $HML^*$ , the predictiveness is evolving through the negative prediction of the long leg ( $H^*$ ), which contains value stocks. The linear decreasing predictability of B/M sorted portfolios confirms the results.

## VI. Risk Predictability

There are two main strands of literature connecting systematic and idiosyncratic risk to the market risk premium, the value premium, growth options, and especially to the business

cycle. In this section the empirical link between the various risk measures and correlations is investigated, and placed in the wider context (see Figure 1).

In order to explore the existing risk channel predictive regressions for various risk measures on implied and realized correlations are performed,

$$Risk_{t \rightarrow t+\tau_r} = \gamma + \beta_{IC} IC(t, t + \tau_r) + \varepsilon_t, \quad (29)$$

where  $Risk_{t \rightarrow t+\tau_r}$  denotes the realized risk measure for a period from  $t$  to  $\tau_r$ . The set of risk measures consist of the overall market risk level, of the dispersion of market betas  $\sigma^2(\beta_M)$ , value and growth betas  $(\beta_H, \beta_L)$ , the cross-sectional return dispersion ( $RD$ ), and the average idiosyncratic risk proxied by the equally and value-weighted sum of squared residuals ( $EWIV$  and  $VWIV$ ) estimated via a Fama and French six-factor model.

The results for the dispersion of market betas are presented in Table IV and are confirm the results in Buss, Schoenleber, and Vilkov (2018). On an aggregated market level,  $IC$  and  $RC$  predict the dispersion of market betas for all horizons with a negative significant coefficient and  $R^2$ s ranging from 2% to 25%. An increase in market-wide correlation translates to a concentration of the market betas around their mean, decreasing the diversification possibilities. Market-wide correlations are able to capture the dispersion of market betas. The results are in line with the findings of Santos and Veronesi (2004), that is, the dispersion of market betas is positively related to growth opportunities, which, in turn, are negatively related to the equity risk premium.

For value and growth betas, the signs are in line with the results by Petkova and Zhang (2005), and market-wide correlations positively (negatively) predict future value (growth) betas, and are, therefore, directionally correctly comoving with the expected market risk premium.

$IC$  loads negatively on the future return dispersion, estimated as the cross-sectional return dispersion ( $RD$ ) from the 100 book-to-market and size sorted portfolios, again indicating that the market moves intensified in one direction during times of turmoil. As Stivers and Sun (2010) argue:  $RD$  increases when the economy is slowing down (leading countercyclical state

variable); that is, it is negatively related with the market return and positively related with the value premium. Since  $IC$  ( $RC$ ) is negatively related to the future return dispersion and the value premium, and positively related to the future market excess return, one can argue that  $IC$  ( $RC$ ) serves as a leading procyclical state variable.

Market-wide correlations are loading negatively on the future average idiosyncratic risk, proxied by the equal ( $EWIV$ )–or value ( $VWIV$ )–weighted  $SSR$  (the sum of squared residuals estimated via a six-factor model). In line with the intuition, increasing correlation lowers the prevalent idiosyncratic risk in the market. The  $R^2$ s for regressions predicting the value-weighted implied volatility exceeds the  $R^2$ s for regressions predicting the equally weighted implied volatility by far. By showing that  $IC$  predicts future idiosyncratic stock market volatility with a negative sign, one can indirectly relate  $IC$  to the future US value premium which serves as the link between the two findings Guo and Savickas (2008), since their idiosyncratic volatility measure is negatively related to the future US equity premium (controlling for the market volatility), positively related to the future US value premium, and contemporaneously negative related to the aggregate B/M ratio.<sup>16</sup>

Overall, correlation does not only predict the value factor by itself (as shown in the previous section) but also risk measures, which are known to be associated with the value premium, the market equity premium, and the present value of growth options.

## VII. Additional Evidence

In this section I investigate whether implied correlations also predict other Fama and French (2015) value factors. In the next step the predictability is repeated, exploiting the more specific information content for implied correlations extracted for the S&P Value Index. At the end, the different correlation risk premia for the market, growth stocks, and value stocks are discussed.

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<sup>16</sup>See Guo and Savickas (2008) Table 5 and Table 7.

### A. Predicting Value with Correlations constructed for the S&P500

Closely related to the book-to-market concept are factors considering the investment expenses or the individual operating profitability of the company. Such factors deliver an excess return by investing in companies with conservative versus aggressive investments expenses (*CMA*, Conservative Minus Aggressive) or by investing in companies with higher operating probability (*RMW*, Robust Minus Weak). The latter two portfolios can theoretically be linked to the book-to-market ratio of the company and, therefore, to the value premium; for a motivation, see Hou, Xue, and Zhang (2015), Fama and French (2006), or the short recap in Appendix I.B.

In the first step of this additional investigation, the predictability and inheritable features of implied correlations, w.r.t, other value strategies outlined above, are analyzed. The main result can be summarized as follows: i) Option-implied correlations extracted from a large index, such as the S&P500, are able to predict the factor returns related to the value premium for horizons up to one year; ii) The predicting channel is evolving through the short legs of the considered value factors (*A* and *W*) or the market-neutral long legs (*C\** and *R\**).

As shown in Table X and visualized in Figure 11 (Panel A and Panel C), *CMA* (*RMW*) is predicted negatively with an  $R^2$  of about 20% (32%) for the yearly horizon. While *CMA* is always on the edge of being significant at the 5% level, *RMW* displays a strong significance across predictive horizons larger than one month.

When investigating the predictability of the individual legs of the factors, see Table XI and Figure 11 (Panel B and Panel D), it turns out that *IC* positively predicts the short leg, that is, predicting returns on companies with aggressive investment behavior (*A*) and companies with low operating profitability (*W*), where the  $R^2$ s reach around 16% for the respective legs for a yearly horizon. When considering the market-neutral version of the legs, the predictability is shifted to the long legs of the value factors (*C\** and *R\**).

Since growth firms (low book-to-market ratio) tend to invest more, the results are in line with the economic theory around the linkage of operating profitability and investment expenditures to growth and value stocks provided by Fama and French (2006) and Zhang (2005).

As discussed in Novy-Marx (2010), the profitability factor always merits some discussion. More profitable firms earn significantly higher average returns than unprofitable firms. They do so despite having, on average, lower book-to-markets and higher market capitalization. Therefore the profitability factor is considered a growth strategy rather than a value strategy. In terms of the author,  $IC$  predicts the returns on “bad value” ( $W$ ) and a market-neutral version of “good growth” ( $R^*$ ).

Analogous to the predictability of  $HML$ ,  $IC$  significantly predicts both legs (of each strategy) positively, but it is important to mention that the  $R^2$ s for predicting the short legs ( $W$  and  $A$ ) are much higher than their long antagonists ( $R$  and  $C$ ), and as a result,  $IC$  loads negatively on their differences,  $RMW$  and  $CMA$ .

### *B. Predicting Value with Correlations Constructed for the S&P500 Value Index*

In most studies, expected correlations are constructed for large major indices, such as the S&P500, S&P100, and DJ30, or the nine economic sectors of the S&P500; see Driessen, Maenhout, and Vilkov (2005), Buss, Schoenleber, and Vilkov (2016), and Buss, Schoenleber, and Vilkov (2018).

This paper is about value and growth, and, therefore, it seems natural to construct implied correlations for a value or growth index. The S&P500 Value Index (IVE) consists of value stocks, which are selected based on three characteristics: the ratios of book value, earnings, and sales to price. The index is rebalanced quarterly and its constituents are drawn from the S&P500 parent index.<sup>17</sup> Index options are available starting from August 2006.<sup>18</sup>

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<sup>17</sup>S&P style Indices divide the complete market capitalization of each parent index into growth and value segments.

<sup>18</sup>Implied correlations for the S&P500 Growth Index are not constructed due to the late availability for the S&P500 Growth Index Option data starting in 2012.

As shown in Table I, the mean of the expected correlation for the S&P500 Value Index is on average larger and, in addition, more volatile, as recognizable in Figure 12. The correlation between the regular  $IC$  and the  $IC_{IVE}$  ranges from 0.48 (for 30 days maturity) to 0.75 (for 365 days maturity).

In the following analysis, the predictive information of two different expected correlations, namely for the S&P500 and the S&P500 Value Index, will be compared in terms of predictability across the three value factors  $HML$ ,  $CMA$ ,  $RMW$ , including their long and short legs.

As visible in Table XIII, when running the insample predictive regressions starting from 2006, the various value premia are predicted with a positive sign. One potential reason, as visible in Figure 4, is that the difference in correlation of growth stocks with the correlation of value stocks comoves positively, with implied correlation starting from around 2007. Additionally, when investigating the individual legs of the value strategies (see Table XIV), it turns out that the predictiveness of the long legs is on average stronger, and, consequentially, the premium prediction is positive.

Figure 13 displays the insample  $R^2$ s for both predictors. Exploiting the value correlation index increases the coefficient of determination by almost 33% (from 15% to 20%) at a yearly horizon when predicting  $HML$ . For  $CMA$ , both expected correlations predict similar, while for  $CMA^*$ ,  $IC_{IVE}$  predicts slightly better on average. For the  $RMW$  growth factor, the market-wide  $IC$  still outperforms the value  $IC_{IVE}$ . The superior information content of expected correlations extracted for the S&P Value Index only inherits partially to the long and short legs of the individual factors. For  $H$  and  $L$ , Figure 14, it turns out that the regular  $IC$  delivers on average slightly better prediction results. For the individual legs of  $CMA$ , the predictive power of  $IC_{IVE}$  stands out, especially for the market-neutral value part  $C^*$ . For  $RMW$ ,  $IC_{IVE}$  outperforms the regular  $IC$  for the  $R$  and  $W$  parts but underperforms when predicting  $R^*$  and  $W^*$ .

The coefficient of determination is not the only way to ascertain whether there is a differential information content in  $IC_{IVE}$  over  $IC$ . Another approach would be to first run

$$IC_{IVE} = \alpha + \beta_{IC}IC + \varepsilon_{IC_{IVE}}, \quad (30)$$

and, hence, to decompose  $IC_{IVE}$  into its part explained by  $IC$ , and the additional information content represented by the residuals  $\varepsilon_{IC_{IVE}}$ . In the next step, future factor returns ( $MKTRF$ ,  $HML$ ,  $CMA$ , and  $RMW$ ) are regressed on market-wide correlations ( $IC$ ) and the residuals  $\varepsilon_{IC_{IVE}}$

$$r_{t \rightarrow t+\tau_r}^F = \gamma + \beta_{IC}IC(t, t + \tau_r) + \beta_{\varepsilon_{IC_{IVE}}} \varepsilon_{IC_{IVE}} + \varepsilon_t, \quad (31)$$

where  $r_{t \rightarrow t+\tau_r}^F$  denotes the factor return for a period from  $t$  to  $\tau_r$ .

The results of the described regression procedure are presented in Table XVI. While the residuals ( $Res_{IC_{IVE}} := \varepsilon_{IC_{IVE}}$ ) are not significant when predicting  $MKTRF$ , they indeed matter when predicting value factor returns with results similar, as presented in Table XIII, indicating that there is significant additional information content in  $IC_{IVE}$  over  $IC$ .<sup>19</sup>

### C. Correlation Risk Premia

The extraction of option implied data for the S&P Value Index not only allows comparing the implied correlations but also the correlation risk premia associated to the S&P500 and the S&P Value Index. As shown in Table XII and displayed in Figure 12, the correlation risk premia for the S&P Value Index ( $IC_V := IC_{IVE}$ ) is (on average) tremendously higher for shorter horizons (up to 182 days) and more volatile, indicating stronger time-varying correlation risk dynamics among value stocks compared to the market itself.

Since there are no index options for the S&P Growth Index, it is assumed that the market correlation  $IC$  can be decomposed (not necessarily linearly) into  $IC_V$  and  $IC_G$ . The S&P Value Index and S&P Growth Index are disjoint, and their union results in the whole S&P500 Index

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<sup>19</sup>Decomposing  $IC$  into  $IC_{IVE}$  and residuals ( $\varepsilon_{IC}$ ), and then predicting  $r_{t \rightarrow t+\tau_r}^F = \gamma + \beta_{IC_{IVE}}IC_{IVE}(t, t + \tau_r) + \beta_{\varepsilon_{IC}}\varepsilon_{IC} + \varepsilon_t$  leads to the same qualitative result. The beta coefficient for the residual ( $\beta_{\varepsilon_{IC}}$ ) is not significant.



itself; therefore, one can assume that  $IC_V \geq IC \geq IC_G$ . With the empirical result that growth stocks comove more strongly among itself,  $RC_G \geq RC_V$ ,<sup>20</sup> one can conclude that

$$CRP_V = IC_V - RC_V \geq IC_G - RC_V \geq IC_G - RC_G = CRP_G. \quad (32)$$

Therefore, despite the fact that the correlation among growth stocks is larger compared to value stocks, the higher correlation risk premium for value stocks serves as another explanation of why value stocks generate higher returns on average.

Overall, the results obtained in this section confirm the following: Expected correlation does not only predict *HML* but also other value-related factors such as *CMA* and *RMW*. In addition, if one considers expected correlation on an even more suited (and even smaller) index, such as the S&P500 Value Index, the predictability of value factors works similar, but sometimes even better. Last, but not least, the different realized and implied correlation dynamics of the subindices confirm that value stocks earn on average higher returns (relative to growth firms) due to the fact that they carry a higher correlation risk premium.

## VIII. Robustness

To verify the robustness results of the analysis to various specifications, a series of tests are carried out and reported in Appendix AI1. Overall, the results in the main part of the paper are robust.

### A. Growth Predictability

The predictive growth options regressions are repeated, that is, equation (27), for realized correlations over the full sample, Table AI101, and over the respective subsample divided by the NBER recession indicator, Table AI102, for realized correlations (starting in 1965) and Table AI103 for implied correlations (starting in 1996).

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<sup>20</sup>Even the realized correlation of the S&P500 Growth Index exceeds the realized correlation of the S&P500 Value Index by 5% on average.

Realized correlations predict changes in future growth option proxies for a horizon up to a quarter. In addition, the predictive power of realized correlations is clearly superior in contraction states. Noticeably the information content of implied correlations stays comparable, regardless of the economic state of the world.

### *B. Return Predictability*

In Table AI104, the return predictability is repeated starting from 1965, using realized correlations as a predictor. The signs for the market return and the value premium are consistent.

To get a comprehensive return predictability result, in the next step, expansion and contraction phases are incorporated. The regressions consider realized correlations as a predictor, starting from 1965, while the sample for implied correlations starts in 1996. Considering realized correlations over the full sample divided into contraction and expansion, Table AI106, it turns out that the predictive power is stronger in contraction states, especially for the pure value premium  $HML^*$ , with  $R^2$ s ranging from 2% to 24% for the period starting in 1965 and the five predictive horizons. The signs of the coefficients are consistently negative within the two subsamples, even though significance is sometimes missing.

As displayed in Table AI107, Panel A, within the contraction phases,  $IC$  predicts  $HML$  and the pure value premium  $HML^*$  stronger for short horizons and for the one-year horizon. Since the recession periods are relatively short, the one-year-ahead return also incorporates the beginnings of the market's recovery phase, and, therefore, the results should be treated with caution. When considering expansion states, Panel B, the results w.r.t  $IC$  stay more or less the same across horizons and the various factors.  $IC$  and  $RC$  do a great job in predicting the pure value returns  $H^*$  during contraction; see Panel A of Table AI108 and Table AI109. For the expansion state (Panel B),  $IC$  predicts similar, as in the full sample, while the  $R^2$ s of  $RC$  are slightly inferior. During contraction, especially for short horizons, the predictive power of market-wide correlations is larger when predicting pure value portfolios ( $H^*$ ) and growth stocks

( $L$ ). A graphical overview about the predictiveness of  $IC$  and the factors, that is their legs in the various states is shown in Figure AI1.

In the insample return predictions in Section V, the traditional variables used in previous studies is controlled. Specifically, the Earnings Price Ratio (EP), the Term Spread (TMS), the Default Yield Spread (DFY), the Book-to-Market Ratio (BTM), and the Net Equity Expansion (NTIS) are included in the regressions. These variables are constructed from the data following the procedures from the study of Goyal and Welch (2008).<sup>21</sup> EP is defined as the log ratio of earnings to prices; TMS is the difference between the long-term yield on government bonds and the Treasury bill; DFY is the difference between BAA- and AAA-rated corporate bond yields; BTM is the ratio of book value to market value for the Dow Jones Industrial Average and NTIS is the ratio of 12-month moving sums of net issues by NYSE listed stocks divided by the total end-of-year market capitalization of NYSE stocks. All these variables are added to the set of predictors and present the results in Table AI110.

## IX. Conclusion

Value strategies follow the approach of buying securities that are undervalued (value stocks) and selling securities that are overvalued (growth stocks), based on its “value” fundamentals, such as a firms book-to-market ratio. As it turns out, not only the return of value and growth firms differ, but also their correlation dynamic. This paper relates, theoretically and empirically, market-wide expected correlation and its dynamics to growth options, growth stocks, and the value premium. An increase in expected correlation happens due to an increase in expectations of economic growth. When firms accumulate growth options, they gain in value simultaneously, thus showing higher correlation. The overvaluation of growth stocks leads to increasing returns on the market and a decreasing value premium.

New insights provided by the production model confirm that correlation is a function of the present value of growth options and that the correlation among growth stocks is on average

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<sup>21</sup>I am grateful to the authors for providing the data on their website.

larger than the correlation among value stocks. The theoretical model also supports existing empirical findings that relate market-wide correlations and idiosyncratic variances, via growth options, to aggregate market returns and the value premium. Theoretically, firm-specific idiosyncratic variance affects correlation and serves as the connector between the market variance and the correlation dynamics.

Empirically validated, correlations are able to predict future changes in growth options with a positive sign, and the comovement among growth stocks is indeed stronger, compared to the comovement among value stocks. Correlation significantly predicts future value factor returns for horizons up to one year with a negative sign. The predictiveness can be attributed to the ability of correlations predicting returns on stocks with low B/M ratios (growth stocks). When considering the pure value premium, that is, a market-neutral version of the value factor, the predictability evolves through the aggregate return on value stocks. In addition to the new economic mechanism, the predictability results could potentially be utilized for a value factor timing strategy in a portfolio management context. Correlations extracted for the S&P500 Value Index improve the predictability results and further motivate the use of implied correlations beyond the large major indices. The larger correlation risk premium among value stocks indicates a bigger fear of losing diversification benefits among value stocks (compared to growth stocks).

Overall, the findings are in line with several papers that connect idiosyncratic and systematic risk to growth options, the value premium, market returns, and the business cycle. Taking together the results, it affirms the hypotheses that correlation serves as a leading procyclical state variable.

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**Table I** Summary Statistics – Correlation Measures

The table reports the summary statistics (time-series mean, p-value for the mean, median, standard deviation, the 10% and 90% percentile) for realized and implied correlations, which are calculated as equicorrelations applying Eq.(25) for the S&P500 Index and for the S&P500 Value Index, for five different maturities of 30, 91, 182, 273, and 365 calendar days. The sample period for realized correlations is ranging from 01/1965 to 12/2017, for implied correlations extracted for the S&P500 from 01/1996 to 12/2017, and for implied correlations for the S&P500 Value Index (*IVE*) from 08/2006 to 12/2017. Second moments are calculated for the index and for all index components from daily realized returns over a respective window for realized variances and as model-free implied variances following Martin (2013) and are sampled on a daily frequency.

*Panel A: Summary Statistics – RC – from 1965*

	<i>RC</i> 30	<i>RC</i> 91	<i>RC</i> 182	<i>RC</i> 273	<i>RC</i> 365
Mean	0.276	0.276	0.278	0.280	0.282
p-val	0.000	0.000	0.000	0.000	0.000
Std	0.133	0.117	0.111	0.109	0.107
Per 10	0.122	0.140	0.150	0.153	0.156
Median	0.256	0.267	0.268	0.271	0.267
Per 90	0.456	0.419	0.409	0.407	0.411

*Panel B: Summary Statistics – IC and RC – from 1996*

	<i>IC</i> 30	<i>IC</i> 91	<i>IC</i> 182	<i>IC</i> 273	<i>IC</i> 365	<i>RC</i> 30	<i>RC</i> 91	<i>RC</i> 182	<i>RC</i> 273	<i>RC</i> 365
Mean	0.378	0.417	0.444	0.453	0.459	0.318	0.316	0.319	0.320	0.320
p-val	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
Std	0.129	0.114	0.105	0.102	0.097	0.148	0.126	0.118	0.114	0.112
Per 10	0.219	0.267	0.317	0.339	0.350	0.152	0.167	0.178	0.181	0.183
Median	0.367	0.416	0.450	0.460	0.462	0.287	0.302	0.306	0.305	0.303
Per 90	0.551	0.563	0.570	0.576	0.578	0.527	0.477	0.456	0.491	0.479

*Panel C: Summary Statistics – IC and RC for the S&P Value Index*

	<i>IC</i> 30	<i>IC</i> 91	<i>IC</i> 182	<i>IC</i> 273	<i>IC</i> 365	<i>RC</i> 30	<i>RC</i> 91	<i>RC</i> 182	<i>RC</i> 273	<i>RC</i> 365
Mean	0.538	0.515	0.518	0.516	0.511	0.393	0.395	0.401	0.406	0.408
p-val	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
Std	0.181	0.130	0.116	0.125	0.135	0.174	0.147	0.133	0.124	0.119
Per 10	0.342	0.363	0.380	0.373	0.359	0.166	0.181	0.219	0.259	0.269
Median	0.491	0.500	0.504	0.497	0.492	0.392	0.399	0.391	0.398	0.413
Per 90	0.812	0.696	0.680	0.696	0.696	0.621	0.604	0.600	0.588	0.582

**Table II** Growth Option Proxies and Correlation Measures

This table displays the summary statistics (Panel A) and the time series correlation of common proxies (and their changes) for the value of growth options with realized correlations ( $RC$ ) calculated from daily realized returns over the respective window and implied correlations ( $IC$ ) from matching-maturity options, both constructed for five different maturities of 30, 91, 182, 273, and 365 calendar days. The proxies for growth options include the ratio of the market value to book value of assets ( $MABA$ ), an estimate of Tobin's  $Q$  ( $Q$ ), the debt to equity ratio ( $DTE$ ), the ratio of capital expenditures to fixed assets ( $CAPEX$ ), and a direct measure of the present value of growth options ( $PVGO$ ). The sample period for the growth option proxies ranges from 1983 to 2018. The data for the calculation of the proxies is obtained from Compustat and available on a monthly frequency. For further details see Appendix I.C. The sample period for realized correlations is ranging from 01/1965 to 12/2017, and for implied correlations extracted for the S&P500 from 01/1996 to 12/2017.

*Panel A: Summary Statistics - Growth Option Proxies*

	MABA	Q	DTE	CAPEX	PVGO
Mean	2.903	2.394	0.276	0.154	0.950
Std	1.594	1.624	0.118	0.049	0.013
Per 10	1.811	1.302	0.144	0.096	0.933
Median	2.533	2.023	0.254	0.152	0.952
Per 90	3.933	3.512	0.454	0.209	0.966
Skew	4.678	4.483	1.152	0.811	-0.573

*Panel B: Contemporaneous Correlation – Levels on Levels*

	$RC_{30}$	$RC_{91}$	$RC_{182}$	$RC_{273}$	$RC_{365}$	$IC_{30}$	$IC_{91}$	$IC_{182}$	$IC_{273}$	$IC_{365}$
MABA	-0.213	-0.264	-0.259	-0.266	-0.275	-0.440	-0.472	-0.512	-0.510	-0.508
Q	-0.210	-0.264	-0.261	-0.264	-0.273	-0.443	-0.471	-0.506	-0.503	-0.499
DTE	0.051	0.071	0.084	0.094	0.128	0.217	0.289	0.277	0.283	0.297
CAPEX	-0.183	-0.180	-0.190	-0.218	-0.243	-0.227	-0.276	-0.320	-0.331	-0.340
PVGO	-0.361	-0.446	-0.482	-0.507	-0.533	-0.518	-0.536	-0.550	-0.562	-0.573

*Panel C: Contemporaneous Correlation – changes on changes*

	$RC_{30}$	$RC_{91}$	$RC_{182}$	$RC_{273}$	$RC_{365}$	$IC_{30}$	$IC_{91}$	$IC_{182}$	$IC_{273}$	$IC_{365}$
MABA	-0.016	-0.078	-0.080	-0.083	-0.076	-0.108	-0.118	-0.127	-0.090	-0.098
Q	-0.007	-0.079	-0.078	-0.077	-0.077	-0.137	-0.142	-0.142	-0.101	-0.106
DTE	0.069	0.040	0.076	0.079	0.074	-0.126	0.049	0.024	0.027	0.081
CAPEX	-0.046	-0.009	-0.027	-0.020	-0.013	0.023	-0.006	0.017	0.029	-0.018
PVGO	-0.063	-0.070	-0.101	-0.094	-0.099	-0.019	-0.156	-0.093	-0.064	-0.119



**Table III** Growth Option Predictability – Changes

This table shows the slope and the  $R^2$ s of the univariate regressions of (log) changes of common proxies for the value of growth options over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations ( $IC$ ) from matching-maturity options and realized correlations ( $RC$ ) calculated from daily realized returns over the respective window. The sample period ranges from 01/1996 to 12/2017 for realized and implied correlations. The proxies for growth options includes the ratio of the market value to book value of assets ( $MABA$ ), an estimate of Tobin's Q ( $Q$ ), the debt to equity ratio ( $DTE$ ), the ratio of capital expenditures to fixed assets ( $CAPEX$ ), and a direct measure of the present value of growth options ( $PVGO$ ). The data for the calculation of the proxies is obtained from Compustat and available on a monthly frequency. For further details see Appendix I.C. The  $p$  – values are computed with Newey and West (1987) standard errors.

30 days				91 days			182 days			273 days			365 days					
$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$				
<i>MABA</i>																		
<i>IC</i>	0.140	0.191	0.050	0.362	0.002	7.114		0.796	0.001	14.818		1.099	0.005	17.956		1.507	0.005	21.525
<i>RC</i>	-0.065	0.501	-0.251	0.252	0.017	3.539		0.224	0.281	1.064		0.375	0.217	2.326		0.559	0.177	3.669
<i>Q</i>																		
<i>IC</i>	0.200	0.092	0.292	0.435	0.001	7.356		0.912	0.001	14.485		1.264	0.003	17.799		1.747	0.003	21.678
<i>RC</i>	-0.095	0.391	-0.175	0.283	0.017	3.176		0.288	0.207	1.399		0.422	0.214	2.187		0.629	0.178	3.471
<i>DTE</i>																		
<i>IC</i>	0.197	0.285	-0.121	-0.204	0.006	4.196		-0.450	0.000	9.337		-0.565	0.002	10.048		-0.655	0.010	9.879
<i>RC</i>	0.094	0.594	-0.292	-0.143	0.041	2.232		-0.173	0.201	1.419		-0.202	0.334	1.309		-0.302	0.223	2.556
<i>CAPEX</i>																		
<i>IC</i>	-0.092	0.516	-0.290	-0.052	0.777	-0.361		-0.072	0.741	-0.352		0.292	0.192	0.096		0.600	0.022	8.873
<i>RC</i>	-0.012	0.930	-0.364	0.094	0.646	-0.287		-0.231	0.235	-0.006		-0.005	0.978	-0.377		0.076	0.759	-0.183
<i>PVGO</i>																		
<i>IC</i>	0.001	0.858	-0.374	0.012	0.000	6.815		0.023	0.000	9.599		0.031	0.000	11.241		0.038	0.000	12.057
<i>RC</i>	-0.000	0.952	-0.365	0.007	0.085	2.320		0.011	0.121	2.137		0.012	0.210	1.814		0.020	0.070	4.129

**Table IV** Risk Predictability – Market Level

This table reports the regression coefficients (with corresponding p-values) and the  $R^2$ s from regressions of various risk measures on implied and realized correlations for horizons of 30 to 365 days. Thereby  $\sigma^2(\beta_M)$  denotes the cross sectional dispersion of market betas,  $EWIV$  ( $VWIV$ ) the equally (value) weighted sum of squared residuals. The measures are calculated from a Fama and French five factor model for the whole CRSP universe.  $\beta_H$  ( $\beta_L$ ) value (growth) betas, are calculated by regressing excess returns of value (growth) portfolios on market excess returns over a rolling window equal to the predictive horizon. Return Dispersion ( $RD$ ) is calculated as the cross sectional dispersion of the 100 size and book-to-market sorted portfolios returns. Realized and option implied equicorrelations are calculated applying Eq.(25) for the S&P500 Index over the sample period ranging from 01/1996 to 12/2017, and for five different maturities of 30, 91, 182, 273, and 365 calendar days. The intercept is not shown. The p-values are computed with Newey and West (1987) standard errors.

30 days				91 days			182 days			273 days			365 days		
$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$	$\beta$	$p - val$	$R^2$	$\beta$	$p - val$	$R^2$	$\beta$	$p - val$	$R^2$
$\sigma^2(\beta_M)$															
<i>IC</i>	-2.255	0.000	2.764	-0.709	0.000	8.411	-0.531	0.000	20.158	-0.408	0.000	25.843	-0.316	0.000	24.674
<i>RC</i>	-3.130	0.000	6.968	-0.861	0.000	15.085	-0.504	0.000	21.082	-0.366	0.001	24.162	-0.283	0.001	25.828
$\beta_H$															
<i>IC</i>	0.589	0.000	5.472	0.873	0.000	11.337	1.107	0.000	18.078	1.192	0.000	21.929	1.232	0.001	22.319
<i>RC</i>	0.696	0.000	9.971	1.024	0.000	18.948	1.283	0.000	28.263	1.506	0.000	40.630	1.606	0.000	49.562
$\beta_L$															
<i>IC</i>	-0.321	0.000	9.238	-0.279	0.000	7.861	-0.216	0.002	5.422	-0.147	0.044	3.014	-0.141	0.079	2.999
<i>RC</i>	-0.146	0.000	2.469	-0.170	0.011	3.545	-0.164	0.094	3.645	-0.129	0.201	2.664	-0.088	0.410	1.491
$EWIV$															
<i>IC</i>	0.002	0.614	0.128	-0.026	0.235	1.855	-0.160	0.001	14.361	-0.282	0.000	19.523	-0.356	0.002	16.700
<i>RC</i>	0.003	0.315	0.631	-0.005	0.827	0.058	-0.066	0.223	2.868	-0.134	0.150	5.111	-0.198	0.126	6.684
$VWIV$															
<i>IC</i>	-0.002	0.194	0.913	-0.030	0.034	6.945	-0.119	0.001	20.210	-0.205	0.000	24.323	-0.272	0.002	21.463
<i>RC</i>	-0.001	0.669	0.087	-0.015	0.221	2.220	-0.060	0.080	5.919	-0.109	0.083	7.961	-0.158	0.078	9.506
$RD$															
<i>IC</i>	-0.068	0.001	5.387	-0.138	0.002	11.931	-0.215	0.000	18.165	-0.259	0.001	18.506	-0.256	0.013	13.349
<i>RC</i>	-0.023	0.157	0.798	-0.056	0.184	2.374	-0.131	0.063	7.788	-0.145	0.132	6.701	-0.155	0.166	6.354

**Table V** Factor Return Overview

This table contains the annualized average return, standard deviation, and sharp ratio of the market- (*MKTRF*) and the value factor returns (*HML*, *HML\**). The monthly timeseries correlation of the respective factors, i.e their long- and short legs, and the book-to-market sorted portfolios is displayed in Panel B and in Panel C. The market neutral returns are estimated applying Eq.(26). The data is obtained from Kenneth French's Website, and ranges from 1965 to the end of 2018.

*Panel A: Factor Return Summary Statistics*

	Ret	Std	Sr
MKTRF	0.048	0.158	0.302
HML	0.037	0.081	0.455
HML*	0.038	0.061	0.618

*Panel B: Monthly Factor Return Correlation*

	MKTRF	H	L	HML	H*	L*	HML*
MKTRF	1.000	0.889	0.953	-0.261	0.197	0.319	-0.046
H	0.889	1.000	0.858	0.120	0.557	0.316	0.273
L	0.953	0.858	1.000	-0.406	0.233	0.571	-0.188
HML	-0.261	0.120	-0.406	1.000	0.537	-0.538	0.844
H*	0.197	0.557	0.233	0.537	1.000	0.211	0.738
L*	0.319	0.316	0.571	-0.538	0.211	1.000	-0.504
HML*	-0.046	0.273	-0.188	0.844	0.738	-0.504	1.000

*Panel C: Monthly Book-to-Market Portfolio Return Correlation*

	MKTRF		MKTRF
Lo10 BM	0.938	Lo10 BM*	-0.154
Dec2 BM	0.946	Dec2 BM*	-0.050
Dec3 BM	0.936	Dec3 BM*	0.070
Dec4 BM	0.909	Dec4 BM*	0.024
Dec5 BM	0.887	Dec5 BM*	-0.011
Dec6 BM	0.850	Dec6 BM*	-0.042
Dec7 BM	0.844	Dec7 BM*	-0.012
Dec8 BM	0.835	Dec8 BM*	-0.019
Dec9 BM	0.862	Dec9 BM*	-0.019
Hi10 BM	0.825	Hi10 BM*	0.127

**Table VI** Insample Factor Return Predictability

The table shows the slope and the  $R^2$ s of the regressions of the excess market and value factor returns realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ), and realized correlations ( $RC$ ) for the S&P500 Index. Implied correlations are computed applying Eq.(25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. Realized correlation are obtained via Eq. (25) and calculated from daily realized returns over a respective backward-looking window, corresponding to the maturity of  $IC$ . The sample period ranges from 01/1996 to 12/2018 for both variables, sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days		Return, 91 days		Return, 182 days		Return, 273 days		Return, 365 days	
<i>MKTRF</i>										
IC	0.057 (0.001)	- -	0.234 (0.000)	- -	0.480 (0.000)	- -	0.668 (0.000)	- -	0.860 (0.000)	- -
RC	- -	0.026 (0.139)	- -	0.112 (0.032)	- -	0.213 (0.032)	- -	0.265 (0.115)	- -	0.474 (0.032)
$R^2$	2.355	0.626	10.936	3.035	19.177	4.507	22.178	4.292	22.690	9.406
<i>HML</i>										
IC	-0.041 (0.007)	- -	-0.148 (0.005)	- -	-0.330 (0.019)	- -	-0.504 (0.035)	- -	-0.720 (0.033)	- -
RC	- -	-0.027 (0.031)	- -	-0.100 (0.044)	- -	-0.117 (0.271)	- -	-0.175 (0.346)	- -	-0.249 (0.345)
$R^2$	2.626	1.492	7.692	4.253	13.985	2.118	17.592	2.608	22.071	3.580
<i>HML*</i>										
IC	-0.037 (0.002)	- -	-0.130 (0.001)	- -	-0.269 (0.002)	- -	-0.396 (0.006)	- -	-0.570 (0.005)	- -
RC	- -	-0.024 (0.022)	- -	-0.109 (0.005)	- -	-0.152 (0.063)	- -	-0.231 (0.103)	- -	-0.338 (0.093)
$R^2$	2.824	1.524	6.682	5.766	11.619	4.447	14.756	6.173	19.349	9.302

**Table VII** Insample Factor Long- and Short Leg Return Predictability

The table shows the slope and the  $R^2$ s of the regressions of the long- and short value factor returns ( $H, L, H^*, L^*$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ), and realized correlations ( $RC$ ) for the S&P500 Index. Implied correlations are computed applying Eq.(25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. Realized correlations  $RC$  are obtained via Eq.(25) and calculated from daily realized returns over a respective backward-looking window, corresponding to the maturity of  $IC$ . The sample period ranges from 01/1996 to 12/2018 for both variables, sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days		Return, 91 days		Return, 182 days		Return, 273 days		Return, 365 days		
<i>H</i>											
IC	0.016 (0.472)	- -	0.099 (0.104)	- -	0.167 (0.145)	- -	0.206 (0.259)	- -	0.219 (0.413)	- -	
RC	- -	-0.005 (0.843)	- -	0.033 (0.657)	- -	0.093 (0.376)	- -	0.094 (0.624)	- -	0.259 (0.339)	
<i>R</i> <sup>2</sup>	0.114	-0.004	1.239	0.149	1.568	0.575	1.420	0.349	0.995	1.932	
<i>L</i>											
IC	0.057 (0.008)	- -	0.247 (0.000)	- -	0.494 (0.000)	- -	0.677 (0.000)	- -	0.875 (0.000)	- -	
RC	- -	0.022 (0.273)	- -	0.135 (0.022)	- -	0.208 (0.072)	- -	0.250 (0.173)	- -	0.473 (0.036)	
<i>R</i> <sup>2</sup>	1.680	0.319	8.494	3.064	15.442	3.280	17.565	2.934	18.838	7.507	
<i>H</i> <sup>*</sup>											
IC	-0.042 (0.000)	- -	-0.131 (0.000)	- -	-0.302 (0.000)	- -	-0.462 (0.001)	- -	-0.672 (0.001)	- -	
RC	- -	-0.031 (0.000)	- -	-0.097 (0.003)	- -	-0.188 (0.010)	- -	-0.296 (0.023)	- -	-0.420 (0.027)	
<i>R</i> <sup>2</sup>	4.886	3.565	9.250	6.179	18.619	8.704	24.121	12.147	29.977	15.979	
<i>L</i> <sup>*</sup>											
IC	-0.005 (0.502)	- -	-0.003 (0.896)	- -	-0.030 (0.281)	- -	-0.060 (0.121)	- -	-0.083 (0.096)	- -	
RC	- -	-0.007 (0.258)	- -	0.011 (0.588)	- -	-0.041 (0.320)	- -	-0.069 (0.209)	- -	-0.081 (0.178)	
<i>R</i> <sup>2</sup>	0.126	0.386	-0.009	0.148	0.458	1.073	1.105	1.794	1.502	1.959	

**Table VIII** Insample Book-to-Market sorted Portfolio Return Predictability

The table shows the slope and the  $R^2$ s of the regressions of the Fama and French book-to-market sorted decile portfolio over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) for the S&P500 Index. Implied correlations are computed applying Eq.(25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 01/1996 to 12/2017, and the variables are sampled at daily frequency. The factor data is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>Lo10 BM</i>					
<i>IC</i>	0.069 (0.000)	0.275 (0.000)	0.550 (0.000)	0.756 (0.000)	1.009 (0.000)
<i>R</i> <sup>2</sup>	3.041	12.947	20.930	23.140	24.737
<i>Dec2 BM</i>					
<i>IC</i>	0.045 (0.004)	0.186 (0.000)	0.349 (0.000)	0.477 (0.001)	0.630 (0.004)
<i>R</i> <sup>2</sup>	1.549	7.524	11.174	12.246	12.890
<i>Dec3 BM</i>					
<i>IC</i>	0.044 (0.004)	0.176 (0.000)	0.332 (0.000)	0.457 (0.000)	0.564 (0.000)
<i>R</i> <sup>2</sup>	1.562	6.990	10.711	12.353	12.186
<i>Dec4 BM</i>					
<i>IC</i>	0.038 (0.037)	0.138 (0.007)	0.232 (0.024)	0.279 (0.055)	0.292 (0.111)
<i>R</i> <sup>2</sup>	0.951	3.642	4.606	4.236	3.069
<i>Dec5 BM</i>					
<i>IC</i>	0.032 (0.090)	0.104 (0.047)	0.147 (0.119)	0.190 (0.144)	0.204 (0.250)
<i>R</i> <sup>2</sup>	0.696	2.023	1.745	1.843	1.350
<i>Dec6 BM</i>					
<i>IC</i>	0.034 (0.047)	0.128 (0.009)	0.201 (0.074)	0.233 (0.161)	0.235 (0.254)
<i>R</i> <sup>2</sup>	0.841	3.200	3.205	2.616	1.758
<i>Dec7 BM</i>					
<i>IC</i>	0.037 (0.052)	0.134 (0.018)	0.214 (0.075)	0.260 (0.131)	0.293 (0.191)
<i>R</i> <sup>2</sup>	0.795	2.696	2.725	2.411	1.939
<i>Dec8 BM</i>					
<i>IC</i>	0.013 (0.563)	0.073 (0.221)	0.132 (0.222)	0.170 (0.312)	0.180 (0.440)
<i>R</i> <sup>2</sup>	0.072	0.777	1.133	1.142	0.810
<i>Dec9 BM</i>					
<i>IC</i>	0.022 (0.318)	0.119 (0.047)	0.201 (0.103)	0.260 (0.197)	0.312 (0.299)
<i>R</i> <sup>2</sup>	0.230	1.856	2.274	2.240	1.971
<i>Hi10 BM</i>					
<i>IC</i>	0.010 (0.742)	0.128 (0.130)	0.229 (0.122)	0.295 (0.221)	0.333 (0.356)
<i>R</i> <sup>2</sup>	0.011	1.221	1.816	1.865	1.464

**Table IX** Insample Market Neutral Book-to-Market sorted Portfolio Return Predictability

The table shows the slope and the  $R^2$ s of the regressions of the Fama and French market neutralized book-to-market sorted decile portfolios over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations ( $IC$ ) for the S&P500 Index. Implied correlations are computed applying Eq.(25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 01/1996 to 12/2017, and the variables are sampled at daily frequency. The market neutral returns are estimated applying equation (26) to the factor returns, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>Lo10 BM*</i>					
IC	0.010 (0.078)	0.029 (0.183)	0.038 (0.437)	0.051 (0.471)	0.118 (0.201)
$R^2$	0.599	0.967	0.706	0.798	2.925
<i>Dec2 BM*</i>					
IC	-0.004 (0.559)	-0.017 (0.364)	-0.061 (0.105)	-0.088 (0.145)	-0.104 (0.232)
$R^2$	0.100	0.654	3.953	4.661	3.900
<i>Dec3 BM*</i>					
IC	-0.003 (0.624)	-0.017 (0.490)	-0.058 (0.274)	-0.086 (0.214)	-0.139 (0.093)
$R^2$	0.062	0.552	2.833	4.478	8.568
<i>Dec4 BM*</i>					
IC	-0.018 (0.016)	-0.092 (0.003)	-0.220 (0.005)	-0.350 (0.004)	-0.531 (0.001)
$R^2$	1.833	9.278	18.229	26.086	37.613
<i>Dec5 BM*</i>					
IC	-0.021 (0.018)	-0.103 (0.002)	-0.259 (0.000)	-0.380 (0.001)	-0.549 (0.000)
$R^2$	1.887	9.094	21.284	28.643	38.110
<i>Dec6 BM*</i>					
IC	-0.014 (0.112)	-0.059 (0.036)	-0.162 (0.019)	-0.259 (0.019)	-0.397 (0.004)
$R^2$	0.827	3.510	9.624	14.744	23.989
<i>Dec7 BM*</i>					
IC	-0.011 (0.236)	-0.055 (0.102)	-0.162 (0.043)	-0.274 (0.024)	-0.441 (0.004)
$R^2$	0.424	2.208	6.574	10.623	16.968
<i>Dec8 BM*</i>					
IC	-0.038 (0.000)	-0.134 (0.000)	-0.275 (0.000)	-0.397 (0.002)	-0.569 (0.001)
$R^2$	3.615	9.472	17.436	22.504	27.758
<i>Dec9 BM*</i>					
IC	-0.039 (0.000)	-0.129 (0.000)	-0.308 (0.001)	-0.467 (0.003)	-0.674 (0.004)
$R^2$	3.385	7.861	16.312	20.071	24.894
<i>Hi10 BM*</i>					
IC	-0.061 (0.000)	-0.153 (0.002)	-0.320 (0.005)	-0.482 (0.005)	-0.721 (0.002)
$R^2$	4.345	6.158	11.060	16.507	24.861

**Table X** Insample Factor Predictability – CMA and RMW

The table shows the slope and the  $R^2$ s of the regressions of the value factor returns ( $CMA$ ,  $CMA^*$ ,  $RMW$ ,  $RMW^*$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) for the S&P500 Index. Implied correlations are computed applying Eq.(25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 01/1996 to 12/2018 when considering implied correlations, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>CMA</i>					
<i>IC</i>	-0.013 (0.169)	-0.074 (0.052)	-0.186 (0.068)	-0.312 (0.065)	-0.457 (0.060)
$R^2$	0.548	4.377	10.213	15.746	19.644
<i>CMA*</i>					
<i>IC</i>	-0.003 (0.688)	-0.026 (0.298)	-0.083 (0.192)	-0.151 (0.143)	-0.218 (0.128)
$R^2$	0.026	0.860	3.303	6.823	8.945
<i>RMW</i>					
<i>IC</i>	-0.018 (0.200)	-0.131 (0.004)	-0.360 (0.000)	-0.572 (0.001)	-0.793 (0.002)
$R^2$	0.679	7.689	20.903	27.184	31.307
<i>RMW*</i>					
<i>IC</i>	0.002 (0.867)	-0.048 (0.145)	-0.174 (0.013)	-0.287 (0.015)	-0.395 (0.031)
$R^2$	-0.007	1.583	8.035	12.339	14.690



**Table XI** Insample Factor Predictability – Legs of CMA and RMW

The table shows the slope and the  $R^2$ s of the regressions of the the long- and short value factor returns ( $C$ ,  $A$ ,  $R$ ,  $W$ ,  $C^*$ ,  $A^*$ ,  $R^*$ ,  $W^*$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) for the S&P500 Index. Implied correlations are computed applying Eq. (25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 01/1996 to 12/2018 when considering implied correlations. The variables are sampled at daily frequency. The market neutral returns are estimated applying Eq. (26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
$C$					
$IC$	0.041 (0.040)	0.175 (0.001)	0.322 (0.000)	0.408 (0.001)	0.492 (0.007)
$R^2$	0.956	4.570	6.725	6.495	6.118
$A$					
$IC$	0.053 (0.023)	0.245 (0.000)	0.492 (0.000)	0.671 (0.000)	0.853 (0.002)
$R^2$	1.295	7.487	13.892	15.968	16.300
$R$					
$IC$	0.039 (0.029)	0.150 (0.001)	0.238 (0.003)	0.289 (0.013)	0.342 (0.044)
$R^2$	1.029	4.392	5.134	4.775	4.232
$W$					
$IC$	0.055 (0.032)	0.271 (0.000)	0.578 (0.000)	0.794 (0.000)	1.007 (0.000)
$R^2$	1.219	7.404	14.434	16.355	16.795
$C^*$					
$IC$	-0.017 (0.021)	-0.052 (0.038)	-0.155 (0.002)	-0.276 (0.001)	-0.408 (0.000)
$R^2$	1.458	2.793	9.543	16.415	21.317
$A^*$					
$IC$	-0.014 (0.072)	-0.024 (0.252)	-0.068 (0.029)	-0.116 (0.006)	-0.174 (0.002)
$R^2$	1.041	0.725	2.783	5.260	8.509
$R^*$					
$IC$	-0.014 (0.004)	-0.060 (0.003)	-0.199 (0.000)	-0.337 (0.000)	-0.488 (0.000)
$R^2$	1.973	7.077	26.466	38.692	46.825
$W^*$					
$IC$	-0.017 (0.128)	-0.014 (0.649)	-0.020 (0.656)	-0.044 (0.507)	-0.081 (0.419)
$R^2$	0.826	0.102	0.093	0.302	0.713

**Table XII** Summary Statistics – Correlation Risk Premia

The table reports the summary statistics (time-series mean, p-value for the mean, median, standard deviation, the 10% and 90% percentile) for the correlation risk premium (implied correlations - realized correlations), which are calculated as equicorrelations applying Eq.(25) for the S&P500 Index and for the S&P500 Value Index, for five different maturities of 30, 91, 182, 273, and 365 calendar days. The sample period is ranging from 08/2006 to 12/2017. Second moments are calculated for the index and for all index components from daily realized returns over a respective window for realized variances and as model-free implied variances following Martin (2013) and are sampled on a daily frequency.

*Panel A: Summary Statistics - Correlation Risk Premium*

	<i>CRP30</i>	<i>CRP91</i>	<i>CRP182</i>	<i>CRP273</i>	<i>CRP365</i>
Mean	0.047	0.090	0.124	0.134	0.132
p-val	0.000	0.000	0.000	0.000	0.000
Std	0.115	0.074	0.071	0.075	0.069
Per 10	-0.100	-0.010	0.024	0.021	0.028
Median	0.055	0.095	0.136	0.154	0.148
Per 90	0.187	0.177	0.209	0.219	0.216

*Panel C: Summary Statistics - Correlation Risk Premium for the S&P Value Index*

	<i>CRP30</i>	<i>CRP91</i>	<i>CRP182</i>	<i>CRP273</i>	<i>CRP365</i>
Mean	0.137	0.114	0.112	0.101	0.088
p-val	0.000	0.000	0.000	0.000	0.000
Std	0.190	0.118	0.090	0.081	0.077
Per 10	-0.074	-0.032	-0.004	-0.000	-0.001
Median	0.121	0.118	0.113	0.102	0.085
Per 90	0.378	0.259	0.216	0.191	0.172

**Table XIII** Insample Factor Predictability –  $IC$  vs.  $IC_{IVE}$ 

The table shows the slope and the  $R^2$ s of the regressions of the value factor returns ( $MKTRF$ ,  $HML$ ,  $HML^*$ ,  $CMA$ ,  $CMA^*$ ,  $RMW$ ,  $RMW^*$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) on the S&P500, and implied correlation ( $IC$ ) on the S&P500 Value Index ( $IVE$ ). Implied correlations are computed applying Eq. (25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 08/2006 to 12/2018, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days		Return, 91 days		Return, 182 days		Return, 273 days		Return, 365 days	
<i>MKTRF</i>										
<i>IC</i>	0.036 (0.077)	- -	0.153 (0.048)	- -	0.413 (0.050)	- -	0.675 (0.037)	- -	0.918 (0.029)	- -
<i>IC<sub>IVE</sub></i>	- -	0.026 (0.073)	- -	0.089 (0.135)	- -	0.320 (0.009)	- -	0.379 (0.006)	- -	0.464 (0.002)
<i>R</i> <sup>2</sup>	0.998	0.925	3.923	1.970	9.158	9.532	13.097	9.535	14.456	12.155
<i>HML</i>										
<i>IC</i>	-0.017 (0.251)	- -	-0.020 (0.685)	- -	0.119 (0.164)	- -	0.300 (0.037)	- -	0.455 (0.024)	- -
<i>IC<sub>IVE</sub></i>	- -	-0.005 (0.655)	- -	-0.013 (0.771)	- -	0.129 (0.015)	- -	0.224 (0.001)	- -	0.279 (0.000)
<i>R</i> <sup>2</sup>	0.544	0.043	0.116	0.063	2.433	4.996	10.175	13.152	15.956	19.780
<i>HML*</i>										
<i>IC</i>	-0.031 (0.020)	- -	-0.098 (0.080)	- -	-0.058 (0.589)	- -	0.058 (0.728)	- -	0.157 (0.503)	- -
<i>IC<sub>IVE</sub></i>	- -	-0.011 (0.262)	- -	-0.049 (0.305)	- -	0.011 (0.877)	- -	0.071 (0.473)	- -	0.082 (0.501)
<i>R</i> <sup>2</sup>	1.992	0.402	3.280	1.209	0.496	0.001	0.329	1.222	1.883	1.687
<i>CMA</i>										
<i>IC</i>	0.011 (0.108)	- -	0.048 (0.053)	- -	0.187 (0.000)	- -	0.319 (0.000)	- -	0.422 (0.000)	- -
<i>IC<sub>IVE</sub></i>	- -	0.012 (0.003)	- -	0.053 (0.007)	- -	0.143 (0.000)	- -	0.212 (0.000)	- -	0.227 (0.000)
<i>R</i> <sup>2</sup>	1.098	2.409	3.174	5.905	16.875	17.182	28.243	28.848	30.114	28.699
<i>CMA*</i>										
<i>IC</i>	0.009 (0.247)	- -	0.036 (0.166)	- -	0.154 (0.004)	- -	0.271 (0.005)	- -	0.375 (0.009)	- -
<i>IC<sub>IVE</sub></i>	- -	0.013 (0.002)	- -	0.048 (0.022)	- -	0.128 (0.001)	- -	0.188 (0.001)	- -	0.197 (0.007)
<i>R</i> <sup>2</sup>	0.627	2.669	1.939	5.000	11.623	14.012	20.163	22.339	23.723	21.489
<i>RMW</i>										
<i>IC</i>	0.003 (0.777)	- -	-0.033 (0.153)	- -	-0.124 (0.070)	- -	-0.218 (0.068)	- -	-0.248 (0.136)	- -
<i>IC<sub>IVE</sub></i>	- -	-0.000 (0.944)	- -	-0.037 (0.062)	- -	-0.102 (0.025)	- -	-0.114 (0.044)	- -	-0.087 (0.128)
<i>R</i> <sup>2</sup>	0.005	-0.033	1.151	2.292	5.732	6.846	9.298	5.822	7.388	2.948
<i>RMW*</i>										
<i>IC</i>	0.012 (0.144)	- -	0.016 (0.411)	- -	-0.009 (0.870)	- -	-0.067 (0.554)	- -	-0.062 (0.710)	- -
<i>IC<sub>IVE</sub></i>	- -	0.005 (0.366)	- -	-0.007 (0.713)	- -	-0.022 (0.619)	- -	-0.028 (0.663)	- -	-0.005 (0.943)
<i>R</i> <sup>2</sup>	1.035	0.342	0.313	0.072	0.006	0.423	1.229	0.471	0.615	-0.023

**Table XIV** Insample Factor Predictability - Legs –  $IC$  vs.  $IC_{IVE}$ 

The table shows the slope and the  $R^2$ s of the regressions of the long- and short value factor returns ( $H$ ,  $L$ ,  $C$ ,  $A$ ,  $R$ ,  $W$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) on the S&P500, and implied correlation ( $IC_{IVE}$ ) on the S&P500 Value Index ( $IVE$ ). Implied correlations are computed applying Eq. (25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 08/2006 to 12/2018, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days		Return, 91 days		Return, 182 days		Return, 273 days		Return, 365 days	
<i>H</i>										
<i>IC</i>	0.023 (0.464)	- -	0.141 (0.153)	- -	0.480 (0.049)	- -	0.854 (0.029)	- -	1.214 (0.022)	- -
<i>IC<sub>IVE</sub></i>	- -	0.022 (0.319)	- -	0.078 (0.340)	- -	0.404 (0.006)	- -	0.536 (0.003)	- -	0.689 (0.000)
<i>R</i> <sup>2</sup>	0.180	0.322	1.773	0.802	7.397	9.090	12.692	11.535	15.174	16.063
<i>L</i>										
<i>IC</i>	0.041 (0.061)	- -	0.164 (0.046)	- -	0.369 (0.111)	- -	0.543 (0.128)	- -	0.710 (0.113)	- -
<i>IC<sub>IVE</sub></i>	- -	0.027 (0.078)	- -	0.091 (0.134)	- -	0.278 (0.045)	- -	0.310 (0.072)	- -	0.393 (0.036)
<i>R</i> <sup>2</sup>	1.113	0.840	4.007	1.826	6.594	6.525	7.814	5.866	8.216	8.286
<i>C</i>										
<i>IC</i>	0.046 (0.061)	- -	0.203 (0.021)	- -	0.547 (0.020)	- -	0.875 (0.012)	- -	1.192 (0.009)	- -
<i>IC<sub>IVE</sub></i>	- -	0.034 (0.042)	- -	0.130 (0.061)	- -	0.429 (0.003)	- -	0.550 (0.001)	- -	0.692 (0.000)
<i>R</i> <sup>2</sup>	1.196	1.187	4.984	3.041	11.771	12.596	16.385	14.964	18.292	20.299
<i>A</i>										
<i>IC</i>	0.034 (0.164)	- -	0.148 (0.093)	- -	0.334 (0.173)	- -	0.517 (0.172)	- -	0.710 (0.144)	- -
<i>IC<sub>IVE</sub></i>	- -	0.022 (0.213)	- -	0.071 (0.271)	- -	0.269 (0.072)	- -	0.311 (0.105)	- -	0.426 (0.056)
<i>R</i> <sup>2</sup>	0.644	0.453	2.731	0.904	4.738	5.330	6.268	5.219	7.140	8.466
<i>R</i>										
<i>IC</i>	0.041 (0.070)	- -	0.161 (0.051)	- -	0.376 (0.087)	- -	0.578 (0.079)	- -	0.807 (0.057)	- -
<i>IC<sub>IVE</sub></i>	- -	0.028 (0.071)	- -	0.084 (0.170)	- -	0.296 (0.026)	- -	0.365 (0.025)	- -	0.500 (0.010)
<i>R</i> <sup>2</sup>	1.092	0.893	3.864	1.534	7.265	7.779	9.581	8.845	11.170	14.131
<i>W</i>										
<i>IC</i>	0.038 (0.159)	- -	0.185 (0.048)	- -	0.477 (0.071)	- -	0.758 (0.062)	- -	1.004 (0.058)	- -
<i>IC<sub>IVE</sub></i>	- -	0.028 (0.140)	- -	0.117 (0.111)	- -	0.385 (0.018)	- -	0.468 (0.019)	- -	0.575 (0.006)
<i>R</i> <sup>2</sup>	0.695	0.674	3.542	2.091	7.756	8.754	10.640	9.352	11.408	12.287

**Table XV** Insample Factor Predictability - Legs –  $IC$  vs.  $IC_{IVE}$ 

The table shows the slope and the  $R^2$ s of the regressions of the long- and short value factor returns ( $H^*$ ,  $L^*$ ,  $C^*$ ,  $A^*$ ,  $R^*$ ,  $W^*$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) on the S&P500, and implied correlation ( $IC$ ) on the S&P500 value index ( $IVE$ ). Implied correlations are computed applying Eq. (25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 08/2006 to 12/2018, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days		Return, 91 days		Return, 182 days		Return, 273 days		Return, 365 days	
$H^*$										
$IC$	-0.024 (0.037)	- -	-0.070 (0.095)	- -	-0.066 (0.409)	- -	-0.023 (0.851)	- -	-0.000 (0.998)	- -
$IC_{IVE}$	- -	-0.012 (0.154)	- -	-0.040 (0.281)	- -	-0.015 (0.784)	- -	0.024 (0.725)	- -	0.033 (0.683)
$R^2$	1.870	0.748	2.815	1.356	1.023	0.064	0.053	0.189	-0.035	0.386
$L^*$										
$IC$	0.006 (0.248)	- -	0.026 (0.214)	- -	-0.011 (0.787)	- -	-0.085 (0.184)	- -	-0.158 (0.059)	- -
$IC_{IVE}$	- -	-0.001 (0.780)	- -	0.009 (0.608)	- -	-0.029 (0.336)	- -	-0.048 (0.285)	- -	-0.049 (0.366)
$R^2$	0.373	-0.014	1.283	0.174	0.062	1.093	3.499	2.564	9.209	2.864
$C^*$										
$IC$	0.005 (0.482)	- -	0.030 (0.187)	- -	0.074 (0.120)	- -	0.102 (0.165)	- -	0.124 (0.234)	- -
$IC_{IVE}$	- -	0.005 (0.226)	- -	0.029 (0.098)	- -	0.062 (0.060)	- -	0.098 (0.012)	- -	0.113 (0.004)
$R^2$	0.203	0.360	1.741	2.460	4.112	5.085	4.795	10.397	4.972	13.734
$A^*$										
$IC$	-0.004 (0.562)	- -	-0.006 (0.766)	- -	-0.076 (0.020)	- -	-0.162 (0.000)	- -	-0.242 (0.000)	- -
$IC_{IVE}$	- -	-0.008 (0.051)	- -	-0.018 (0.204)	- -	-0.064 (0.019)	- -	-0.086 (0.037)	- -	-0.080 (0.125)
$R^2$	0.113	1.334	0.054	1.156	5.172	6.270	14.432	9.423	22.669	8.187
$R^*$										
$IC$	0.005 (0.333)	- -	0.014 (0.363)	- -	-0.024 (0.346)	- -	-0.095 (0.033)	- -	-0.138 (0.073)	- -
$IC_{IVE}$	- -	0.001 (0.810)	- -	-0.000 (0.984)	- -	-0.025 (0.247)	- -	-0.025 (0.424)	- -	-0.005 (0.906)
$R^2$	0.308	-0.019	0.641	-0.035	0.659	1.219	5.539	0.835	7.274	-0.001
$W^*$										
$IC$	-0.007 (0.405)	- -	-0.002 (0.930)	- -	-0.013 (0.822)	- -	-0.021 (0.829)	- -	-0.061 (0.623)	- -
$IC_{IVE}$	- -	-0.004 (0.468)	- -	0.007 (0.725)	- -	-0.002 (0.974)	- -	0.006 (0.925)	- -	0.001 (0.980)
$R^2$	0.318	0.201	-0.029	0.070	0.061	-0.034	0.109	-0.009	0.893	-0.034

**Table XVI** Insample Factor Predictability –  $IC$  vs.  $IC_{IVE}$ 

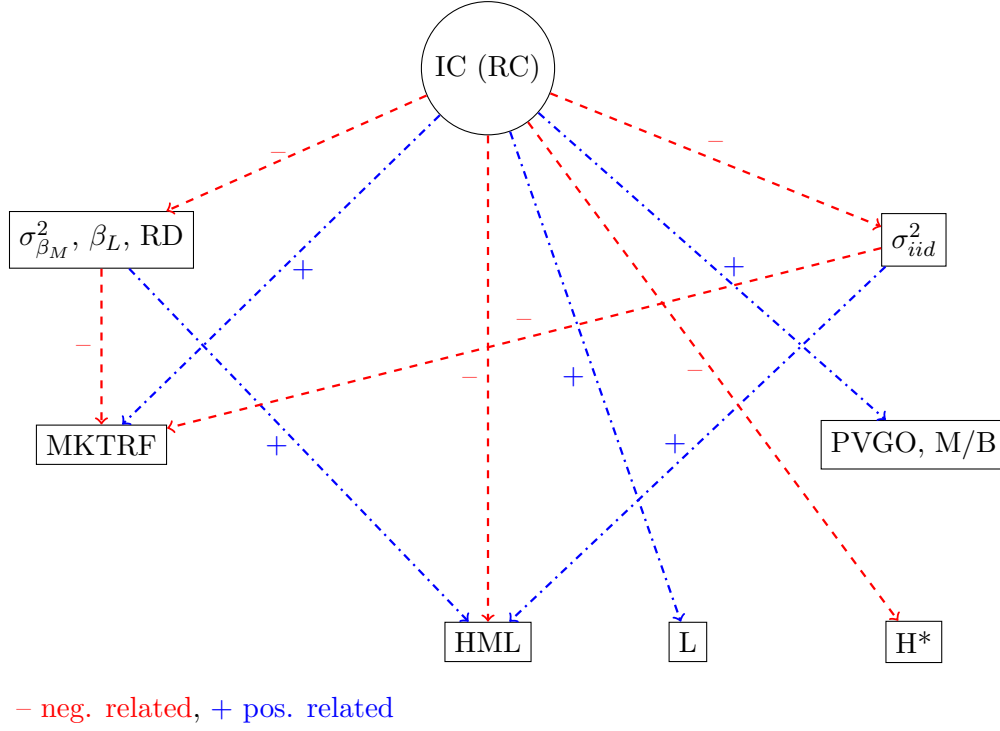
The table shows the slope and the  $R^2$ s of the regressions of the value factor returns ( $MKTRF$ ,  $HML$ ,  $CMA$ , and  $RMW$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) on the S&P500, and the residuals ( $Res_{IC_{IVE}}$ ) obtained from Eq. (30) regressing  $IC_{IVE}$  on implied correlation ( $IC$ ) and a constant. Implied correlations are computed applying Eq. (25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 08/2006 to 12/2018, and the variables are sampled at daily frequency. The factor data is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days		Return, 91 days		Return, 182 days		Return, 273 days		Return, 365 days	
<i>MKTRF</i>										
<i>IC</i>	0.036 (0.077)	0.036 (0.077)	0.153 (0.048)	0.153 (0.048)	0.413 (0.050)	0.413 (0.052)	0.675 (0.037)	0.675 (0.039)	0.918 (0.029)	0.918 (0.030)
<i>Res<sub>IC<sub>IVE</sub></sub></i>	- (0.240)	0.017 (0.240)	- (0.941)	0.005 (0.941)	- (0.032)	0.193 (0.032)	- (0.624)	0.093 (0.624)	- (0.451)	0.200 (0.451)
<i>R<sup>2</sup></i>	0.998	1.258	3.923	3.892	9.158	10.513	13.097	13.302	14.456	15.460
<i>HML</i>										
<i>IC</i>	-0.017 (0.251)	-0.017 (0.251)	-0.020 (0.685)	-0.020 (0.685)	0.119 (0.164)	0.119 (0.145)	0.300 (0.037)	0.300 (0.028)	0.455 (0.024)	0.455 (0.015)
<i>Res<sub>IC<sub>IVE</sub></sub></i>	- (0.819)	0.002 (0.819)	- (0.942)	-0.004 (0.942)	- (0.014)	0.148 (0.014)	- (0.023)	0.177 (0.023)	- (0.015)	0.207 (0.015)
<i>R<sup>2</sup></i>	0.544	0.524	0.116	0.085	2.433	5.030	10.175	13.526	15.956	20.887
<i>CMA</i>										
<i>IC</i>	0.011 (0.108)	0.011 (0.103)	0.048 (0.053)	0.048 (0.052)	0.187 (0.000)	0.187 (0.000)	0.319 (0.000)	0.319 (0.000)	0.422 (0.000)	0.422 (0.000)
<i>Res<sub>IC<sub>IVE</sub></sub></i>	- (0.014)	0.011 (0.014)	- (0.014)	0.050 (0.014)	- (0.128)	0.083 (0.128)	- (0.087)	0.124 (0.087)	- (0.080)	0.122 (0.080)
<i>R<sup>2</sup></i>	1.098	2.479	3.174	5.893	16.875	19.173	28.243	32.285	30.114	33.879
<i>RMW</i>										
<i>IC</i>	0.003 (0.777)	0.003 (0.777)	-0.033 (0.153)	-0.033 (0.152)	-0.124 (0.070)	-0.124 (0.074)	-0.218 (0.068)	-0.218 (0.068)	-0.248 (0.136)	-0.248 (0.137)
<i>Res<sub>IC<sub>IVE</sub></sub></i>	- (0.740)	-0.002 (0.740)	- (0.157)	-0.036 (0.157)	- (0.111)	-0.075 (0.111)	- (0.896)	-0.009 (0.896)	- (0.695)	0.031 (0.695)
<i>R<sup>2</sup></i>	0.005	-0.001	1.151	2.260	5.732	7.156	9.298	9.279	7.388	7.526

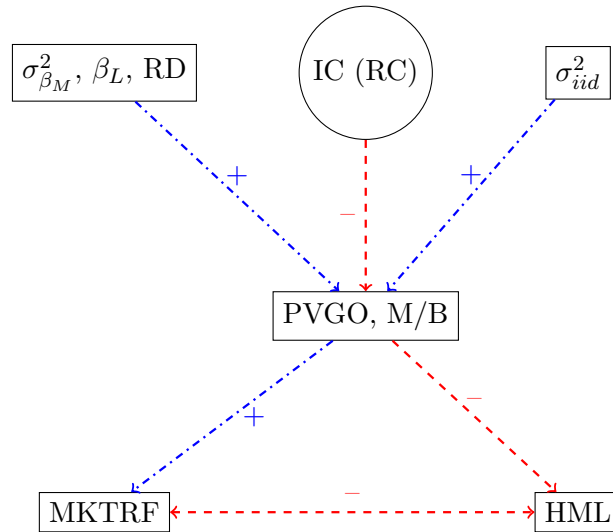
**Figure 1.** The interplay of  $IC$ , Risks, Growth Options, and Factor Returns

The figure displays the relation between implied correlations (at time  $t$ ) and future- risk variables, growth options, and factor returns (Panel A). In Panel B the contemporaneous relation between implied correlations, risk variables, growth options, and factor returns is depicted. The network is collected from several empirical and theoretical research papers explained in Section ?? and complemented by the findings in this paper.

*A: The Predictive Interplay of  $IC$ , Risks, Growth Options, and Factor Returns*



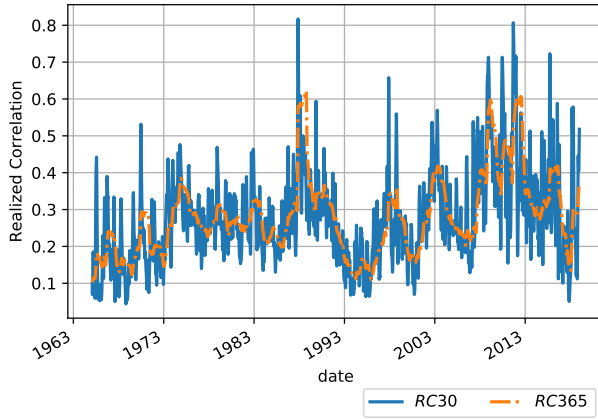
*B: The Contemporaneous Interplay of  $IC$ , Risks, Growth Options, and Factor Returns*



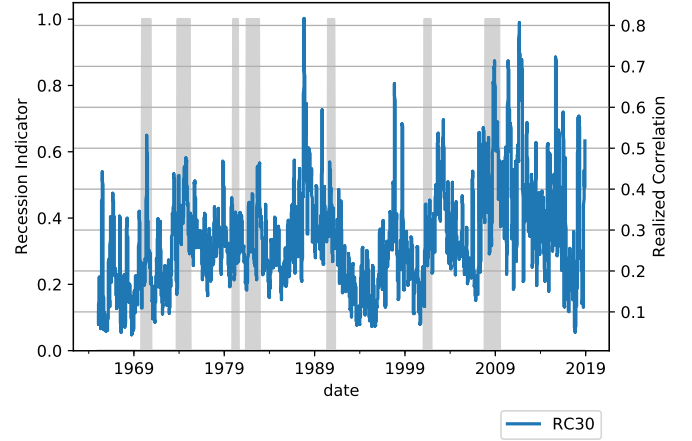
**Figure 2.** Realized and Implied Correlations

The figure shows the time series plot (i.e. the 21 days moving average) of realized correlation ( $RC$ ) and implied correlation ( $IC$ ) for a maturity of 30 and 365 calendar days, in Panel A and Panel C. In Panel B and Panel D realized and implied correlations with a maturity of 30 days are displayed together with the NBER Recession Indicator (see Appendix I.D), which equals 1 if the economy is in recession and 0 elsewhere (expansion). Realized and implied correlations, are calculated as equicorrelations applying Eq.(25) for the S&P500 Index for five different maturities of 30, 91, 182, 273, and 365 calendar days. The sample period for realized correlations is ranging from 01/1965 to 12/2017 and for implied correlations extracted for the S&P500 from 01/1996 to 12/2017. Second moments are calculated for the index and for all index components from daily realized returns over a respective window for realized variances and as model-free implied variances following Martin (2013) and are sampled on a daily frequency.

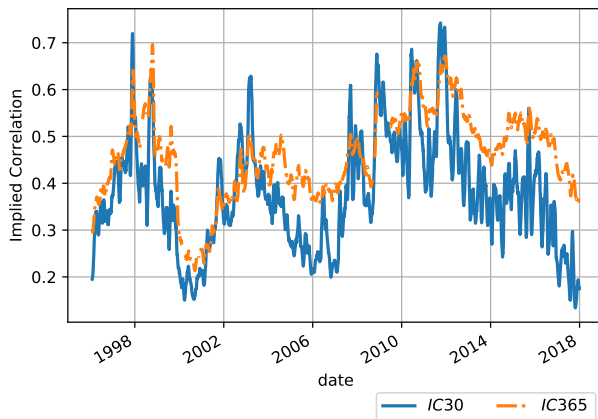
*A:  $RC_{30}$  and  $RC_{365}$*



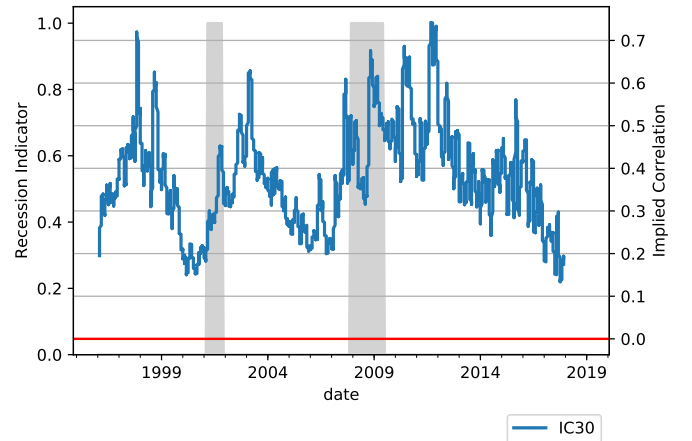
*B:  $RC_{30}$  and Recession Indicator*



*C:  $IC_{30}$  and  $IC_{365}$*



*D:  $IC_{30}$  and Recession Indicator*

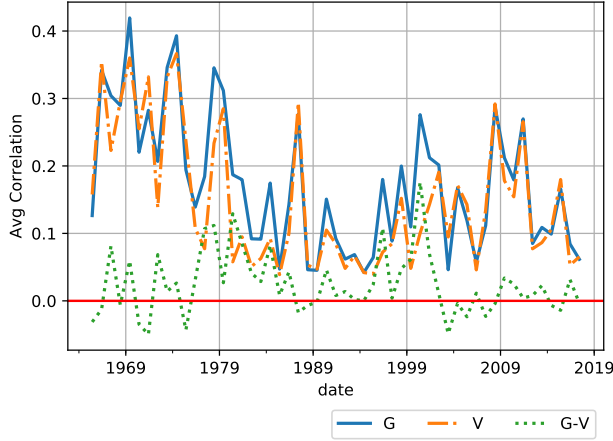




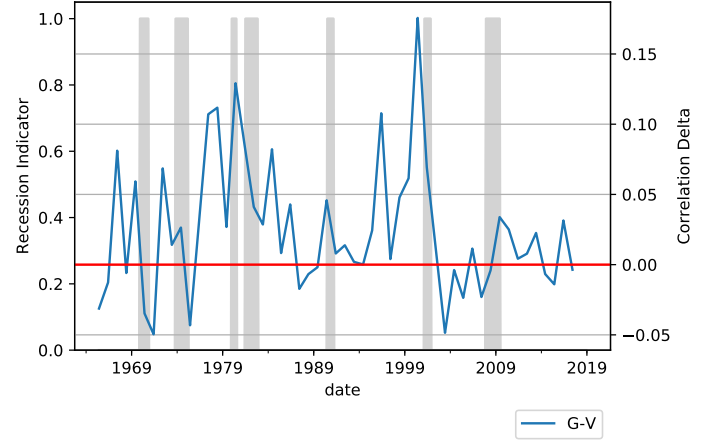
**Figure 3.** Average Correlation in B/M Sorted Portfolios

The figure shows the time series plots of the average correlation in growth ( $G = Lo_{10}$ ) and value ( $V = Hi_{10}$ ) portfolios and its difference, called Correlation Delta ( $\Delta\rho := \rho(G) - \rho(V) = G - V$ ). The yearly average correlation among the various portfolios is calculated in forward looking manner from  $t$  to  $t + 1$ , where  $t$  denotes the rebalancing month (June). The sample period for the measures is ranging from 01/1965 to 12/2017. In Panel B the Correlation Delta is displayed together with the NBER Recession Indicator (see Appendix I.D), which equals 1 if the economy is in recession and 0 elsewhere (expansion). The correlations are calculated using monthly data.

*A: Forward-looking  $\Delta\rho_{t,t+1}$*



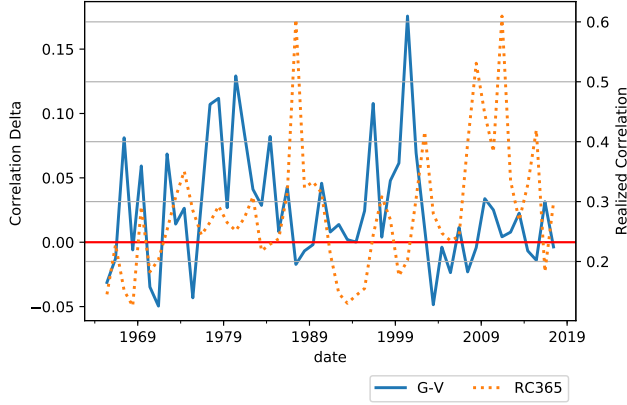
*B:  $\Delta\rho_{t,t+1}$  and Recession Indicator*



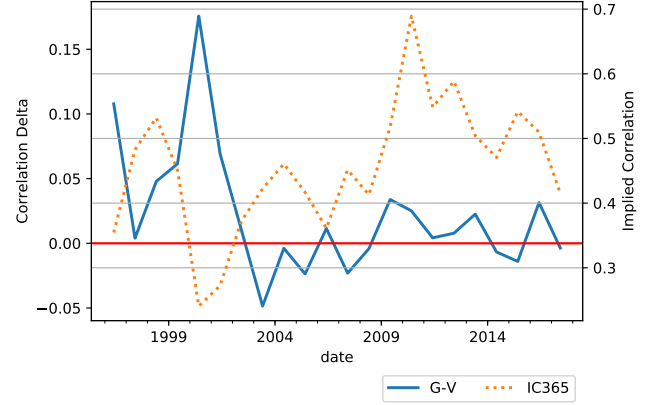
**Figure 4.** Growth-Value Correlation Delta and RC / IC

The figure displays the time series plots of the average Correlation Delta ( $\Delta\rho := \rho(G) - \rho(V) = G - V$ ) together with realized correlations (Panel A) or implied correlations (Panel B). The yearly average Correlation Delta is calculated in a forward looking manner from  $t$  to  $t + 1$ , where  $t$  denotes the rebalancing month (July). The sample period for the measures is ranging from 01/1965 to 12/2017 for realized correlations and for implied correlations extracted for the S&P500 from 01/1996 to 12/2017. Second moments are calculated for the index and for all index components from daily realized returns over a respective window for realized variances and as model-free implied variances following Martin (2013) and are sampled on a yearly frequency.

*A:  $\Delta\rho_{t,t+1}$  and  $RC_{365,t,t+1}$*



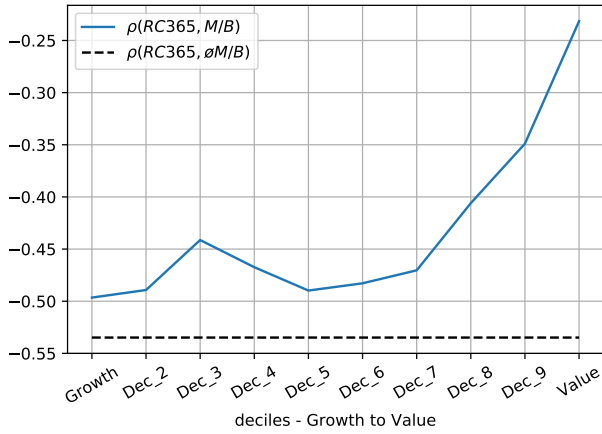
*B:  $\Delta\rho_{t,t+1}$  and  $IC_{365,t,t+1}$*



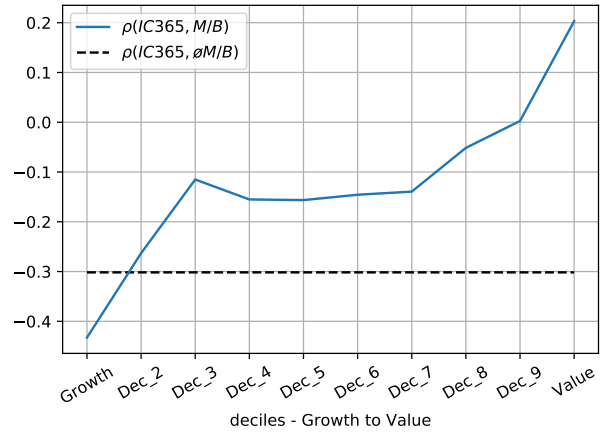
**Figure 5.** Contemporaneous: Implied Correlations and Book-to-Market Characteristics

The figure shows the time series correlation of realized correlation ( $RC$ ) and implied correlation ( $IC$ ) for a maturity of 365 calendar days and the value weighted market-to-book values of the ten book-to-market sorted portfolios. The market-to-book characteristics for year  $t$  are available at Kenneth French's website. Thereby the book value of year  $t$  is the book equity for the last fiscal year end in  $t - 1$  and the market value is price times shares outstanding at the end of December of  $t - 1$ . Since book-to-market is calculated in December of  $t - 1$ ,  $RC$  and  $IC$  are sampled at end of December in  $t - 1$  (Panel A and Panel B). The sample period for realized correlations is ranging from 01/1965 to 12/2017 and for implied correlations extracted for the S&P500 from 01/1996 to 12/2017. The sample period for the market-to-book characteristics ranges from 01/1965 to 12/2017 and is available on a yearly frequency. The dashed line displays the time series correlation w.r.t the average value weighted market-to-book characteristic across all deciles.

*A: Correlation -  $RC_{Dec,t-1}$*



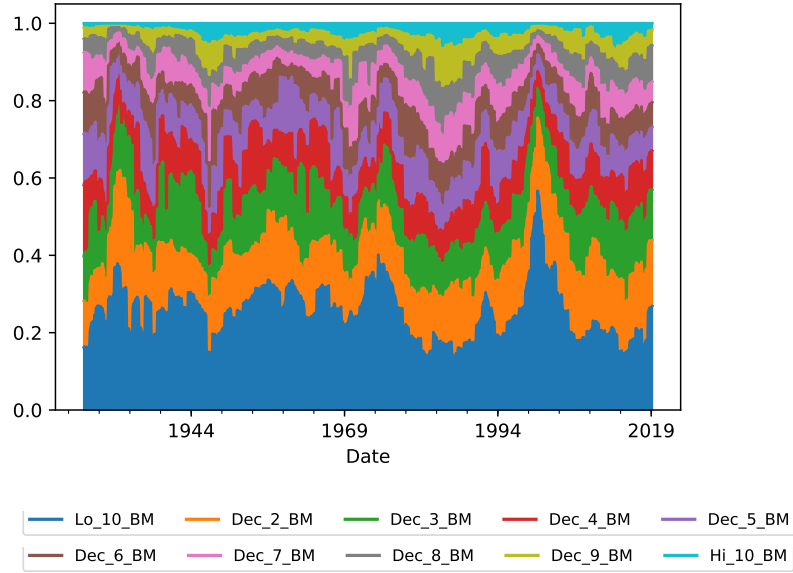
*B: Correlation -  $IC_{Dec,t-1}$*



**Figure 6.** Market Capitalization of Book-to-Market sorted decile Portfolios

The figure shows the relative market capitalization of the ten book-to-market sorted portfolios, calculated as number of firms multiplied by the average firm size, in the respective decile. The sample period ranges from 01/1926 to 12/2017 and is available on a monthly frequency. The factor data, is obtained from Kenneth French's Website.

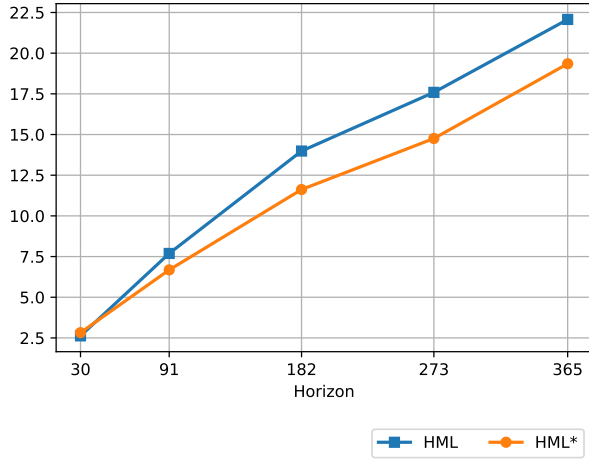
*A: Market Capitalization - Book-to-Market sorted Deciles*



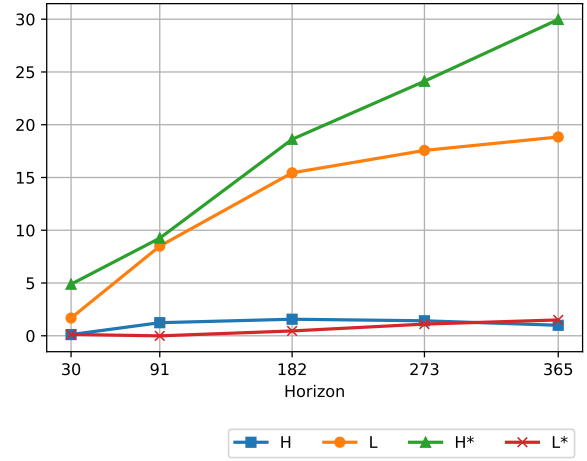
**Figure 7.** Predictive: Insample Factor Returns

The figure shows the  $R^2$ s of the regressions of the value factor returns ( $HML$ ,  $HML^*$ ) and the individual long- and short legs returns of the factors ( $H$ ,  $L$ ,  $H^*$ ,  $L^*$ ), realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations ( $IC$ ) for the S&P500 Index from matching-maturity options. The sample period is from 01/1996 to 12/2017, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website.

*A:  $R^2$  - Factors*



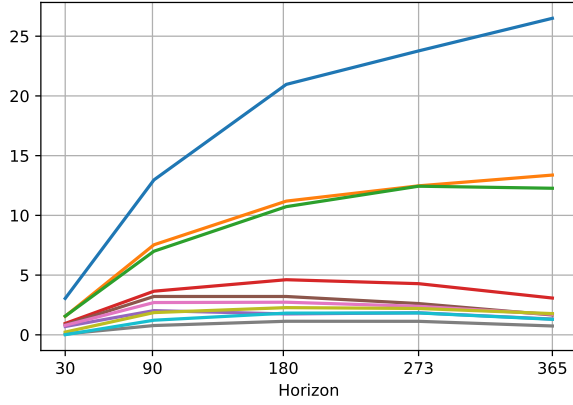
*B:  $R^2$  - Legs of the Factors*



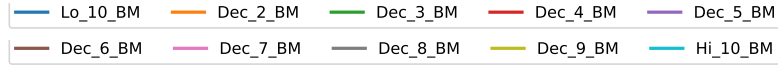
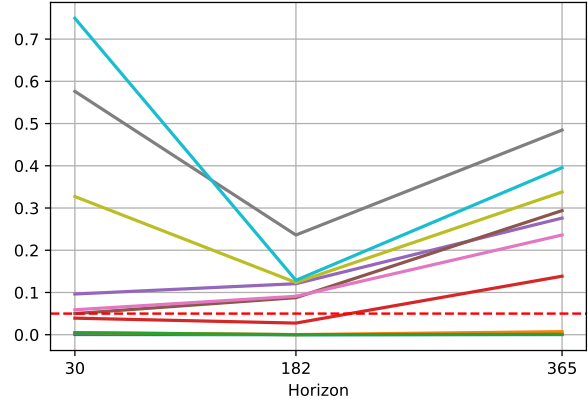
**Figure 8.** Predictive: Book-to-Market Sorted Decile Portfolios

The figure shows the  $R^2$ s (Panel A) and the p-values (Panel B) of the regressions of the Fama and French book-to-market sorted decile portfolios, realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations ( $IC$ ) for the S&P500 Index from matching-maturity options. The sample period is from 01/1996 to 12/2017, and the variables are sampled at monthly frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website.

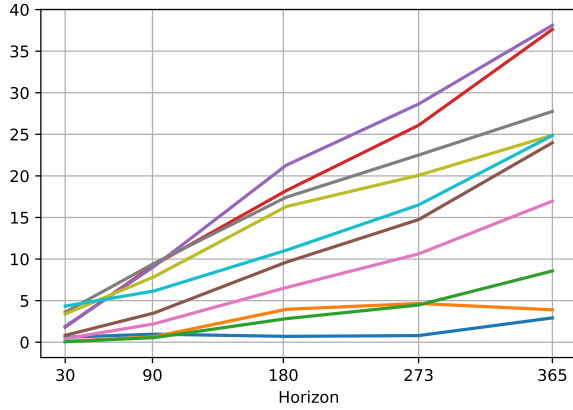
*A:  $R^2$  - Factors*



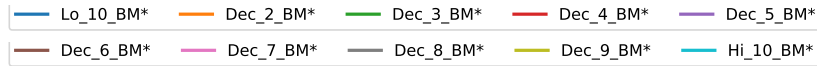
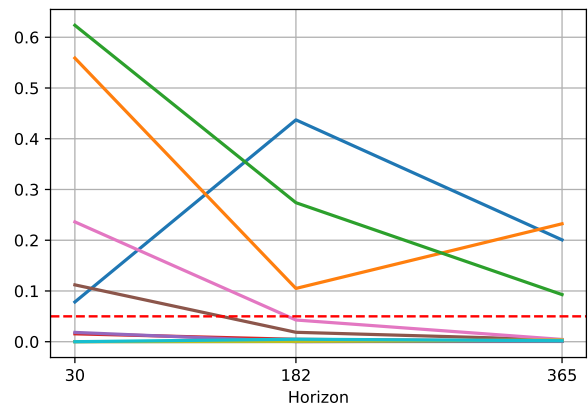
*B: p-values*



*C:  $R^2$  - Market Neutral Factors*



*D: p-values*

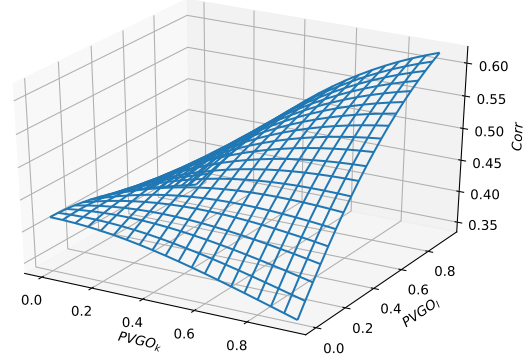
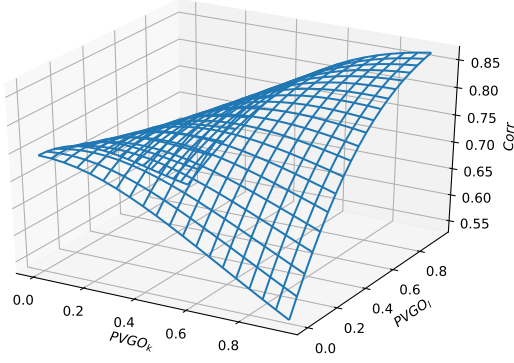


**Figure 9.** Model Correlation between two Stocks

The figure displays the correlation between two stocks as calculated in equation (20) for different idiosyncratic levels. Thereby  $\sigma_x = 0.17$ ,  $\alpha = 0.85$ ,  $\sigma_z = 0.035$ , and  $V_k = V_l = 1$  normalized to one. The function is evaluated for  $PVGO_k$  and  $PVGO_l$  between 0 and 1.

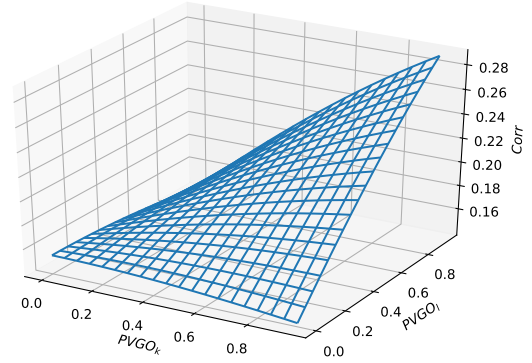
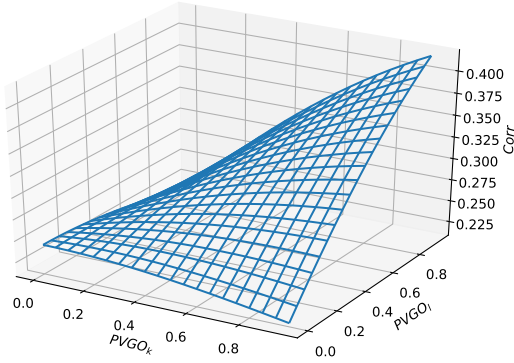
*A: Stock Correlation - Idiosyncratic = 0.1*

*B: Stock Correlation - Idiosyncratic = 0.2*



*C: Stock Correlation - Idiosyncratic = 0.3*

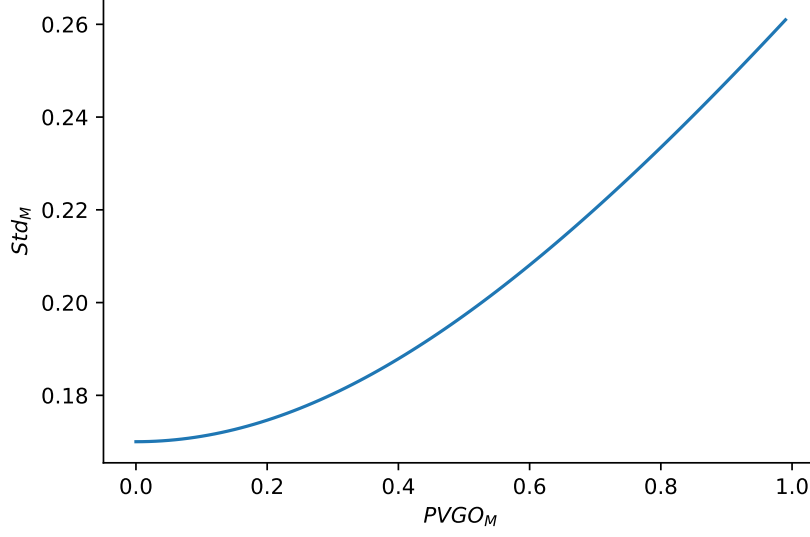
*D: Stock Correlation - Idiosyncratic = 0.4*



**Figure 10.** Market Volatility

The figure displays the market volatility as calculated in equation (23). Thereby  $\sigma_x = 0.17$ ,  $\alpha = 0.85$ ,  $\sigma_z = 0.035$ , and  $V_M = 1$  normalized to one. The function is evaluated for  $PVGO_M$  between 0 and 1.

*A: Market Volatility*

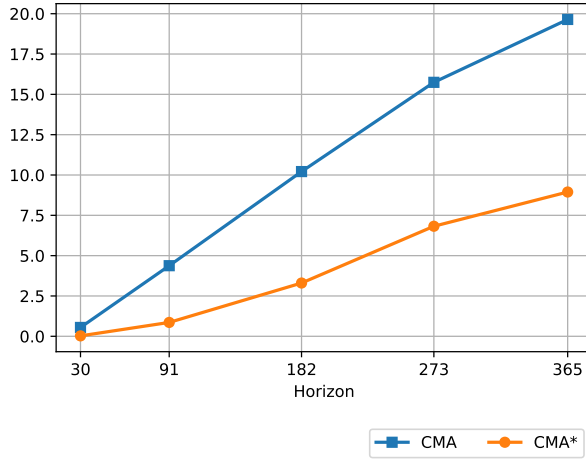




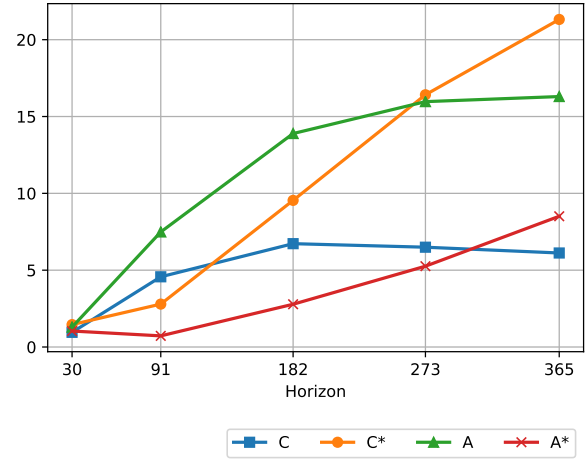
**Figure 11.** Predictive: Insample Factor Returns - CMA and RMW

The figure shows the  $R^2$ s of the regressions of the value factor returns ( $HML$ ,  $HML^*$ ) and the individual long- and short legs returns of the factors ( $H$ ,  $L$ ,  $H^*$ ,  $L^*$ ), realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations ( $IC$ ) for the S&P500 Index from matching-maturity options. The sample period is from 01/1996 to 12/2017, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website.

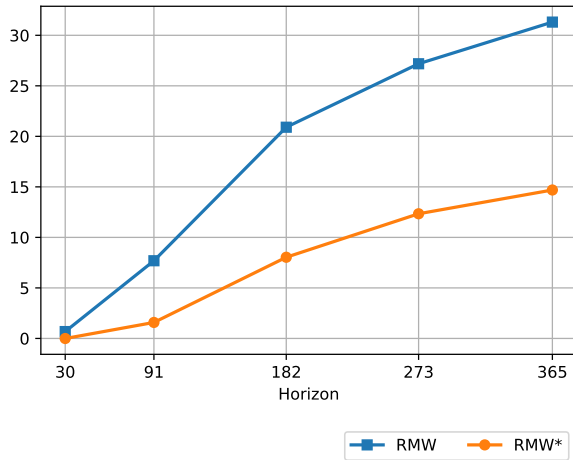
*A:  $R^2$  - Factors*



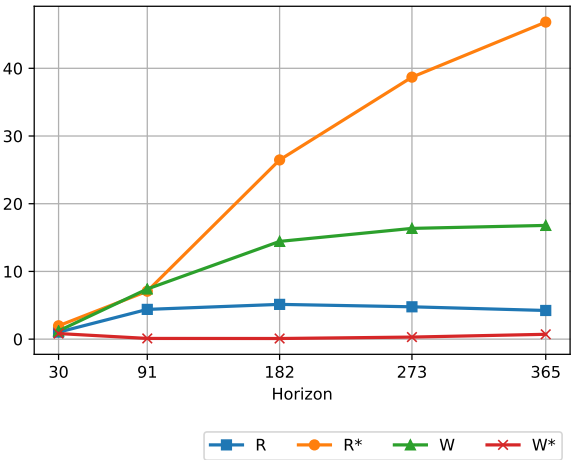
*B:  $R^2$  - Legs of the Factors*



*C:  $R^2$  - Factors*



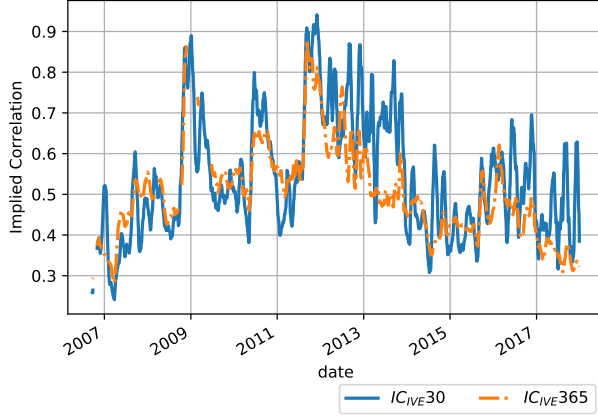
*D:  $R^2$  - Legs of the Factors*



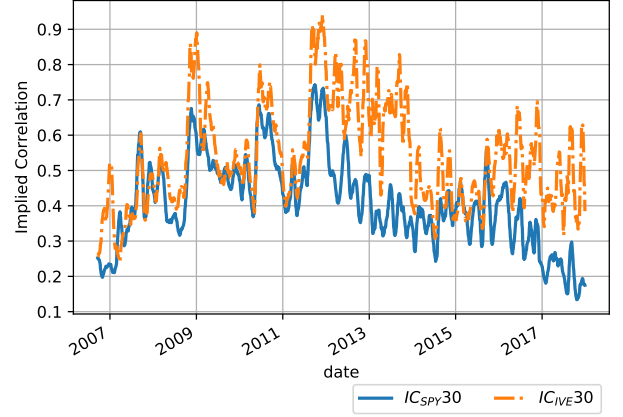
**Figure 12.** Implied Correlations - S&P500 and S&P500 Value Index

The figure shows the time series plots for implied correlations, which are calculated as equicorrelations applying Eq. (25) for the S&P500 Index ( $IC$ ) and for the S&P500 Value Index ( $IC_{IVE}$ ), for 30 and 365 calendar days. The sample period for the implied correlations extracted ranges from 08/2006 to 12/2017. Second moments are calculated for the index and for all index components as model-free implied variances following Martin (2013) and are sampled on a daily frequency.

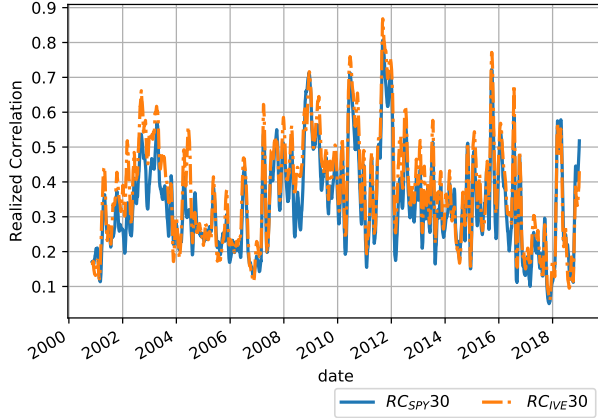
*A:  $IC_{IVE}$*



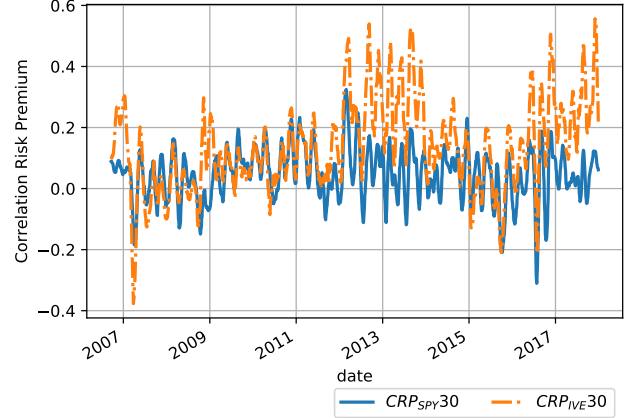
*B:  $IC$  vs.  $IC_{IVE}$*



*C:  $RC$  vs.  $RC_{IVE}$*

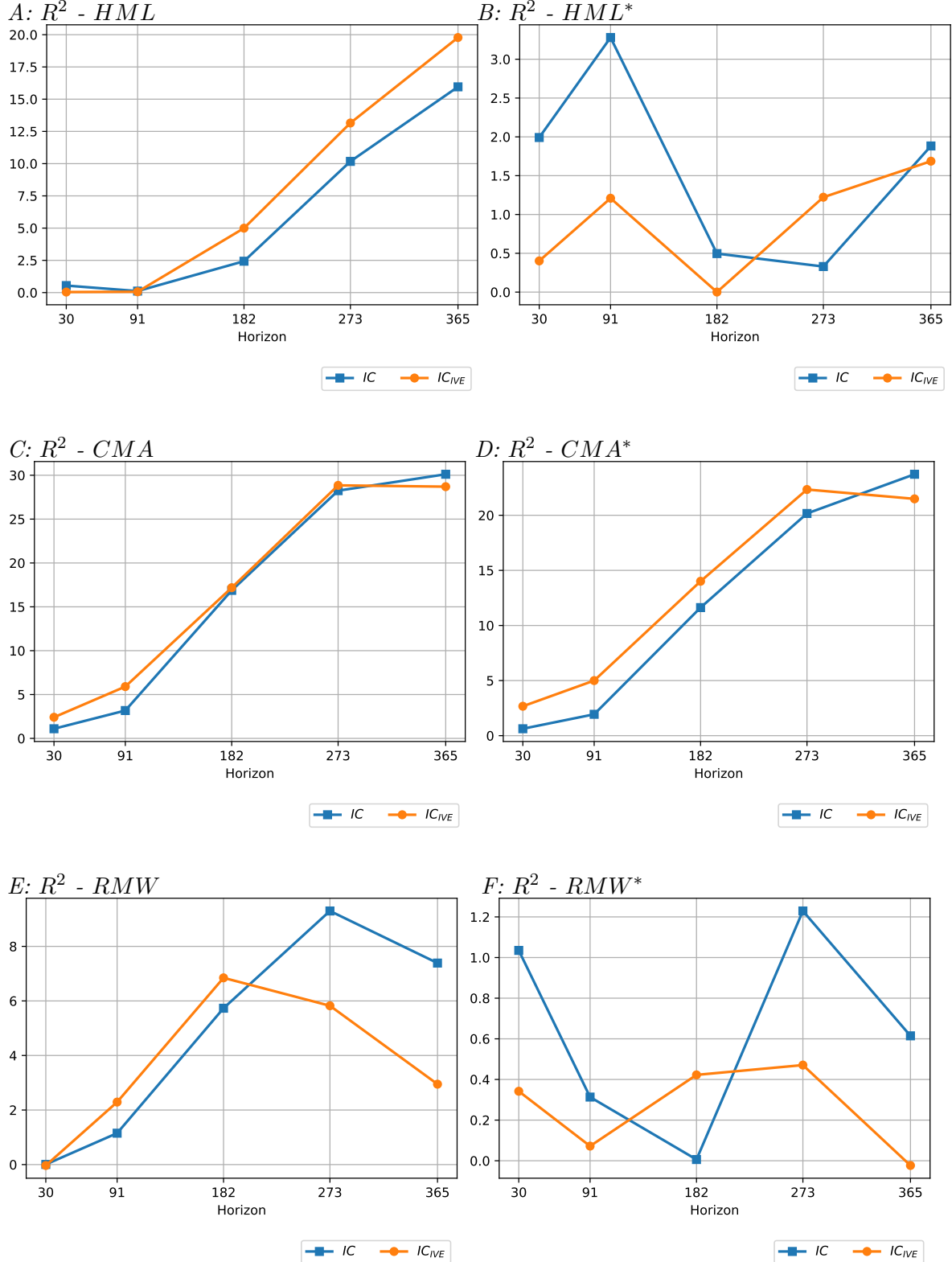


*D:  $CRP$  vs.  $CRP_{IVE}$*



**Figure 13.** Predictive: Insample Factor Returns -  $IC$  vs.  $IC_{IVE}$

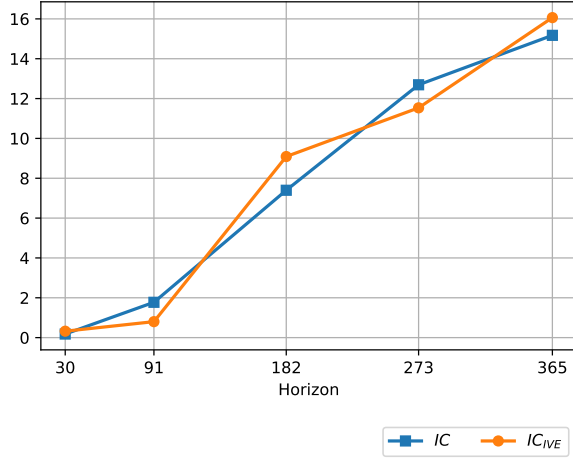
The figure shows the  $R^2$ s of the regressions of the value factor returns ( $HML$ ,  $HML^*$ ,  $CMA$ ,  $CMA^*$ ,  $RMW$ ,  $RMW^*$ ), realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations for the S&P500 Index ( $IC$ ), and on implied correlations for the S&P500 Value Index ( $IC_{IVE}$ ) from matching-maturity options. The sample period ranges from 08/2006 to 12/2017, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website.



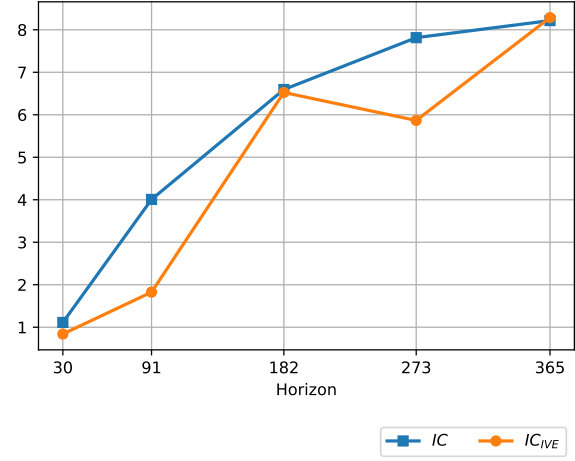
**Figure 14.** Predictive: Insample HML Returns -  $IC$  vs.  $IC_{IVE}$

The figure shows the  $R^2$ s of the regressions of the value factor returns ( $H, L, H^*, L^*$ ), realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations for the S&P500 Index ( $IC$ ), and on implied correlations for the S&P500 Value Index ( $IC_{IVE}$ ) from matching-maturity options. The sample period ranges from 08/2006 to 12/2017, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website.

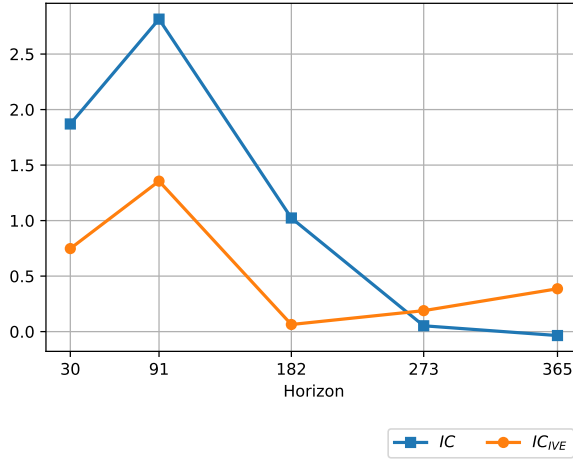
*A:  $R^2 - H$*



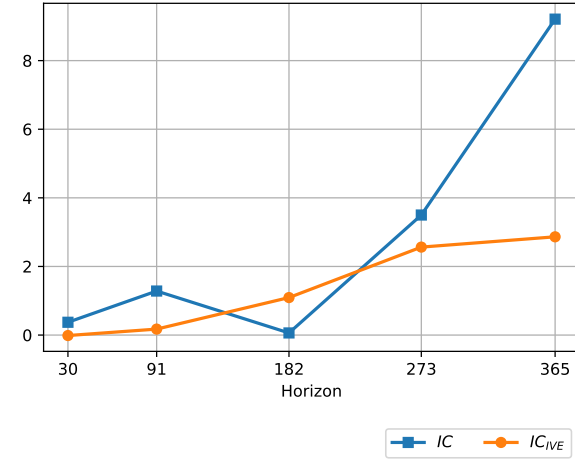
*B:  $R^2 - L$*



*C:  $R^2 - H^*$*



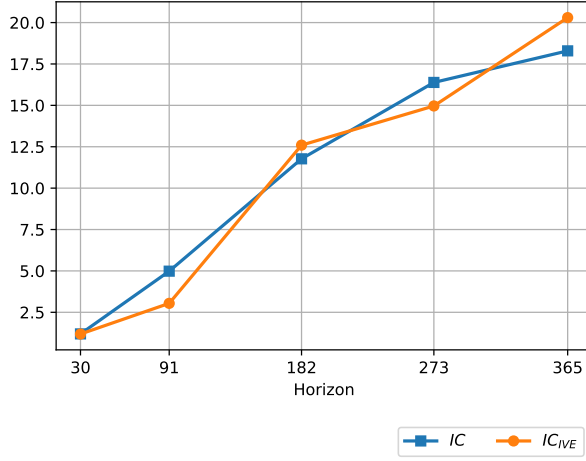
*D:  $R^2 - L^*$*



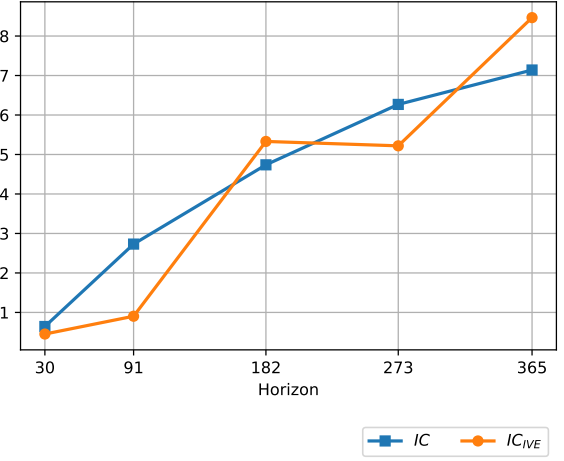
**Figure 15.** Predictive: Insample CMA Returns -  $IC$  vs.  $IC_{IVE}$

The figure shows the  $R^2$ s of the regressions of the value factor returns ( $C$ ,  $A$ ,  $C^*$ ,  $A^*$ ), realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations for the S&P500 Index ( $IC$ ), and on implied correlations for the S&P500 Value Index ( $IC_{IVE}$ ) from matching-maturity options. The sample period ranges from 08/2006 to 12/2017, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website.

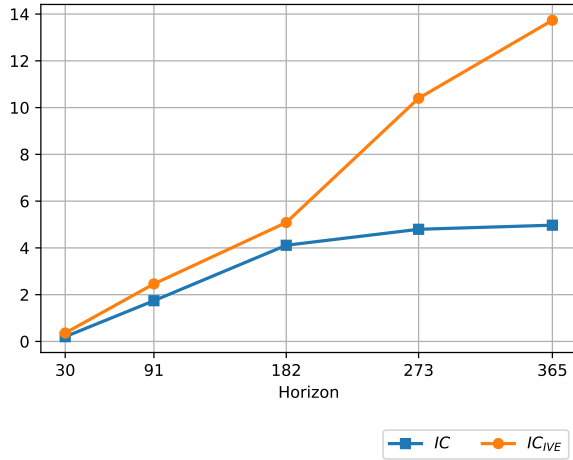
A:  $R^2 - C$



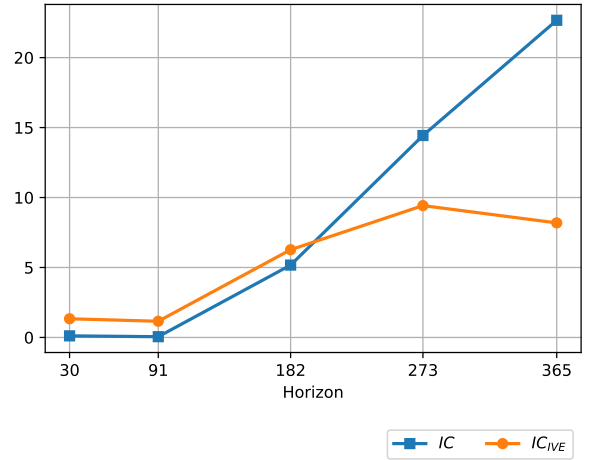
B:  $R^2 - A$



C:  $R^2 - C^*$



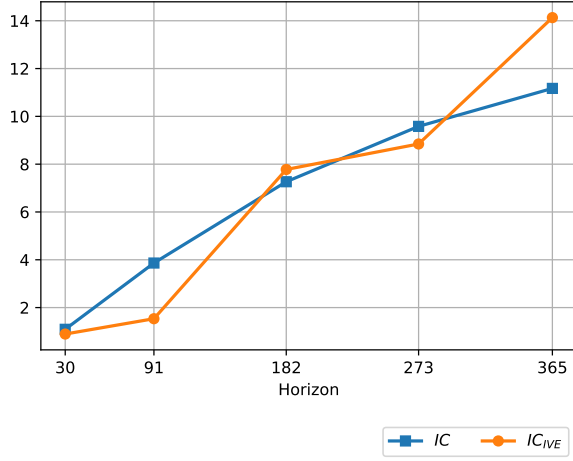
D:  $R^2 - A^*$



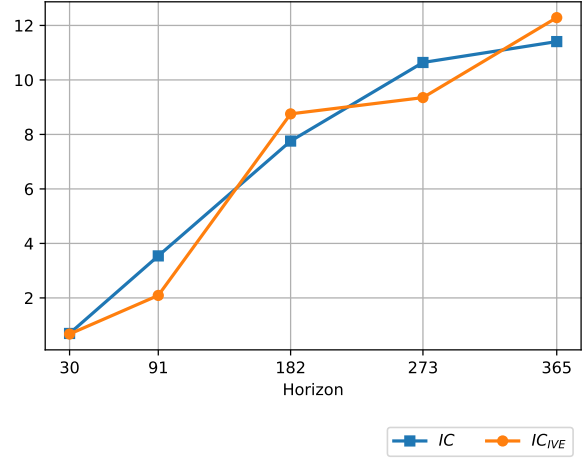
**Figure 16.** Predictive: Insample RMW Returns -  $IC$  vs.  $IC_{IVE}$

The figure shows the  $R^2$ s of the regressions of the value factor returns ( $R$ ,  $W$ ,  $R^*$ ,  $W^*$ ), realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations for the S&P500 Index ( $IC$ ), and on implied correlations for the S&P500 Value Index ( $IC_{IVE}$ ) from matching-maturity options. The sample period ranges from 08/2006 to 12/2017, and the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website.

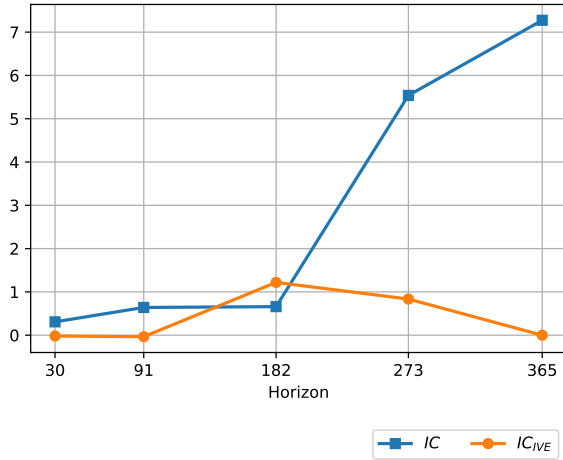
A:  $R^2 - R$



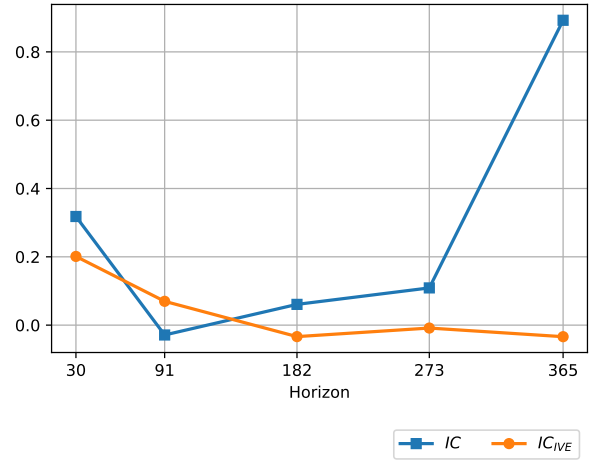
B:  $R^2 - W$



C:  $R^2 - R^*$



D:  $R^2 - W^*$



## I. Appendix

### A. A Brief Description of the Fama-French Factors

$MKTRF$  denotes the excess return on the market, value-weight return of all CRSP firms incorporated in the US and listed on the NYSE, AMEX, or NASDAQ that have a CRSP share code of 10 or 11 at the beginning of month  $t$ , good shares and price data at the beginning of  $t$ , and good return data for  $t$  minus the one-month Treasury bill rate (from Ibbotson Associates).

$HML$  (High Minus Low) is the average return on the two value portfolios minus the average return on the two growth portfolios. The portfolios are constructed at the end of June. The book-to-market ratio considers the book equity at the last fiscal year end of the prior calendar year divided by market equity at the end of December of the prior year.

$RMW$  (Robust Minus Weak) is the average return on the two robust operating profitability portfolios minus the average return on the two weak operating profitability portfolios. The sorting criteria is the operating profitability (OP), which is an accounting figure that measures the profit earned from a company's ongoing core business operations (excluding deductions of interest and taxes). In Fama and French OP is calculated as the annual revenues minus cost of goods sold, interest expense, and selling, general, and administrative expenses divided by book equity for the last fiscal year. Earnings per share can serve as an indicator of a company's profitability too.

$CMA$  (Conservative Minus Aggressive) is the average return on the two conservative investment portfolios minus the average return on the two aggressive investment portfolios. The sorting criteria is the investment.

### B. The connection between $HML$ , $RMW$ and $CMA$

The motivation follows closely Fama and French (2006) where the market value of a share of a firm's stock at time  $t$ ,  $M_t$ , is given by the present value of its expected dividends  $E[D_{t+\tau}]$ .

$$M_t = \sum_{\tau=1}^{\infty} \frac{E[D_{t+\tau}]}{(1+r)^\tau} \quad (\text{A1})$$

$r$  denotes the internal rate of return on the expected dividends, which proxies the return of the stock. Theoretically the dividend should be the difference of the equity earnings per share ( $Y_t$ ) and the reinvestment, i.e the change in book equity per share ( $dB_t = B_t - B_{t-1}$ ).

$$M_t = \sum_{\tau=1}^{\infty} \frac{E[Y_{t+\tau} - dB_{t+\tau}]}{(1+r)^\tau} \quad (\text{A2})$$

Dividing both sides by the time  $t$  book equity leads to

$$\frac{M_t}{B_t} = \sum_{\tau=1}^{\infty} \frac{E[Y_{t+\tau} - dB_{t+\tau}]}{B_t(1+r)^\tau} \quad (\text{A3})$$

Comparative statics of equation (A3) leads to the following implications, solving for  $r$ : i) A higher  $B/M$  ratio, and therefore a lower  $M/B$  ratio, needs to be offset with a higher value of  $r$ . ii) Keeping the left hand side fix, more profitable firms, i.e higher earnings  $Y$  relative to the book equity, indirectly increase the amplitude of  $r$ . iii) Taken  $B/M$  and  $Y$  as given, the stock return  $r$  is decreasing in the growth in equity due to reinvestment  $dB$ .

Overall the stylized model links the several components book-to-market, investment and operating profitability to each other and further motivates the *HML*, *RMW* and *CMA* investment factors.

### *C. Proxies for Growth Options*

In order to calculate the proxies for the growth options I follow Cao, Simin, and Zhao (2008). The ratio of the market value to book value of assets (*MABA*), an estimate of Tobin's  $Q$  ( $Q$ ), the debt to equity ratio (*DTE*), and the ratio of capital expenditures to fixed assets (*CAPEX*) and a direct measure of the present value of growth options (*PVGO*).



$$MABA = (ATQ - CEQQ + PRCCQ \times CSHOQ)/ATQ \quad (A4)$$

$$Q = (PRCCQ \times CSHOQ + PSTKQ + LCTQ - ACTQ + DLTTQ)/ATQ \quad (A5)$$

$$DTE = (DLCQ + DLTTQ + PSTKQ)/(PRCCQ \times CSHOQ) \quad (A6)$$

$$CAPEX = CAPXY/PPENTQ \quad (A7)$$

$$PVGO = ((PRCCQ \times CSHOQ) - VoAiP)/(PRCCQ \times CSHOQ) \quad (A8)$$

**Table XVII** Compustat Items - Calculation of Growth Option Proxies

Item #	Name	Description
5	<i>LCTQ</i>	Current Liabilities - Total
6	<i>ATQ</i>	Assets - Total
14	<i>PRCCQ</i>	Price
19	<i>DVPQ</i>	Dividends - Preferred
40	<i>ACTQ</i>	Current Assets - Total
42	<i>PPENTQ</i>	Property Plant and Equipment - Total (Net)
44	<i>ATQ</i>	Assets-Total
45	<i>DLCQ</i>	Debt in Current Liabilities
49	<i>LCTQ</i>	Current Liabilities - Total
51	<i>DLTTQ</i>	Long-Term Debt - Total
55	<i>PSTKQ</i>	Preferred/Preference Stock (Capital) - Total
59	<i>CEQQ</i>	Common/Ordinary Equity - Total
61	<i>CSHOQ</i>	Common Shares Outstanding
90	<i>CAPXY</i>	Capital Expenditures
308	<i>OANCFY</i>	Operating Cash Flow

To reduce outliers when calculating the debt to equity ratio I exclude stocks with market capitalization below 1 mio US\$ and financials (sic code between 6000 and 6999). I include only common stocks (CRSP share code in 10 or 11).

In order to calculate the value of assets in place (*VoAiP*), i.e the discounted future cash flow (DFC) I follow Cao, Simin, and Zhao (2008). I first estimate the ROE at a given point in time by the operating cash flow (item 308) divided by the beginning period book value of long-term liabilities not including debt (item 6 – item 5 – item 19). I then take an equally weighted average of the four previous ROE’s observations as the estimator for the ROE for year *t*. I obtain the projected earning by multiplying the average ROE by the end-of-period non debt long-term liability. The estimation of the value of asset-in-place, defined as the discounted projected-cash-flows happens by discounting the projected cash-flows with the average quarterly

$MKTRF$  rate estimated over the last five years.  $PVGO$  is obtained by the the total market value of equity minus the value of asset-in-place divided by the total market value of equity. As discussed by Cao, Simin, and Zhao (2008) and Long, Wald, and Jingfeng (2002) the estimation of  $PVGO$  is robust w.r.t different definitions of the  $ROE$  and the usage of the risk free rate.

#### D. NBER Recession Indicator - Contraction and Expansion

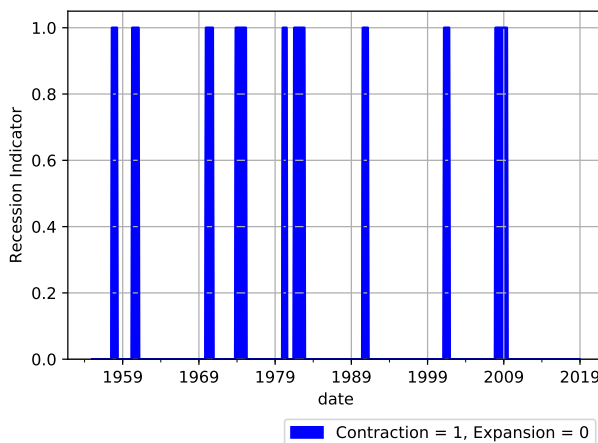
The time series is composed of dummy variables that represent periods recession (1) and expansion (0). The recession begins at the first day of the period following a peak and ends on the last day of the period of the trough. The NBER defines the contraction periods (peak to trough) as displayed in the table. The rest of the time is defined as expansion.

**Table XVIII** NBER - Contraction and Expansion Periods

Peak	Trough	Lenght
1957-08	1958-04	8
1960-04	1961-02	10
1969-12	1970-11	11
1973-11	1975-03	16
1980-01	1980-07	6
1981-07	1982-11	16
1990-07	1991-03	8
2001-03	2001-11	8
2007-12	2009-06	18

**Figure 17.** Recession Indicator – Contraction and Expansion

The figure shows the Contraction and Expansion periods as defined by NBER from the period of 1957 to 2018. Contraction periods are characterized by the bars equal to 1. By definition, not being in contraction means that the economy is situated in expansion.



## E. Appendix – Model

In this subsection some derivations and equations stated in the main text are derived and explained in more detail.

### E.1. Assets in Place

The time- $t$  market value of an existing project  $j$ ,  $p(\varepsilon_{ft}, u_{jt}, x_t, K_j)$  is equal to the present value of its cash flows

$$\begin{aligned} p(\varepsilon_{ft}, u_{jt}, x_t, K_j) &= \mathbb{E}_t \left[ \int_t^\infty e^{-\delta(s-t)} \frac{\pi_s}{\pi_t} y_{fjs} ds \right] \\ &= \mathbb{E}_t \left[ \int_t^\infty e^{-\delta(s-t)} \frac{\pi_s}{\pi_t} \varepsilon_{fs} u_{js} x_s K_j^\alpha ds \right] \\ &= A(\varepsilon_{ft}, u_{jt}) x_t K_j^\alpha, \end{aligned} \tag{A9}$$

where

$$\begin{aligned} A(\varepsilon, u) &= \frac{1}{r + \gamma_x \sigma_x + \delta - \mu_x} + \frac{1}{r + \gamma_x \sigma_x + \delta - \mu_x + \theta_\varepsilon} (\varepsilon - 1) + \frac{1}{r + \gamma_x \sigma_x + \delta - \mu_x + \theta_u} (u - 1) \\ &\quad + \frac{1}{r + \gamma_x \sigma_x + \delta - \mu_x + \theta_\varepsilon + \theta_u} (\varepsilon - 1)(u - 1). \end{aligned} \tag{A10}$$

### E.2. Optimal Investment

The optimal investment  $K_j$  of firm  $f$  in project  $j$  at time  $t$  is given by

$$K_f = (z_t \alpha A(\varepsilon_{ft}, 1))^{\frac{1}{1-\alpha}}. \tag{A11}$$

Proof:  $K_f$  is the solution to the problem

$$\max_{K_f} A(\varepsilon_{ft}, 1) x_t K_f^\alpha - z_t^{-1} x_t K_f \tag{A12}$$

The first order condition reads as

$$\begin{aligned} 0 &= \frac{\partial}{\partial K_f} [A(\varepsilon_{ft}, 1) x_t K_f^\alpha - z_t^{-1} x_t K_f] \\ &= \alpha A(\varepsilon_{ft}, 1) K_f^{\alpha-1} - z_t^{-1}, \end{aligned} \tag{A13}$$

and hence

$$\begin{aligned} K_f^{\alpha-1} &= z_t^{-1}(\alpha A(\epsilon_{f_t}, 1))^{-1} \\ \Rightarrow K_f &= (z_t \alpha A(\epsilon_{f_t}, 1))^{\frac{1}{1-\alpha}}. \end{aligned} \quad (\text{A14})$$

### E.3. The Value of Growth Opportunities

The NPV of future projects determines the value of growth opportunities. The value added net of investment costs, when a project is financed is

$$K_f A(\epsilon_{f_t}, 1) x_t - \frac{K_f x_t}{z_t} = [\alpha^{\frac{\alpha}{1-\alpha}} - \alpha^{\frac{1}{1-\alpha}}] z_t^{\frac{\alpha}{1-\alpha}} x_t A(\epsilon_{f_t}, 1)^{\frac{1}{1-\alpha}} = C z_t^{\frac{\alpha}{1-\alpha}} x_t A(\epsilon_{f_t}, 1)^{\frac{1}{1-\alpha}}. \quad (\text{A15})$$

The present value of growth options can then be written as

$$\begin{aligned} PVGO_{ft} &= \mathbb{E}_t^{\mathbb{Q}} \left[ \int_t^{\infty} e^{-r(s-t)} \lambda_{fs} C z_t^{\frac{\alpha}{1-\alpha}} x_t A(\epsilon_{f_t}, 1)^{\frac{1}{1-\alpha}} ds \right] \\ &= C z_t^{\frac{\alpha}{1-\alpha}} x_t \mathbb{E}_t \left[ \int_t^{\infty} e^{-\rho(s-t)} \lambda_{fs} A(\epsilon_{f_t}, 1)^{\frac{1}{1-\alpha}} ds \right] \\ &= C z_t^{\frac{\alpha}{1-\alpha}} x_t G(\epsilon_{f_t}, \lambda_{f_t}). \end{aligned} \quad (\text{A16})$$

where  $\mathbb{E}_t^{\mathbb{Q}}$  denotes the expectations under the risk-neutral measure  $\mathbb{Q}$ .

$$\begin{aligned} G_{ft} &:= G(\epsilon_{f_t}, \lambda_{f_t}) = C \cdot \mathbb{E}_t \left[ \int_t^{\infty} e^{-\rho(s-t)} \lambda_{fs} A(\epsilon_{f_t}, 1)^{\frac{1}{1-\alpha}} ds \right] \\ &= \begin{cases} \lambda_f(G_1(\epsilon_{f_t}) + \frac{\mu_L}{\mu_L + \mu_H}(\lambda_H - \lambda_L)G_2(\epsilon_{f_t})) & \bar{\lambda}_{ft} = \lambda_H \\ \lambda_f(G_1(\epsilon_{f_t}) - \frac{\mu_H}{\mu_L + \mu_H}(\lambda_H - \lambda_L)G_2(\epsilon_{f_t})) & \bar{\lambda}_{ft} = \lambda_L \end{cases} \end{aligned} \quad (\text{A17})$$

with

$$\rho = r + \gamma_x \sigma_x - \mu_x - \frac{\alpha}{1-\alpha}(\mu_z - \gamma_z \sigma_z + \frac{1}{2}\sigma_z^2) - \frac{\alpha^2 \sigma_z^2}{2(1-\alpha)^2}, \quad (\text{A18})$$

and

$$C = \alpha^{\frac{1}{1-\alpha}}(\alpha^{-1} - 1). \quad (\text{A19})$$

The functions  $G_1(\epsilon)$  and  $G_2(\epsilon)$  solve the following ODE

$$a(\epsilon)z' - b(\epsilon)z - \rho y + c(\epsilon) = 0, \quad (\text{A20})$$

where  $a(\varepsilon) = \frac{1}{2}\sigma_\varepsilon^2\varepsilon$ ,  $b(\varepsilon) = \theta_\varepsilon(\varepsilon - 1)$ ,  $c(\varepsilon) = CA(\varepsilon, 1)^{\frac{1}{1-\alpha}}$ ,  $y = G$ , and  $z = G'$ .

For further details see Kogan and Papanikolaou (2014)

#### E.4. Value and Growth Dynamics

For notational convenience define  $\sum_f A_{ft} := \sum_{j \in J_t^f} A(\varepsilon_{ft}, u_{jt})K_j^\alpha$  and  $G_{ft} := G(\varepsilon_{ft}, \lambda_{ft})$ .

The dynamics of value of assets in place can be written as:

$$\begin{aligned} dVAP_{ft} &= dx_t \sum_f A_{ft} + x_t d \sum_f A_{ft} + dx_t d \sum_f A_{ft} \\ &= dx_t \sum_f A_{ft} + x_t d \sum_f A_{ft}, \end{aligned} \quad (\text{A21})$$

and therefore

$$\begin{aligned} \frac{dVAP_{ft}}{VAP_{ft}} &= \frac{dx_t}{x_t} \frac{\sum_f A_{ft}}{\sum_f A_{ft}} + \frac{x_t}{x_t} \frac{d \sum_f A_{ft}}{\sum_f A_{ft}} \\ &= \frac{dx_t}{x_t} + \frac{d \sum_f A_{ft}}{\sum_f A_{ft}}. \end{aligned} \quad (\text{A22})$$

The dynamics of the present value of growth options can be written as:

$$\begin{aligned} dPVGO_{ft} &= d(z_t^{\frac{\alpha}{1-\alpha}} x_t G_{ft}) \\ &= d(z_t^{\frac{\alpha}{1-\alpha}} x_t) G_{ft} + z_t^{\frac{\alpha}{1-\alpha}} x_t dG_{ft} + d(z_t^{\frac{\alpha}{1-\alpha}} x_t) dG_{ft}. \end{aligned} \quad (\text{A23})$$

First calculate

$$\begin{aligned} d(z_t^{\frac{\alpha}{1-\alpha}} x_t) &= z_t^{\frac{\alpha}{1-\alpha}} dx_t + x_t d(z_t^{\frac{\alpha}{1-\alpha}}) + d[x_t, z_t^{\frac{\alpha}{1-\alpha}}] \\ &= z_t^{\frac{\alpha}{1-\alpha}} dx_t + x_t d(z_t^{\frac{\alpha}{1-\alpha}}) \\ &= z_t^{\frac{\alpha}{1-\alpha}} dx_t + x_t \frac{\alpha}{1-\alpha} z_t^{\frac{\alpha}{1-\alpha}-1} dz_t + x_t \frac{1}{2} \frac{\partial^2 z_t^{\frac{\alpha}{1-\alpha}}}{\partial z^2} \sigma_z^2 z_t^2 dt \\ &= z_t^{\frac{\alpha}{1-\alpha}} dx_t + x_t \frac{\alpha}{1-\alpha} z_t^{\frac{\alpha}{1-\alpha}-1} dz_t + x_t R(z_t) dt, \end{aligned} \quad (\text{A24})$$

and therefore

$$dPVGO_{ft} = (z_t^{\frac{\alpha}{1-\alpha}} dx_t + x_t \frac{\alpha}{1-\alpha} z_t^{\frac{\alpha}{1-\alpha}-1} dz_t + x_t R(z_t) dt) G_{ft} + z_t^{\frac{\alpha}{1-\alpha}} x_t dG_{ft}. \quad (\text{A25})$$

In relative terms one obtains

$$\begin{aligned}
\frac{dPVGO_{ft}}{PVGO_{ft}} &= \frac{z_t^{\frac{\alpha}{1-\alpha}} dx_t}{z_t^{\frac{\alpha}{1-\alpha}} x_t} + \frac{x_t \frac{\alpha}{1-\alpha} z_t^{\frac{\alpha}{1-\alpha}-1} dz_t}{z_t^{\frac{\alpha}{1-\alpha}} x_t} + \frac{R(z_t)dt}{z_t^{\frac{\alpha}{1-\alpha}}} + \frac{z_t^{\frac{\alpha}{1-\alpha}} x_t dG_{ft}}{z_t^{\frac{\alpha}{1-\alpha}} x_t G_{ft}} \\
&= \frac{dx_t}{x_t} + \frac{\alpha}{1-\alpha} \frac{dz_t}{z_t} + \frac{R(z_t)dt}{z_t^{\frac{\alpha}{1-\alpha}}} + \frac{dG_{ft}}{G_{ft}}.
\end{aligned} \tag{A26}$$

### E.5. Expected Returns Dynamics

The risk premium on assets in place (growth opportunities) can be calculated by the covariance with the pricing kernel

$$\frac{d\pi}{\pi} = -r dt - \gamma_x dB_{xt} - \gamma_z dB_{zt}. \tag{A27}$$

Therefore

$$\begin{aligned}
E_t[R_{ft}^{VAP}] - r_f &= -cov\left(\frac{dVAP_{ft}}{VAP_{ft}}, \frac{d\pi_t}{\pi_t}\right) \\
&= -cov\left(\frac{dx_t}{x_t}, \frac{d\pi_t}{\pi_t}\right) \\
&= \sigma_x \gamma_x dt,
\end{aligned} \tag{A28}$$

and

$$\begin{aligned}
E_t[R_{ft}^{GO}] - r_f &= -cov\left(\frac{dPVGO_{ft}}{PVGO_{ft}}, \frac{d\pi_t}{\pi_t}\right) \\
&= -cov\left(\frac{dx_t}{x_t} + \frac{\alpha}{1-\alpha} \frac{dz_t}{z_t}, \frac{d\pi_t}{\pi_t}\right) \\
&= \sigma_x \gamma_x dt + \frac{\alpha}{1-\alpha} \sigma_z \gamma_z dt.
\end{aligned} \tag{A29}$$

And hence

$$\begin{aligned}
E_t[R_{ft}] - r_f &= \frac{VAP_{ft}}{V_t}(E_t[R_{ft}^{VAP}] - r_f) + \frac{PVGO_{ft}}{V_t}(E_t[R_{ft}^{GO}] - r_f) \\
&= \frac{VAP_{ft}}{V_t}(\sigma_x \gamma_x) + \frac{PVGO_{ft}}{V_t}(\sigma_x \gamma_x + \frac{\alpha}{1-\alpha} \sigma_z \gamma_z) \\
&= (\frac{VAP_{ft}}{V_t} + \frac{PVGO_{ft}}{V_t})\sigma_x \gamma_x + \frac{PVGO_{ft}}{V_t} \frac{\alpha}{1-\alpha} \sigma_z \gamma_z \\
&= \sigma_x \gamma_x + \frac{\alpha}{1-\alpha} \sigma_z \gamma_z \frac{PVGO_{ft}}{V_t}.
\end{aligned} \tag{A30}$$

## E.6. Return Dynamics

The dynamics for the changes in firm value can be calculated as follows

$$\begin{aligned}
dV_{ft} &= dVAP_{ft} + dPVGO_{ft} \\
&= \sum_f A_{ft} dx_t + x_t d \sum_f A_{ft} + (z_t^{\frac{\alpha}{1-\alpha}} dx_t + x_t \frac{\alpha}{1-\alpha} z_t^{\frac{\alpha}{1-\alpha}-1} dz_t + R(z_t) dt) G_{ft} + z_t^{\frac{\alpha}{1-\alpha}} x_t dG_{ft} \\
&= R(z_t) G_{ft} dt + (\sum_k A_{ft} + z_t^{\frac{\alpha}{1-\alpha}} G_{ft}) dx_t + x_t \frac{\alpha}{1-\alpha} z_t^{\frac{\alpha}{1-\alpha}-1} G_{ft} dz_t + x_t d \sum_f A_{ft} + z_t^{\frac{\alpha}{1-\alpha}} x_t dG_{ft} \\
&= \bar{R}(z_t) dt + (\sum_k A_{ft} + z_t^{\frac{\alpha}{1-\alpha}} G_{ft}) \sigma_x x_t dB_{xt} + x_t \frac{\alpha}{1-\alpha} z_t^{\frac{\alpha}{1-\alpha}-1} G_{ft} \sigma_z z_t dB_{zt} + dIdio_f \\
&= \bar{R}(z_t) dt + \sigma_x dB_{xt} (x_t \sum_k A_{ft} + x_t z_t^{\frac{\alpha}{1-\alpha}} G_{ft}) + x_t z_t^{\frac{\alpha}{1-\alpha}} G_{ft} \frac{\alpha}{1-\alpha} \sigma_z dB_{zt} + dIdio_f \\
&= \bar{R}(z_t) dt + \sigma_x dB_{xt} V_{ft} + \frac{\alpha}{1-\alpha} PVGO_{ft} \sigma_z dB_{zt} + dIdio_f,
\end{aligned} \tag{A31}$$

where  $dIdio_f$  denotes the dynamics associated to  $A_{ft}$  (as a function of  $\varepsilon_{ft}, u_{jt}, K_j^\alpha$ ) and  $G_{ft}$ .

$$dIdio_f = x_t d \sum_f A_{ft} + z_t^{\frac{\alpha}{1-\alpha}} x_t dG_{ft}. \tag{A32}$$

The return dynamic of the firm can be written as

$$dR_{ft} = \frac{dV_{ft}}{V_{ft}} = E[R_{ft}] dt + \sigma_x dB_{xt} + \frac{\alpha}{1-\alpha} \frac{PVGO_{ft}}{V_{ft}} \sigma_z dB_{zt} + \frac{dIdio_f}{V_{ft}}. \tag{A33}$$

Since idiosyncratic terms are uncorrelated one can calculate the covariance between two returns as follows

$$\begin{aligned}
dR_{kt}dR_{lt} &= (E[R_{kt}]dt + \sigma_x dB_{xt} + \frac{\alpha}{1-\alpha}\sigma_z \frac{PVGO_{kt}}{V_{kt}}dB_{zt} + dIdio_k) \\
&\quad \times (E[R_{lt}]dt + \sigma_x dB_{xt} + \frac{\alpha}{1-\alpha}\sigma_z \frac{PVGO_{lt}}{V_{lt}}dB_{zt} + dIdio_l) \\
&= (\sigma_x dB_{xt} + \frac{\alpha}{1-\alpha}\sigma_z \frac{PVGO_{kt}}{V_{kt}}dB_{zt})(\sigma_x dB_{xt} + \frac{\alpha}{1-\alpha}\sigma_z \frac{PVGO_{lt}}{V_{lt}}dB_{zt}) \\
&= \sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 \frac{PVGO_{kt}}{V_{kt}} \frac{PVGO_{lt}}{V_{lt}} dt.
\end{aligned} \tag{A34}$$

The variance of the return process is given by

$$\begin{aligned}
\sigma^2(dR_{ft}) &= dR_{ft}dR_{ft} = (E[R_f]dt + \sigma_x dB_{xt} + \frac{\alpha}{1-\alpha}\sigma_z \frac{PVGO_{ft}}{V_{ft}}dB_{zt} + dIdio_f) \\
&\quad \times (E[R_f]dt + \sigma_x dB_{xt} + \frac{\alpha}{1-\alpha}\sigma_z \frac{PVGO_{ft}}{V_{ft}}dB_{zt} + dIdio_f) \\
&= \sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 (\frac{PVGO_{ft}}{V_{ft}})^2 dt + dIdio_f^2.
\end{aligned} \tag{A35}$$

Therefore the correlation can be calculates as

$$\frac{dR_{kt}dR_{lt}}{\sqrt{\sigma^2(dR_{kt})}\sqrt{\sigma^2(dR_{lt})}} = \frac{\sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 \frac{PVGO_{kt}}{V_{kt}} \frac{PVGO_{lt}}{V_{lt}} dt}{\sqrt{\sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 (\frac{PVGO_{kt}}{V_{kt}})^2 dt + dIdio_k^2} \sqrt{\sigma_x^2 dt + (\frac{\alpha}{1-\alpha})^2 \sigma_z^2 (\frac{PVGO_{lt}}{V_{lt}})^2 dt + dIdio_l^2}}. \tag{A36}$$

## F. Market Return Dynamics

To aggregate the individual components into the market index, it is assumed that constituents are market cap weighted, hence  $V_{it}/\sum V_{it} := V_{it}/V_{Mt}$ . The market return can be



written as

$$\begin{aligned}
\sum_f \frac{1}{dt} \frac{V_{ft}}{V_{Mt}} E[R_{ft}] - r_f &= \sum_f \frac{V_{ft}}{V_{Mt}} \gamma_x \sigma_x + \frac{\alpha}{1-\alpha} \gamma_z \sigma_z \sum_l \frac{V_{ft}}{V_{Mt}} \frac{PVGO_{ft}}{V_{ft}} \\
&= \gamma_x \sigma_x + \frac{\alpha}{1-\alpha} \gamma_z \sigma_z \sum_f \frac{PVGO_{ft}}{V_{Mt}} \\
&= \gamma_x \sigma_x + \frac{\alpha}{1-\alpha} \gamma_z \sigma_z \frac{PVGO_{Mt}}{V_{Mt}}, \tag{A37}
\end{aligned}$$

where  $PVGO_M := \sum_f PVGO_f$ .

The market return variance can be written as

$$\begin{aligned}
\sum_k \sum_l w_k w_l dR_{kt} dR_{lt} &= \sum_k \sum_l \frac{V_{kt}}{V_{Mt}} \frac{V_{lt}}{V_{Mt}} \sigma_x^2 dt + \left(\frac{\alpha}{1-\alpha}\right)^2 \sigma_z^2 \sum_k \sum_l \frac{V_{kt}}{V_{Mt}} \frac{V_{lt}}{V_{Mt}} \frac{PVGO_{kt}}{V_{kt}} \frac{PVGO_{lt}}{V_{lt}} dt \\
&= \sum_k \sum_l \frac{V_{kt}}{V_{Mt}} \frac{V_{lt}}{V_{Mt}} \sigma_x^2 dt + \left(\frac{\alpha}{1-\alpha}\right)^2 \sigma_z^2 \sum_k \sum_l \frac{PVGO_{kt}}{V_{Mt}} \frac{PVGO_{lt}}{V_{Mt}} dt \\
&= \sigma_x^2 dt + \left(\frac{\alpha}{1-\alpha}\right)^2 \sigma_z^2 \left(\frac{PVGO_{Mt}}{V_{Mt}}\right)^2 dt, \tag{A38}
\end{aligned}$$

where the last step follows with  $\sum_k \sum_l \frac{V_{kt}}{V_{Mt}} \frac{V_{lt}}{V_{Mt}} = 1$  and

$$PVGO_M^2 := \left(\sum_k PVGO_k\right)^2 = \sum_k \sum_l PVGO_k PVGO_l.$$

## AI1. Robustness

**Table AI101** Growth Option Predictability – Changes – RC – Full Sample

This table shows the slope and the  $R^2$ s of the univariate regressions of (log) changes of common proxies for the value of growth options over a future horizon of 30, 91, 182, 273, and 365 calendar days on realized correlations ( $RC$ ) calculated from daily realized returns over the respective window. The sample period for realized correlations is ranging from 01/1965 to 12/2017. The proxies for growth options includes the ratio of the market value to book value of assets ( $MABA$ ), an estimate of Tobin's Q ( $Q$ ), the debt to equity ratio ( $DTE$ ), the ratio of capital expenditures to fixed assets ( $CAPEX$ ), and a direct measure of the present value of growth options ( $PVGO$ ). The sample period for the growth option proxies ranges from 1983 to 2018. The data for the calculation of the proxies is obtained from Compustat and available on a monthly frequency. For further details see Appendix I.C. The  $p$  – values are computed with Newey and West (1987) standard errors.

30 days			91 days			182 days			273 days			365 days			
$\beta$	$p - val$	$R^2$	$\beta$	$p - val$	$R^2$	$\beta$	$p - val$	$R^2$	$\beta$	$p - val$	$R^2$	$\beta$	$p - val$	$R^2$	
<i>MABA</i>															
<i>RC</i>	-0.060	0.392	-0.129	0.178	0.008	2.382	0.132	0.267	0.482	0.200	0.250	0.907	0.294	0.217	1.492
<i>Q</i>															
<i>RC</i>	-0.073	0.364	-0.111	0.213	0.006	2.312	0.180	0.189	0.703	0.236	0.241	0.893	0.346	0.210	1.484
<i>DTE</i>															
<i>RC</i>	0.114	0.401	-0.119	-0.101	0.067	0.680	-0.041	0.729	-0.151	-0.008	0.960	-0.239	-0.130	0.438	0.330
<i>CAPEX</i>															
<i>RC</i>	0.019	0.855	-0.233	-0.024	0.890	-0.234	-0.268	0.111	0.250	-0.101	0.477	-0.167	-0.061	0.684	-0.096
<i>PVGO</i>															
<i>RC</i>	-0.003	0.453	-0.189	0.005	0.162	1.063	0.007	0.212	1.057	0.008	0.347	0.796	0.013	0.173	2.109

**Table AI102** Growth Option Predictability – RC – Contraction and Expansion

This table shows the slope and the  $R^2$ s of the univariate regressions of (log) changes of common proxies for the value of growth options over a future horizon of 30, 91, 182, 273, and 365 calendar days on realized correlations ( $RC$ ) calculated from daily realized returns over the respective window. The sample period for realized correlations is ranging from 01/1965 to 12/2017. The proxies for growth options includes the ratio of the market value to book value of assets ( $MABA$ ), an estimate of Tobin's Q ( $Q$ ), the debt to equity ratio ( $DTE$ ), the ratio of capital expenditures to fixed assets ( $CAPEX$ ), and a direct measure of the present value of growth options ( $PVGO$ ). The data for the calculation of the proxies is obtained from Compustat and available on a monthly frequency. For further details see I.C. The sample period for the growth option proxies ranges from 1983 to 2018. The sample is divided into contraction and expansion according to the manifestation of the NBER Recession Indicator, see Appendix I.D. The  $p$  – values are computed with Newey and West (1987) standard errors.

*Panel A: Contraction*

30 days				91 days			182 days			273 days			365 days						
$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$					
<i>MABA</i>																			
RC	-0.388	0.102	0.825		0.109	0.552	-1.913		0.392	0.018	3.111		0.273	0.369	-0.492		0.520	0.023	3.829
<i>Q</i>																			
RC	-0.473	0.081	1.559		0.134	0.587	-2.048		0.503	0.021	2.755		0.352	0.373	-0.607		0.644	0.031	3.276
<i>DTE</i>																			
RC	-0.008	0.989	-2.857		-0.207	0.461	-1.147		-0.684	0.009	6.393		-0.716	0.115	5.125		-1.016	0.012	11.622
<i>CAPEX</i>																			
RC	-0.142	0.665	-2.663		-0.587	0.309	-0.205		-0.452	0.350	-1.548		-0.065	0.884	-2.828		0.133	0.720	-1.832
<i>PVGO</i>																			
RC	-0.017	0.384	-1.566		0.004	0.825	-2.577		0.041	0.052	7.591		0.042	0.187	5.375		0.064	0.029	13.381

*Panel B: Expansion*

30 days				91 days			182 days			273 days			365 days						
$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$		$\beta$	$p - val$	$R^2$					
<i>MABA</i>																			
RC	-0.032	0.664	-0.229		0.203	0.004	2.974		0.137	0.275	0.471		0.242	0.198	1.299		0.323	0.201	1.719
<i>Q</i>																			
RC	-0.039	0.653	-0.226		0.243	0.002	2.964		0.188	0.192	0.729		0.285	0.182	1.325		0.381	0.188	1.745
<i>DTE</i>																			
RC	0.129	0.370	-0.107		-0.105	0.050	0.781		0.016	0.883	-0.248		0.056	0.684	-0.114		-0.052	0.729	-0.167
<i>CAPEX</i>																			
RC	0.036	0.755	-0.245		0.049	0.781	-0.241		-0.208	0.250	0.016		-0.028	0.839	-0.260		0.026	0.823	-0.242
<i>PVGO</i>																			
RC	-0.002	0.702	-0.286		0.006	0.006	2.851		0.006	0.165	1.147		0.008	0.180	1.393		0.012	0.109	2.466

**Table AI103** Growth Option Predictability – IC – Contraction and Expansion

This table shows the slope and the  $R^2$ s of the univariate regressions of (log) changes of common proxies for the value of growth options over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations ( $IC$ ) from matching-maturity options and realized correlations ( $RC$ ) calculated from daily realized returns over the respective window. The sample period for realized correlations is ranging from 01/1965 to 12/2017, and for implied correlations extracted for the S&P500 from 01/1996 to 12/2017. The proxies for growth options includes the ratio of the market value to book value of assets ( $MABA$ ), an estimate of Tobin's  $Q$  ( $Q$ ), the debt to equity ratio ( $DTE$ ), the ratio of capital expenditures to fixed assets ( $CAPEX$ ), and a direct measure of the present value of growth options ( $PVGO$ ). The data for the calculation of the proxies is obtained from Compustat and available on a monthly frequency. For further details see I.C. The sample period for the growth option proxies ranges from 1983 to 2018. The sample is divided into contraction and expansion according to the manifestation of the NBER Recession Indicator, see Appendix I.D. The  $p$  – values are computed with Newey and West (1987) standard errors.

*Panel A: Contraction*

30 days				91 days			182 days			273 days			365 days		
$\beta$	$p-val$	$R^2$		$\beta$	$p-val$	$R^2$		$\beta$	$p-val$	$R^2$		$\beta$	$p-val$	$R^2$	
<i>MABA</i>															
IC	0.141	0.689	-3.500	0.439	0.044	8.775	0.703	0.086	12.220	0.608	0.278	8.085	0.946	0.057	25.623
<i>Q</i>															
IC	0.203	0.588	-3.289	0.547	0.055	7.827	0.912	0.091	11.848	0.792	0.283	7.758	1.182	0.075	23.832
<i>DTE</i>															
IC	0.147	0.850	-3.756	-0.634	0.054	11.590	-1.218	0.039	20.981	-1.152	0.189	14.105	-1.499	0.088	25.457
<i>CAPEX</i>															
IC	-0.763	0.268	0.526	-0.642	0.367	-0.969	-0.368	0.511	-3.156	0.172	0.734	-3.683	0.460	0.104	8.976
<i>PVGO</i>															
IC	-0.001	0.952	-3.837	0.028	0.223	5.173	0.058	0.183	10.485	0.061	0.270	8.564	0.084	0.123	18.022

*Panel B: Expansion*

30 days				91 days			182 days			273 days			365 days						
$\beta$	$p-val$	$R^2$		$\beta$	$p-val$	$R^2$		$\beta$	$p-val$	$R^2$		$\beta$	$p-val$	$R^2$					
<i>MABA</i>																			
IC	0.147	0.191	0.055		0.361	0.004	6.966		0.793	0.005	14.523		1.134	0.016	18.247		1.560	0.016	21.322
<i>Q</i>																			
IC	0.210	0.094	0.327		0.432	0.002	7.303		0.895	0.004	14.158		1.287	0.014	18.069		1.791	0.013	21.414
<i>DTE</i>																			
IC	0.203	0.292	-0.139		-0.170	0.025	3.494		-0.355	0.010	7.512		-0.466	0.037	8.659		-0.505	0.113	6.859
<i>CAPEX</i>																			
IC	-0.037	0.795	-0.412		0.008	0.968	-0.427		-0.051	0.840	-0.412		0.269	0.297	-0.016		0.568	0.025	8.560
<i>PVGO</i>																			
IC	0.001	0.777	-0.404		0.011	0.000	8.651		0.019	0.000	10.726		0.025	0.001	13.029		0.029	0.001	11.129

**Table AI104** Insample Factor Return Predictability – RC – Full Sample

The table shows the slope and the  $R^2$ s of the regressions of the excess market and value factor returns realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on realized correlations ( $RC$ ) for the S&P500 Index. Realized correlation are obtained via Eq. (25) and calculated from daily realized returns over a respective backward-looking window, corresponding to the predictive horizon. The sample period ranges from 01/1965 to 12/2018 for realized correlations, the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>MKTRF</i>					
RC	0.023 (0.050)	0.128 (0.000)	0.223 (0.002)	0.262 (0.016)	0.381 (0.005)
$R^2$	0.444	3.525	4.517	3.942	6.168
<i>HML</i>					
RC	-0.017 (0.023)	-0.070 (0.010)	-0.062 (0.228)	-0.092 (0.268)	-0.154 (0.171)
$R^2$	0.624	2.158	0.670	0.853	1.660
<i>HML*</i>					
RC	-0.016 (0.014)	-0.066 (0.005)	-0.094 (0.059)	-0.145 (0.070)	-0.218 (0.042)
$R^2$	0.761	2.339	1.986	2.889	4.437

**Table AI105** Insample Factor Long- and Short Leg Return Predictability – RC – Full Sample

The table shows the slope and the  $R^2$ s of the regressions of the long- and short value factor returns ( $H, L, H^*, L^*$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on realized correlations ( $RC$ ) for the S&P500 Index. Realized correlations  $RC$  are obtained via Eq.(25) and calculated from daily realized returns over a respective backward-looking window, corresponding to the predictive horizon. The sample period ranges from 01/1965 to 12/2018 for realized correlations, the variables are sampled at daily frequency. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>H</i>					
RC	0.002 (0.894)	0.088 (0.069)	0.180 (0.050)	0.169 (0.219)	0.237 (0.162)
$R^2$	-0.005	1.146	2.014	1.144	1.653
<i>L</i>					
RC	0.019 (0.162)	0.155 (0.000)	0.235 (0.005)	0.248 (0.047)	0.372 (0.014)
$R^2$	0.202	3.119	3.076	2.186	3.689
<i>H*</i>					
RC	-0.021 (0.000)	-0.046 (0.050)	-0.101 (0.044)	-0.183 (0.021)	-0.273 (0.016)
$R^2$	1.665	1.423	2.638	4.777	6.774
<i>L*</i>					
RC	-0.005 (0.282)	0.018 (0.192)	-0.012 (0.671)	-0.041 (0.297)	-0.055 (0.328)
$R^2$	0.123	0.359	0.061	0.501	0.597

**Table AI106** Insample Factor Return Predictability – RC – Contraction and Expansion

The table shows the slope and the  $R^2$ s of the regressions of the excess market- and value factor returns realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on realized correlations ( $RC$ ) for the S&P500 index. Realized correlation  $RC$  is obtained via Eq. (25) and calculated from daily realized returns over a respective window, corresponding to the predictive horizon. The sample period ranges from 01/1965 to 12/2018 for realized correlations, the variables are sampled at daily frequency. The sample is divided into contraction and expansion according to the manifestation of the NBER Recession Indicator, see Appendix I.D. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

*Panel A: Contraction*

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>MKTRF</i>					
RC	0.001 (0.991)	0.178 (0.263)	0.558 (0.019)	0.516 (0.157)	0.563 (0.171)
$R^2$	-0.053	2.163	8.115	4.777	4.918
<i>HML</i>					
RC	-0.058 (0.088)	-0.239 (0.017)	-0.121 (0.525)	-0.069 (0.737)	-0.098 (0.694)
$R^2$	2.807	12.800	1.593	0.384	0.746
<i>HML*</i>					
RC	-0.043 (0.105)	-0.245 (0.000)	-0.242 (0.015)	-0.303 (0.014)	-0.411 (0.000)
$R^2$	2.190	17.303	11.498	15.397	24.721

*Panel B: Expansion*

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>MKTRF</i>					
RC	0.033 (0.001)	0.139 (0.000)	0.190 (0.001)	0.231 (0.008)	0.354 (0.004)
$R^2$	1.169	5.488	4.701	4.242	6.733
<i>HML</i>					
RC	-0.014 (0.039)	-0.052 (0.033)	-0.053 (0.296)	-0.088 (0.315)	-0.157 (0.198)
$R^2$	0.468	1.318	0.512	0.776	1.634
<i>HML*</i>					
RC	-0.014 (0.026)	-0.043 (0.059)	-0.069 (0.174)	-0.115 (0.177)	-0.181 (0.108)
$R^2$	0.608	1.088	1.048	1.695	2.872

**Table AI107** Insample Factor Return Predictability – IC – Contraction and Expansion

The table shows the slope and the  $R^2$ s of the regressions of the excess market- and value factor returns realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) for the S&P500 index. Implied correlations are computed applying Eq. (25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. The sample period ranges from 01/1996 to 12/2018 when considering implied correlations. The variables are sampled at daily frequency. The sample is divided into contraction and expansion according to the manifestation of the NBER Recession Indicator, see Appendix I.D. The market neutral returns are estimated applying Eq. (26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

*Panel A: Contraction*

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>MKTRF</i>					
IC	0.078 (0.378)	0.491 (0.059)	0.830 (0.080)	0.918 (0.275)	1.536 (0.064)
$R^2$	1.177	15.109	18.088	15.194	32.010
<i>HML</i>					
IC	-0.124 (0.051)	-0.227 (0.173)	-0.062 (0.609)	-0.068 (0.721)	-0.185 (0.563)
$R^2$	8.265	8.369	0.212	0.250	3.076
<i>HML*</i>					
IC	-0.154 (0.001)	-0.403 (0.009)	-0.339 (0.140)	-0.346 (0.167)	-0.545 (0.000)
$R^2$	14.186	22.488	10.297	10.791	37.946

*Panel B: Expansion*

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
<i>MKTRF</i>					
IC	0.064 (0.000)	0.217 (0.000)	0.416 (0.000)	0.582 (0.000)	0.719 (0.003)
$R^2$	3.891	12.806	20.350	23.934	21.423
<i>HML</i>					
IC	-0.032 (0.024)	-0.140 (0.011)	-0.357 (0.019)	-0.555 (0.035)	-0.797 (0.033)
$R^2$	1.969	7.826	16.528	20.433	24.910
<i>HML*</i>					
IC	-0.026 (0.026)	-0.101 (0.008)	-0.263 (0.005)	-0.407 (0.011)	-0.589 (0.008)
$R^2$	1.691	5.063	11.833	15.348	19.133



**Table AI108** Insample Factor Leg Return Predictability – RC – Contraction and Expansion

The table shows the slope and the  $R^2$ s of the regressions of the long- and short value factor returns ( $H, L, H^*, L^*$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on realized correlation ( $RC$ ) for the S&P500 index. Realized correlation  $RC$  is obtained via Eq. (25) and calculated from daily realized returns over a respective window, corresponding to the predictive horizon. Thereby  $H, L, H^*, L^*$  represent the return on portfolios with high (low) book-to-market ratio. Realized variance  $RV$  is calculated on each day from daily returns over a respective window, corresponding to the maturity of  $MFIV$ . The sample period ranges from 01/1965 to 12/2017, and the variables are sampled at daily frequency. The sample is divided into contraction and expansion according to the manifestation of the NBER Recession Indicator, see Appendix I.D. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

*Panel A: Contraction*

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
$H$					
RC	-0.051 (0.524)	0.043 (0.858)	0.556 (0.100)	0.423 (0.370)	0.360 (0.540)
$R^2$	0.501	0.043	6.067	2.415	1.259
$L$					
RC	0.005 (0.934)	0.271 (0.145)	0.644 (0.029)	0.469 (0.221)	0.442 (0.308)
$R^2$	-0.047	3.217	6.789	2.421	1.812
$H^*$					
RC	-0.046 (0.053)	-0.171 (0.011)	-0.209 (0.082)	-0.369 (0.021)	-0.542 (0.011)
$R^2$	3.065	10.556	9.778	19.305	23.609
$L^*$					
RC	-0.003 (0.854)	0.073 (0.054)	0.032 (0.682)	-0.061 (0.567)	-0.120 (0.458)
$R^2$	-0.024	3.978	0.310	0.786	2.122

*Panel B: Expansion*

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
$H$					
RC	0.013 (0.288)	0.102 (0.005)	0.124 (0.080)	0.119 (0.286)	0.191 (0.231)
$R^2$	0.139	1.974	1.303	0.745	1.438
$L$					
RC	0.027 (0.034)	0.150 (0.000)	0.168 (0.020)	0.188 (0.078)	0.326 (0.022)
$R^2$	0.501	3.769	2.247	1.768	3.729
$H^*$					
RC	-0.020 (0.000)	-0.037 (0.117)	-0.102 (0.059)	-0.178 (0.043)	-0.258 (0.036)
$R^2$	1.801	1.007	2.656	4.380	6.065
$L^*$					
RC	-0.006 (0.150)	0.003 (0.815)	-0.038 (0.166)	-0.067 (0.092)	-0.076 (0.188)
$R^2$	0.255	0.005	0.771	1.447	1.292

**Table AI109** Insample Factor Leg Return Predictability – IC – Contraction and Expansion

The table shows the slope and the  $R^2$ s of the regressions of the long- and short value factor returns ( $H, L, H^*, L^*$ ) realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlation ( $IC$ ) for the S&P500 index. Implied correlations are computed applying Eq. (25) to model-free implied variances ( $MFIV$ ) using out-of-the money options with the respective maturity. Thereby  $H, L, H^*, L^*$  represent the return on portfolios with high (low) book-to-market ratio. Model-free implied variance ( $MFIV$ ) is computed on each day using out-of-the money options with the respective maturity. The sample period ranges from 01/1996 to 12/2017, and the variables are sampled at daily frequency. The sample is divided into contraction and expansion according to the manifestation of the NBER Recession Indicator, see Appendix I.D. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The p-values (under the slope) are computed with Newey and West (1987) standard errors.

*Panel A: Contraction*

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
$H$					
IC	-0.042 (0.752)	0.314 (0.431)	0.776 (0.171)	0.850 (0.420)	1.501 (0.194)
$R^2$	0.044	3.207	9.493	8.192	18.627
$L$					
IC	0.081 (0.405)	0.551 (0.051)	0.906 (0.059)	0.984 (0.256)	1.669 (0.040)
$R^2$	1.047	15.437	20.494	16.703	36.080
$H^*$					
IC	-0.152 (0.001)	-0.327 (0.014)	-0.274 (0.116)	-0.321 (0.115)	-0.478 (0.000)
$R^2$	19.254	21.802	8.767	11.748	34.636
$L^*$					
IC	0.001 (0.958)	0.078 (0.206)	0.074 (0.314)	0.043 (0.667)	0.089 (0.051)
$R^2$	-0.167	5.500	5.042	1.424	14.016

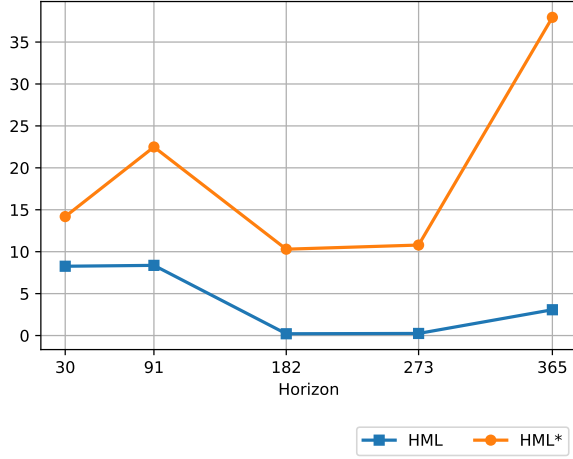
*Panel B: Expansion*

	Return, 30 days	Return, 91 days	Return, 182 days	Return, 273 days	Return, 365 days
$H$					
IC	0.030 (0.090)	0.083 (0.077)	0.078 (0.439)	0.071 (0.658)	-0.014 (0.953)
$R^2$	0.633	1.282	0.460	0.216	-0.015
$L$					
IC	0.062 (0.003)	0.223 (0.000)	0.426 (0.000)	0.586 (0.002)	0.715 (0.010)
$R^2$	2.427	8.632	14.387	16.624	15.671
$H^*$					
IC	-0.032 (0.000)	-0.112 (0.001)	-0.304 (0.001)	-0.483 (0.001)	-0.715 (0.001)
$R^2$	3.689	8.158	19.981	25.770	31.357
$L^*$					
IC	-0.007 (0.366)	-0.012 (0.564)	-0.038 (0.179)	-0.072 (0.077)	-0.109 (0.041)
$R^2$	0.279	0.170	0.725	1.459	2.289

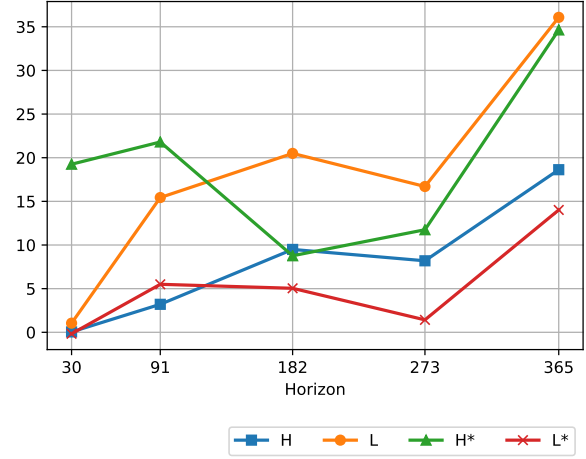
**Figure AI1.** Predictive: Insample Factor Returns – Expansion and Contraction

The figure shows the  $R^2$ s of the regressions of the value factor returns ( $HML$ ,  $HML^*$ ) and the individual long- and short legs returns of the factors ( $H$ ,  $L$ ,  $H^*$ ,  $L^*$ ), realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations ( $IC$ ) for the S&P500 index from matching-maturity options. The sample period is from 01/1996 to 12/2017, and the variables are sampled at daily frequency. The relevant data for contraction and expansion are defined based on the NBER based Recession Indicator. The market neutral returns are estimated applying Eq.(26) to the factor data, which is obtained from Kenneth French's Website.

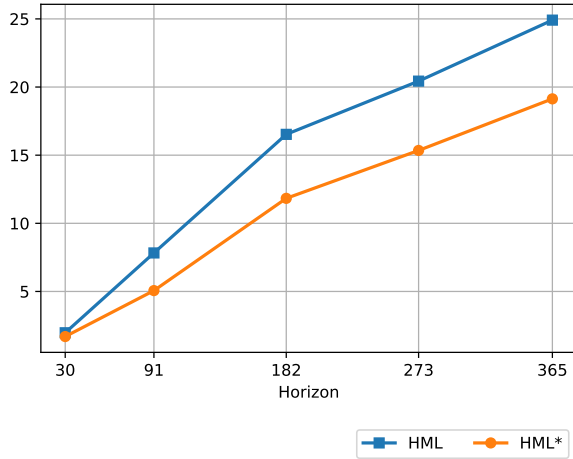
*A:  $R^2$  - factors - Contraction*



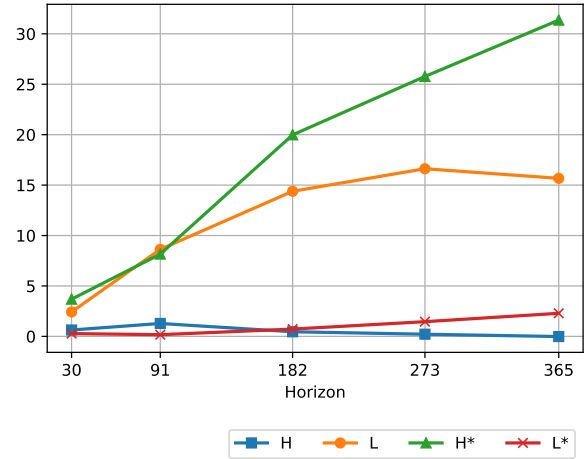
*B:  $R^2$  - legs of the factors - Contraction*



*C:  $R^2$  - factors - Expansion*



*D:  $R^2$  - legs of the factors - Expansion*



**Table AI110** Insample Factor Return Predictability with Controls

The table shows the slope and the  $R^2$ s of the regressions of the excess market- and value factor returns realized over a future horizon of 30, 91, 182, 273, and 365 calendar days on implied correlations ( $IC$ ) and the variance premium ( $VRP = MFIV - RV$ ) for the S&P500 index. Model-free implied variance ( $MFIV$ ) is computed on each day using out-of-the money options with the respective maturity, and realized variance  $RV$  is calculated on each day from daily returns over a respective window, corresponding to the maturity of  $MFIV$ . The sample period is from 01/1996 to 12/2017, and the variables are sampled at monthly frequency. The Earnings Price Ratio (EP), the Term Spread (TMS), the Default Yield Spread (DFY), the Book-to-Market Ratio (BTM), and the Net Equity Expansion (NTIS) are constructed from the data and the procedures from the study of Goyal and Welch (2008). The market neutral returns are estimated applying equation (26) to the factor data, which is obtained from Kenneth French's Website. The intercept is not shown. The  $p$ -values (under the slope) are computed with Newey and West (1987) standard errors.

	Return, 30 days			Return, 91 days			Return, 182 days			Return, 273 days			Return, 365 days		
<i>MKTRF</i>															
IC	0.057 (0.011)	0.087 (0.001)	0.051 (0.030)	0.229 (0.000)	0.329 (0.000)	0.215 (0.000)	0.509 (0.000)	0.629 (0.000)	0.398 (0.000)	0.747 (0.000)	0.802 (0.000)	0.542 (0.000)	0.926 (0.000)	0.850 (0.000)	0.649 (0.000)
VRP	0.355 (0.001)	- (0.001)	- (0.001)	0.554 (0.002)	- (0.002)	- (0.002)	-0.450 (0.247)	- (0.247)	- (0.247)	-0.860 (0.036)	- (0.036)	- (0.036)	-0.872 (0.116)	- (0.116)	- (0.116)
EP12	- (0.546)	-0.006 (0.546)	- (0.546)	- (0.227)	-0.027 (0.227)	- (0.227)	- (0.160)	-0.051 (0.160)	- (0.160)	- (0.334)	-0.046 (0.334)	- (0.334)	- (0.919)	-0.006 (0.919)	- (0.919)
TMS	- (0.494)	-0.148 (0.494)	- (0.494)	- (0.225)	-0.692 (0.225)	- (0.225)	- (0.245)	-1.259 (0.245)	- (0.245)	- (0.562)	-0.812 (0.562)	- (0.562)	- (0.726)	0.572 (0.726)	- (0.726)
DFY	- (0.112)	-1.716 (0.112)	- (0.112)	- (0.145)	-4.067 (0.145)	- (0.145)	- (0.306)	-4.041 (0.306)	- (0.306)	- (0.671)	-2.155 (0.671)	- (0.671)	- (0.895)	0.747 (0.895)	- (0.895)
BM	- (0.342)	- (0.342)	0.042 (0.342)	- (0.237)	- (0.237)	0.112 (0.237)	- (0.038)	- (0.038)	0.319 (0.038)	- (0.016)	- (0.016)	0.522 (0.016)	- (0.014)	- (0.014)	0.729 (0.014)
NTIS	- (0.267)	- (0.267)	0.221 (0.267)	- (0.154)	- (0.154)	0.814 (0.154)	- (0.086)	- (0.086)	1.724 (0.086)	- (0.095)	- (0.095)	2.355 (0.095)	- (0.084)	- (0.084)	2.901 (0.084)
<i>R</i> <sup>2</sup>	9.785	3.558	2.790	16.410	15.996	15.472	21.529	23.486	28.501	26.638	25.013	34.504	25.784	23.958	36.278
<i>HML</i>															
IC	-0.048 (0.004)	-0.039 (0.014)	-0.039 (0.009)	-0.160 (0.003)	-0.142 (0.004)	-0.130 (0.008)	-0.303 (0.022)	-0.336 (0.014)	-0.310 (0.021)	-0.457 (0.051)	-0.539 (0.016)	-0.518 (0.029)	-0.720 (0.033)	-0.860 (0.005)	-0.787 (0.018)
VRP	0.088 (0.055)	- (0.055)	- (0.055)	0.318 (0.056)	- (0.056)	- (0.056)	-0.860 (0.000)	- (0.000)	- (0.000)	-1.032 (0.000)	- (0.000)	- (0.000)	-0.693 (0.102)	- (0.102)	- (0.102)
EP12	- (0.205)	-0.009 (0.205)	- (0.205)	- (0.316)	-0.018 (0.316)	- (0.316)	- (0.817)	-0.008 (0.817)	- (0.817)	- (0.905)	0.006 (0.905)	- (0.905)	- (0.650)	0.028 (0.650)	- (0.650)
TMS	- (0.779)	-0.046 (0.779)	- (0.779)	- (0.811)	-0.105 (0.811)	- (0.811)	- (0.680)	-0.378 (0.680)	- (0.680)	- (0.672)	-0.606 (0.672)	- (0.672)	- (0.869)	-0.296 (0.869)	- (0.869)
DFY	- (0.506)	-0.600 (0.506)	- (0.506)	- (0.856)	-0.409 (0.856)	- (0.856)	- (0.514)	2.315 (0.514)	- (0.514)	- (0.218)	5.116 (0.218)	- (0.218)	- (0.121)	7.625 (0.121)	- (0.121)
BM	- (0.187)	- (0.187)	-0.042 (0.187)	- (0.234)	- (0.234)	-0.093 (0.234)	- (0.698)	- (0.698)	-0.063 (0.698)	- (0.887)	- (0.887)	0.033 (0.887)	- (0.789)	- (0.789)	0.073 (0.789)
NTIS	- (0.434)	- (0.434)	-0.093 (0.434)	- (0.520)	- (0.520)	-0.212 (0.520)	- (0.596)	- (0.596)	-0.303 (0.596)	- (0.811)	- (0.811)	-0.184 (0.811)	- (0.899)	- (0.899)	-0.115 (0.899)
<i>R</i> <sup>2</sup>	3.979	3.114	3.486	10.803	8.595	9.085	19.620	14.660	14.005	22.267	19.515	17.493	25.713	26.855	24.218
<i>HML</i> <sup>*</sup>															
IC	-0.039 (0.002)	-0.027 (0.047)	-0.032 (0.011)	-0.140 (0.000)	-0.109 (0.010)	-0.107 (0.003)	-0.285 (0.001)	-0.268 (0.006)	-0.245 (0.011)	-0.410 (0.004)	-0.409 (0.003)	-0.391 (0.014)	-0.608 (0.002)	-0.631 (0.001)	-0.602 (0.005)
VRP	0.030 (0.726)	- (0.726)	- (0.726)	0.294 (0.001)	- (0.001)	- (0.001)	-0.028 (0.915)	- (0.915)	- (0.915)	-0.139 (0.601)	- (0.601)	- (0.601)	-0.033 (0.918)	- (0.918)	- (0.918)
EP12	- (0.958)	0.000 (0.958)	- (0.958)	- (0.697)	0.006 (0.697)	- (0.697)	- (0.413)	0.023 (0.413)	- (0.413)	- (0.330)	0.041 (0.330)	- (0.330)	- (0.245)	0.061 (0.245)	- (0.245)
TMS	- (0.535)	-0.080 (0.535)	- (0.535)	- (0.548)	-0.229 (0.548)	- (0.548)	- (0.699)	-0.317 (0.699)	- (0.699)	- (0.684)	-0.501 (0.684)	- (0.684)	- (0.859)	-0.282 (0.859)	- (0.859)
DFY	- (0.258)	-0.715 (0.258)	- (0.258)	- (0.477)	-1.120 (0.477)	- (0.477)	- (0.727)	-1.016 (0.727)	- (0.727)	- (0.910)	-0.402 (0.910)	- (0.910)	- (0.961)	0.213 (0.961)	- (0.961)
BM	- (0.158)	- (0.158)	-0.036 (0.158)	- (0.119)	- (0.119)	-0.108 (0.119)	- (0.432)	- (0.432)	-0.123 (0.432)	- (0.805)	- (0.805)	-0.054 (0.805)	- (0.949)	- (0.949)	0.017 (0.949)
NTIS	- (0.758)	- (0.758)	-0.038 (0.758)	- (0.671)	- (0.671)	-0.147 (0.671)	- (0.849)	- (0.849)	-0.103 (0.849)	- (0.800)	- (0.800)	0.182 (0.800)	- (0.447)	- (0.447)	0.587 (0.447)
<i>R</i> <sup>2</sup>	2.870	3.358	3.060	9.633	8.154	8.377	13.050	14.915	13.493	16.556	19.170	16.390	22.253	25.338	22.717